

# Amorphous Ices

## Part 2: Dynamics



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# Collaboration

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Catalin Gainaru, Roland Böhmer

Florian Löw, Carolin Wittich, Franz Fujara

Burkhard Geil

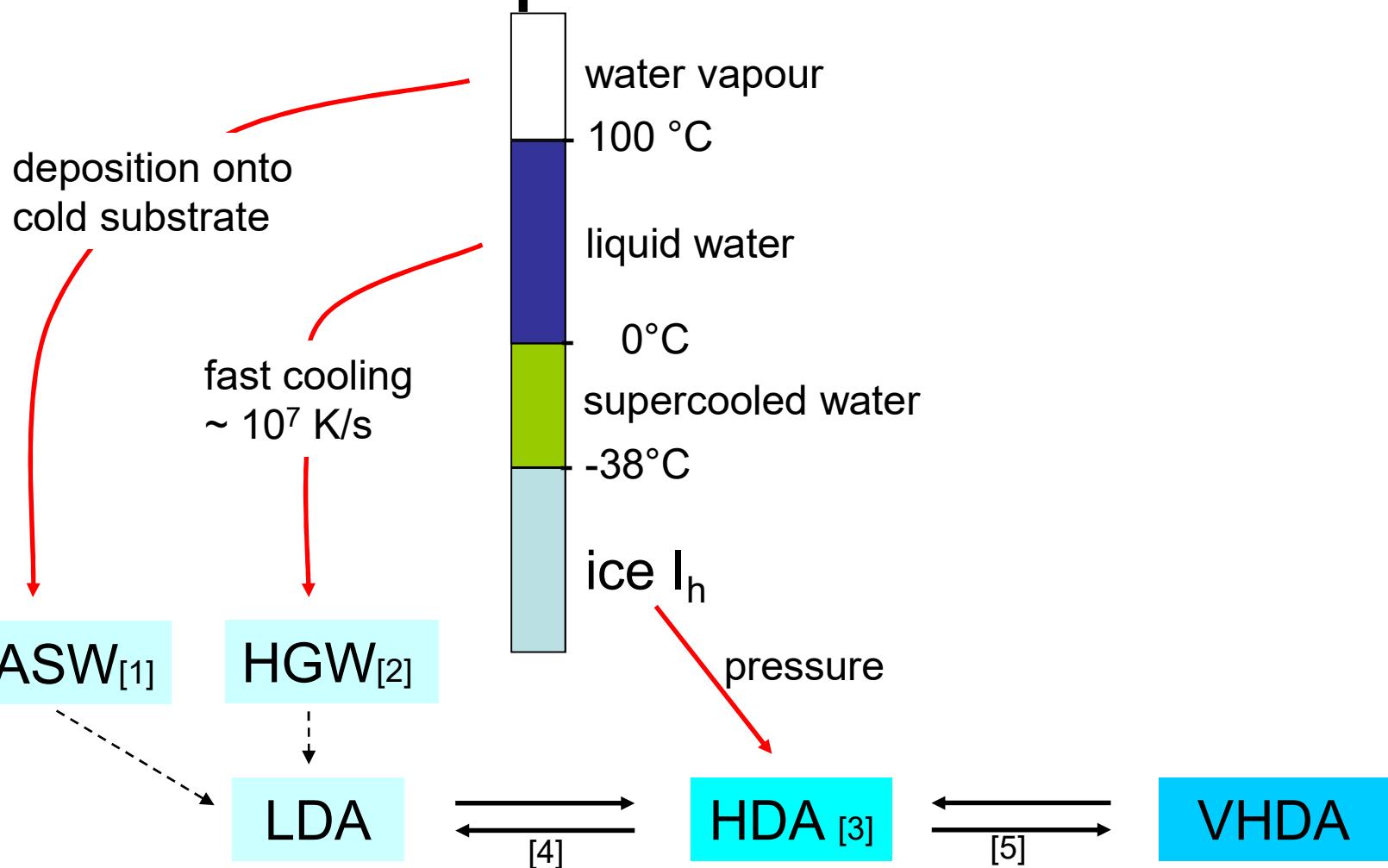
Nicolas Giovambattista

Boris R. Lukanov, Francis W. Starr

Martin Jehser, Clemens Rauer, Gerhard Zifferer  
Marius, Reinecker, Wilfried Schranz



# Amorphous ice



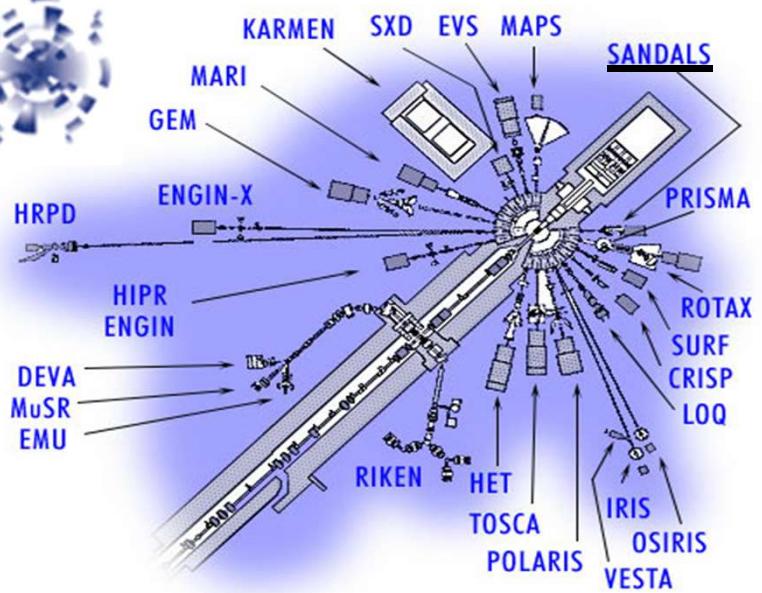
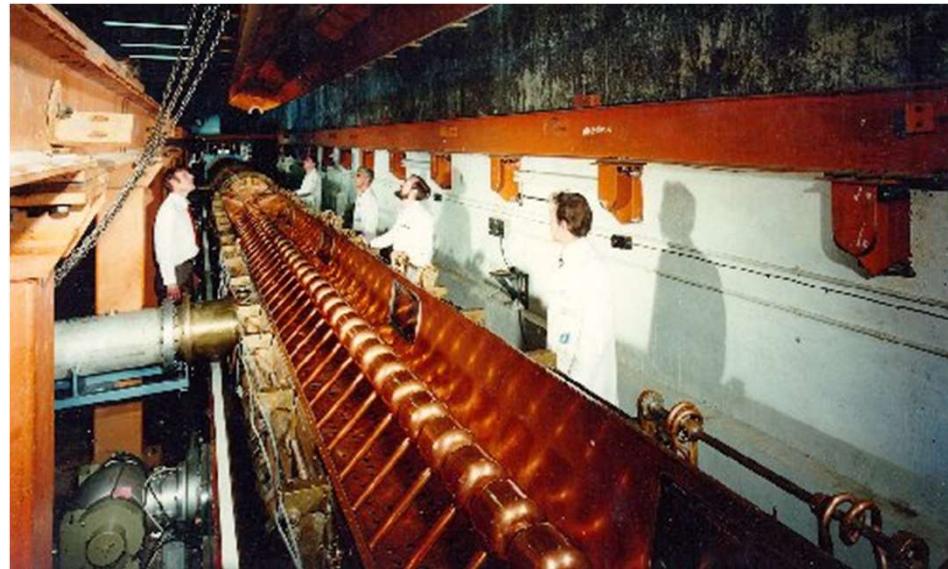
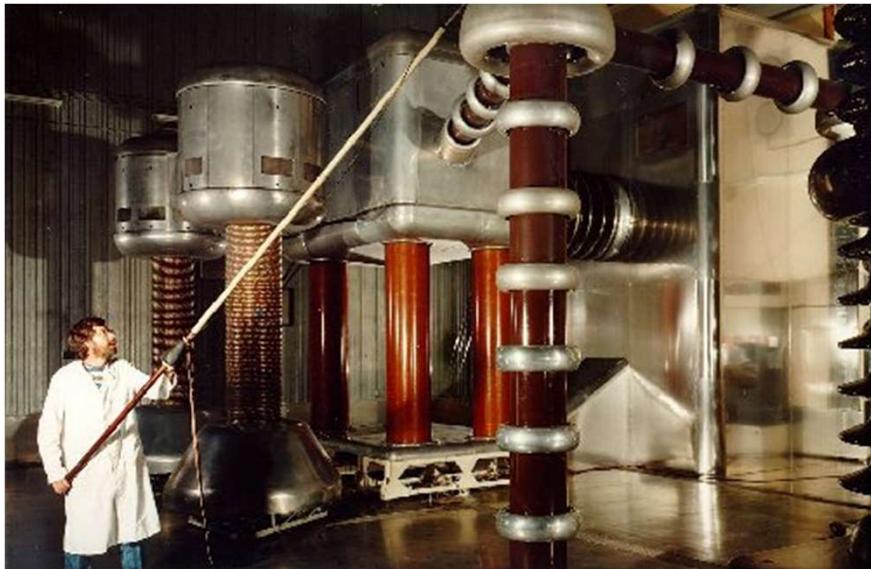
[1] E.F. Burton and W.F. Oliver, *Proc. R. Soc. A*, 153, 1935

[2] P. Brüggele, E. Mayer, *Nature*, 288, 1980; E. Mayer, *J. Appl. Phys.*, 58, 1985

[3] O. Mishima, L.D. Calvert, E. Whalley, *Nature*, 310, 1984;

[4] O. Mishima, L.D. Calvert, E. Whalley, *Nature*, 314, 1985

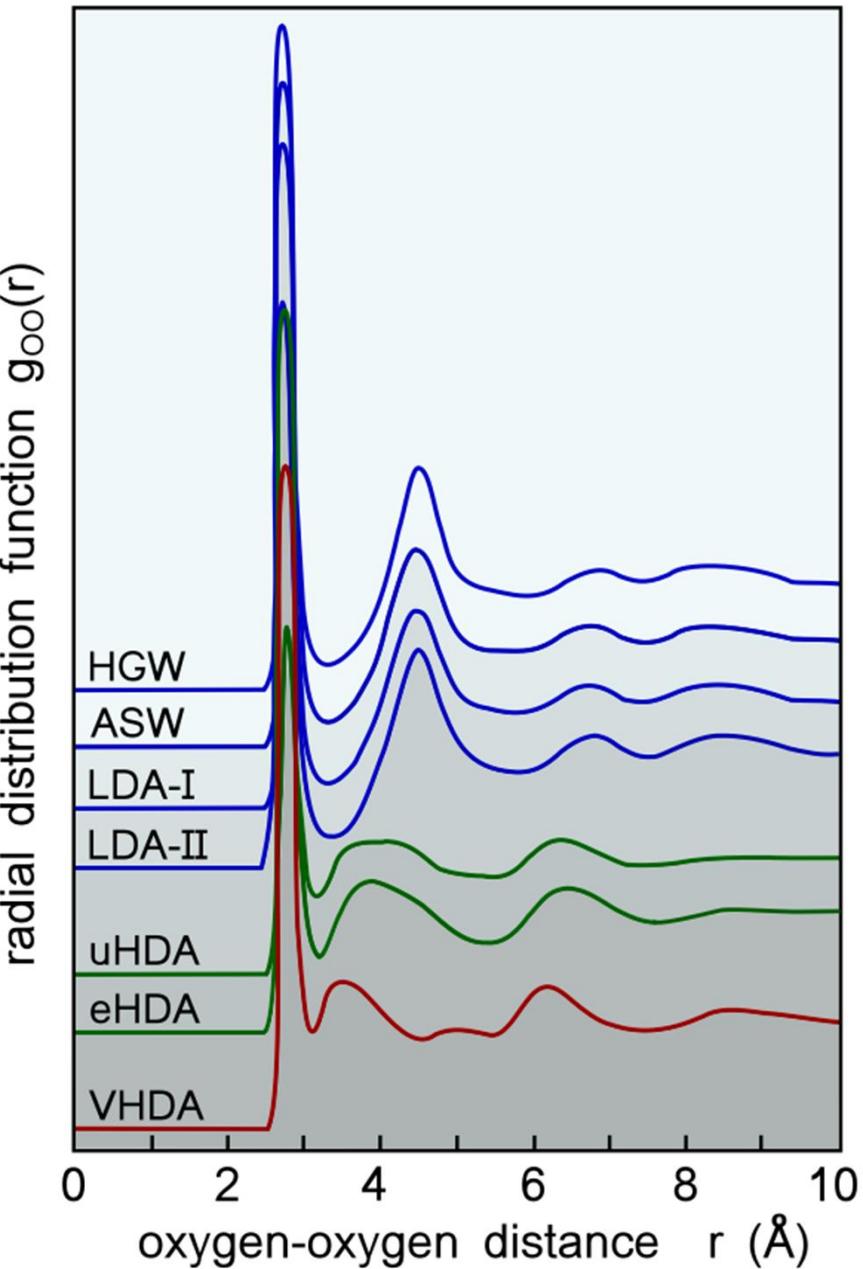
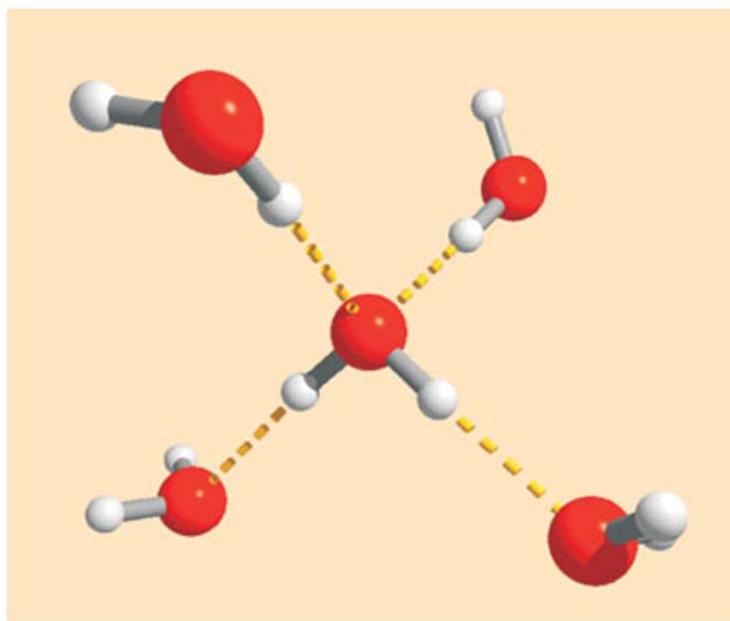
[5] T. Loerting, C. Salzmann, I. Kohl, E. Mayer, A. Hallbrucker, *PCCP*, 3, 2001



**SANDALS -**  
**Small Angle Neutron Diffractometer**  
**for**  
**Amorphous and Liquid Samples**

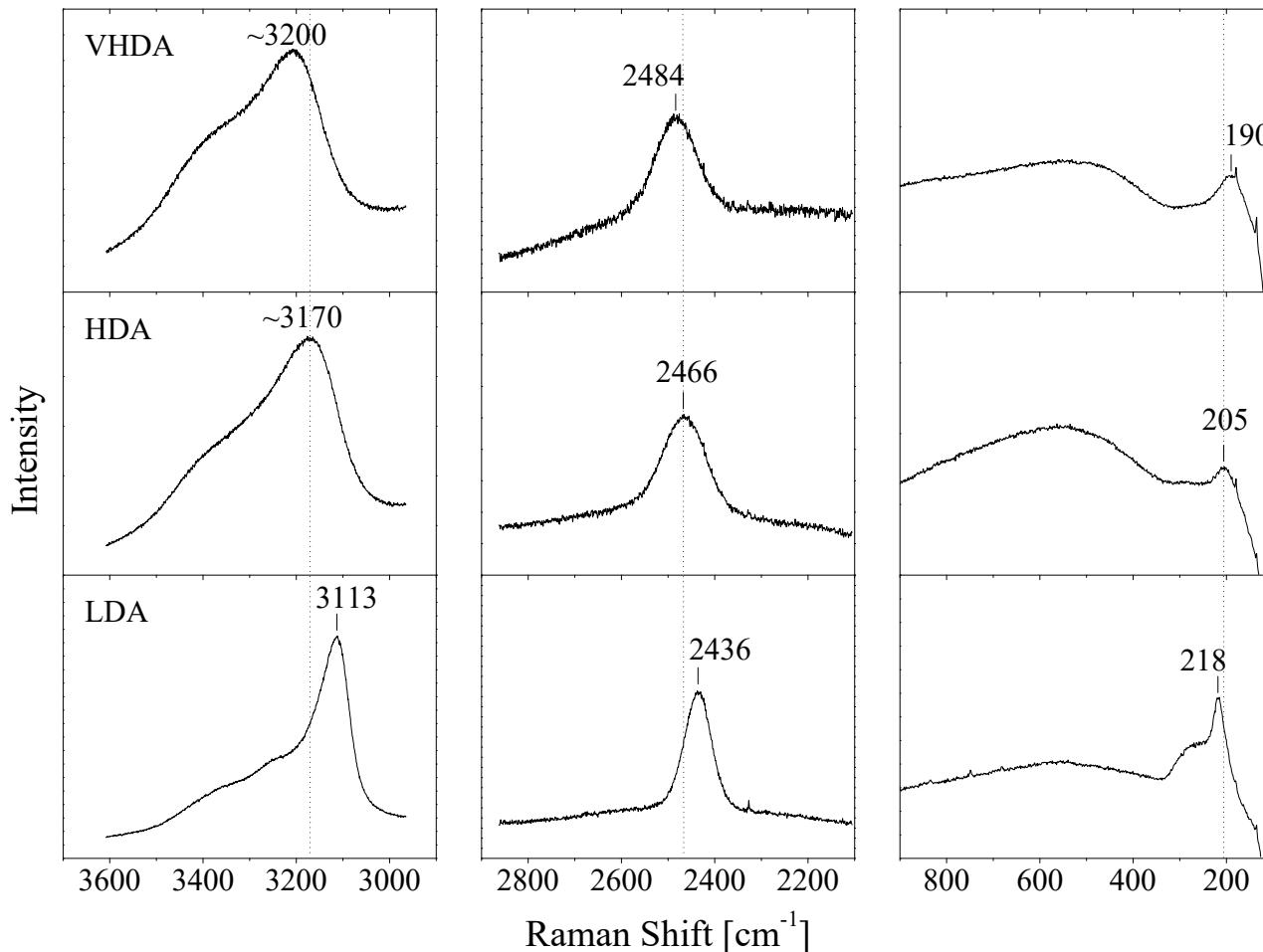
## Radial-Density Functions (rdfs)

Coordination-Number:	
$\text{H}_2\text{O}_{(l)}$	4.3
hex. Ice	3.7
<b>LDA</b>	<b>3.9</b>
<b>HDA</b>	<b>5.0</b>
<b>VHDA</b>	<b>5.9</b>



D. T. Bowron, J.L. Finney, A. Hallbrucker, I. Kohl, T. Loerting, E. Mayer, A. K. Soper, *J. Chem. Phys.* **125**, 194502 (2006)  
J. L. Finney, Daniel T. Bowron, A. K. Soper, E. Mayer, A. Hallbrucker, T. Loerting, *Phys. Rev. Lett.* **89**, 205503(2002)

# Raman-Spectroscopy (77 K)



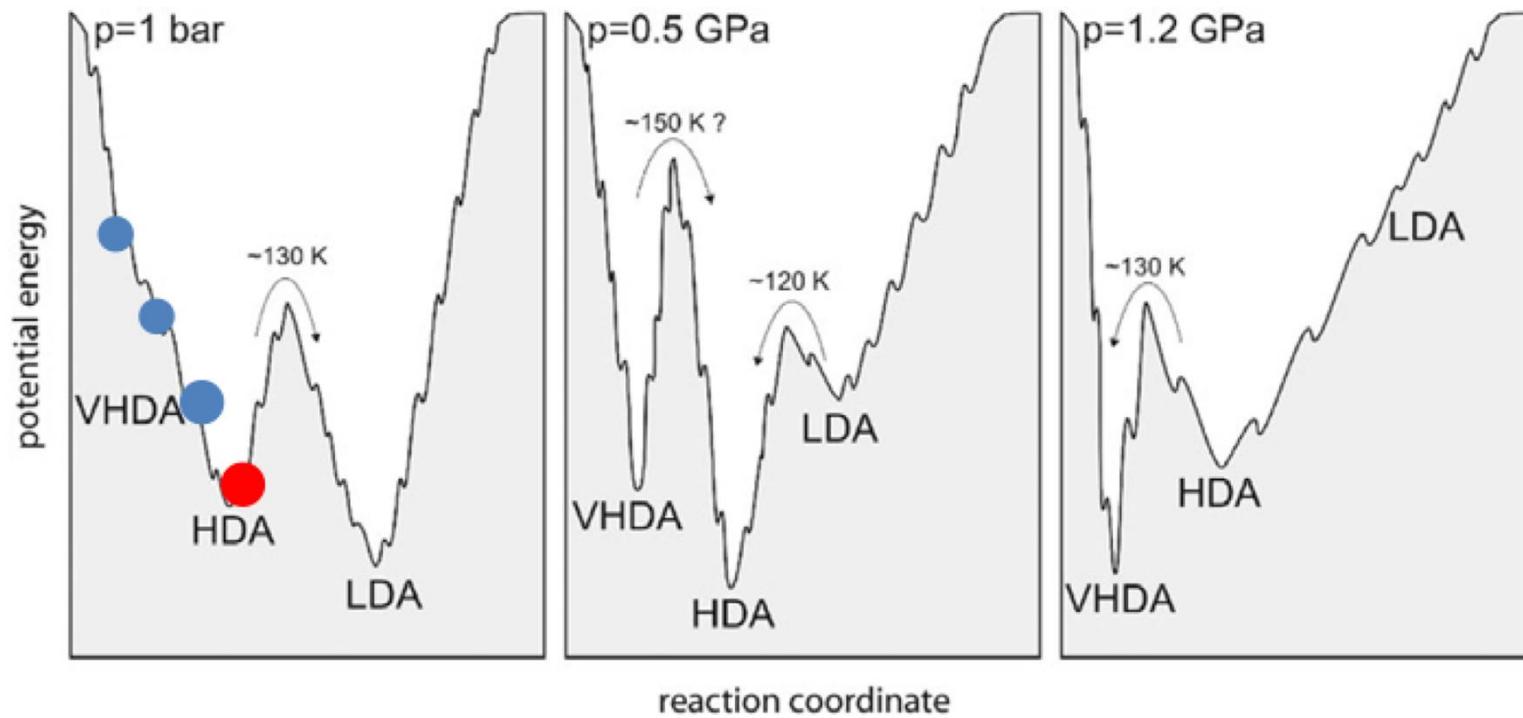
O - D ... O distances:

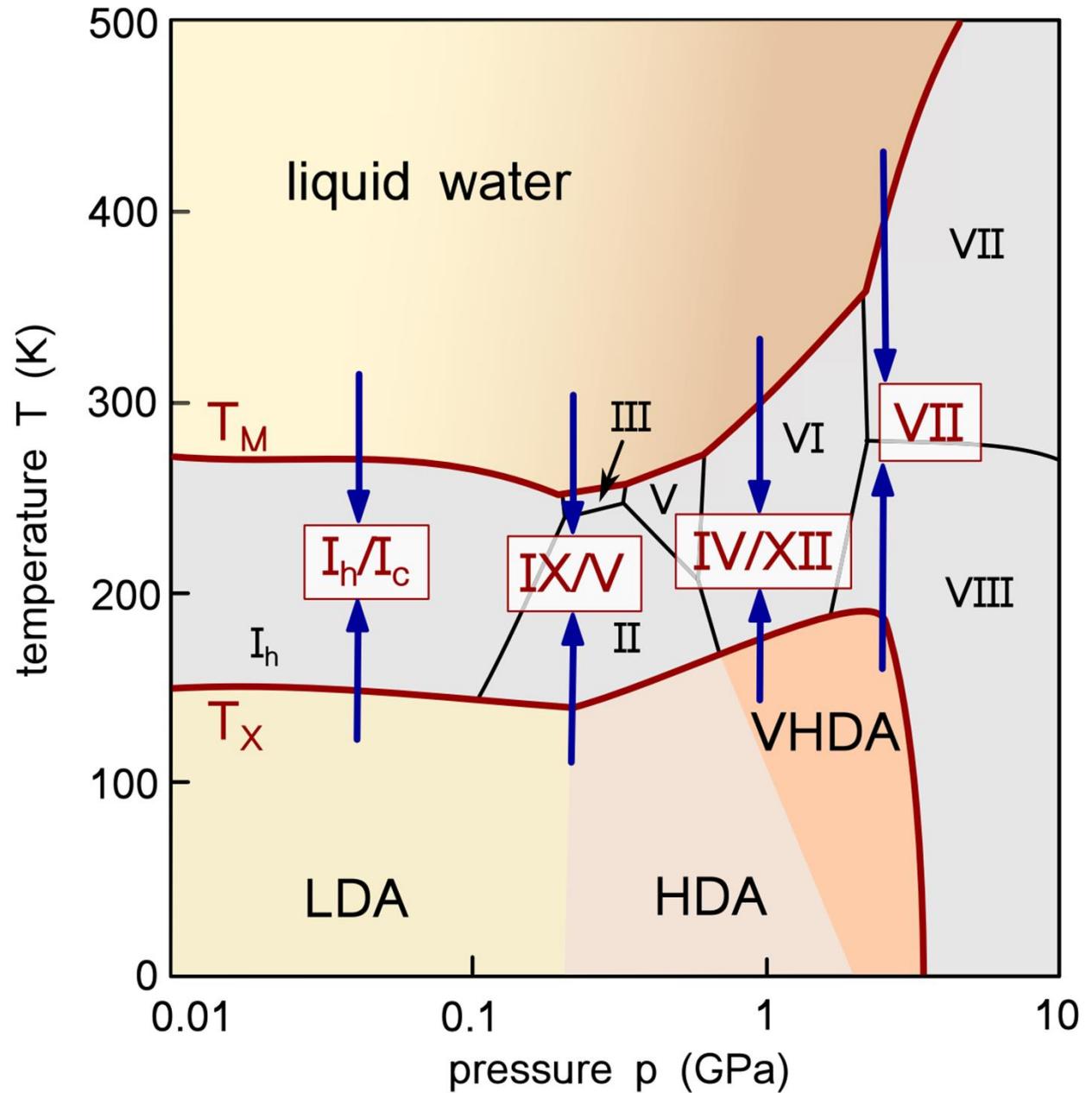
LDA: 2.77 Å

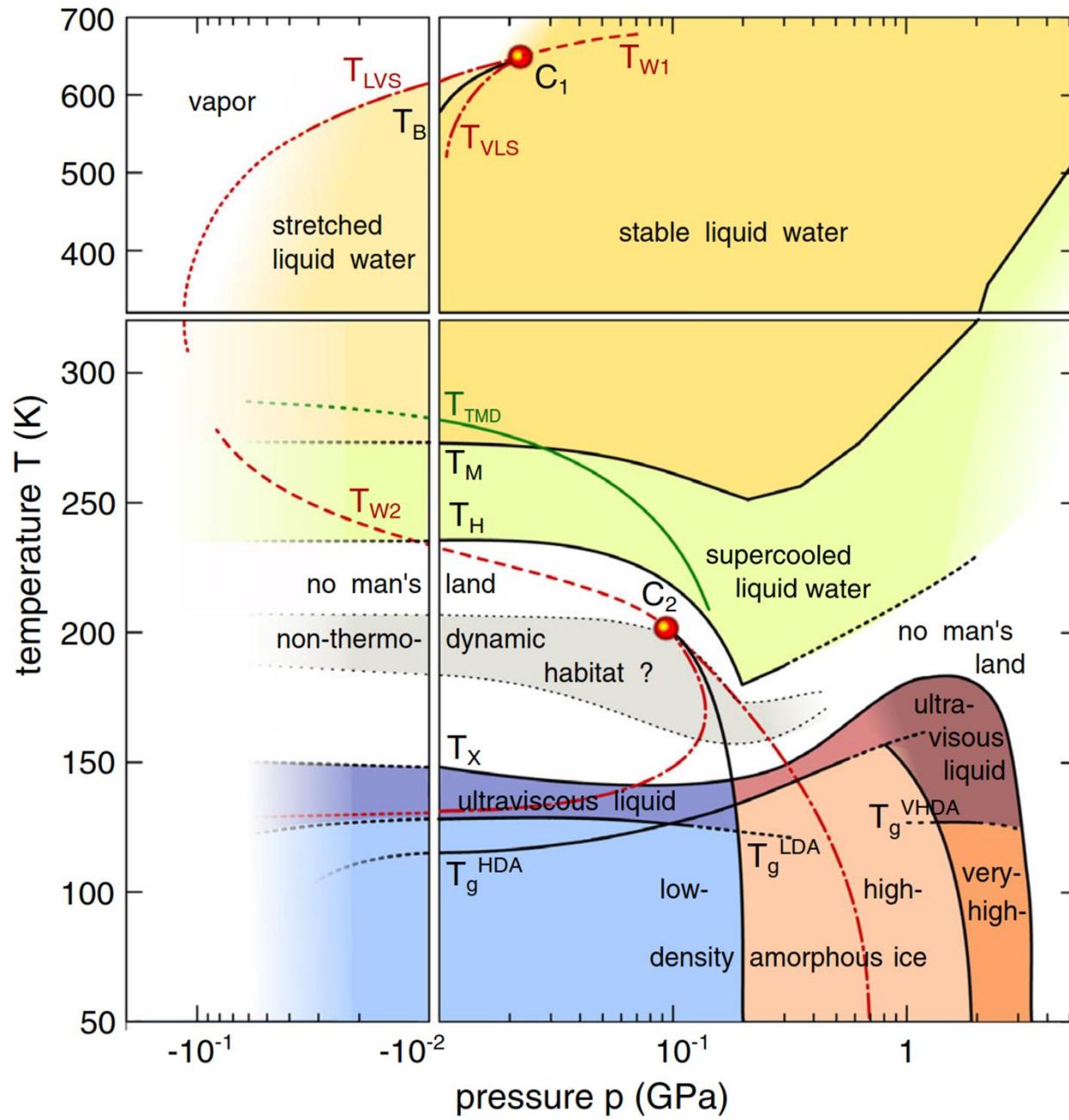
HDA: 2.82 Å

VHDA: 2.85 Å

# Relaxing amorphous ices at different pressures





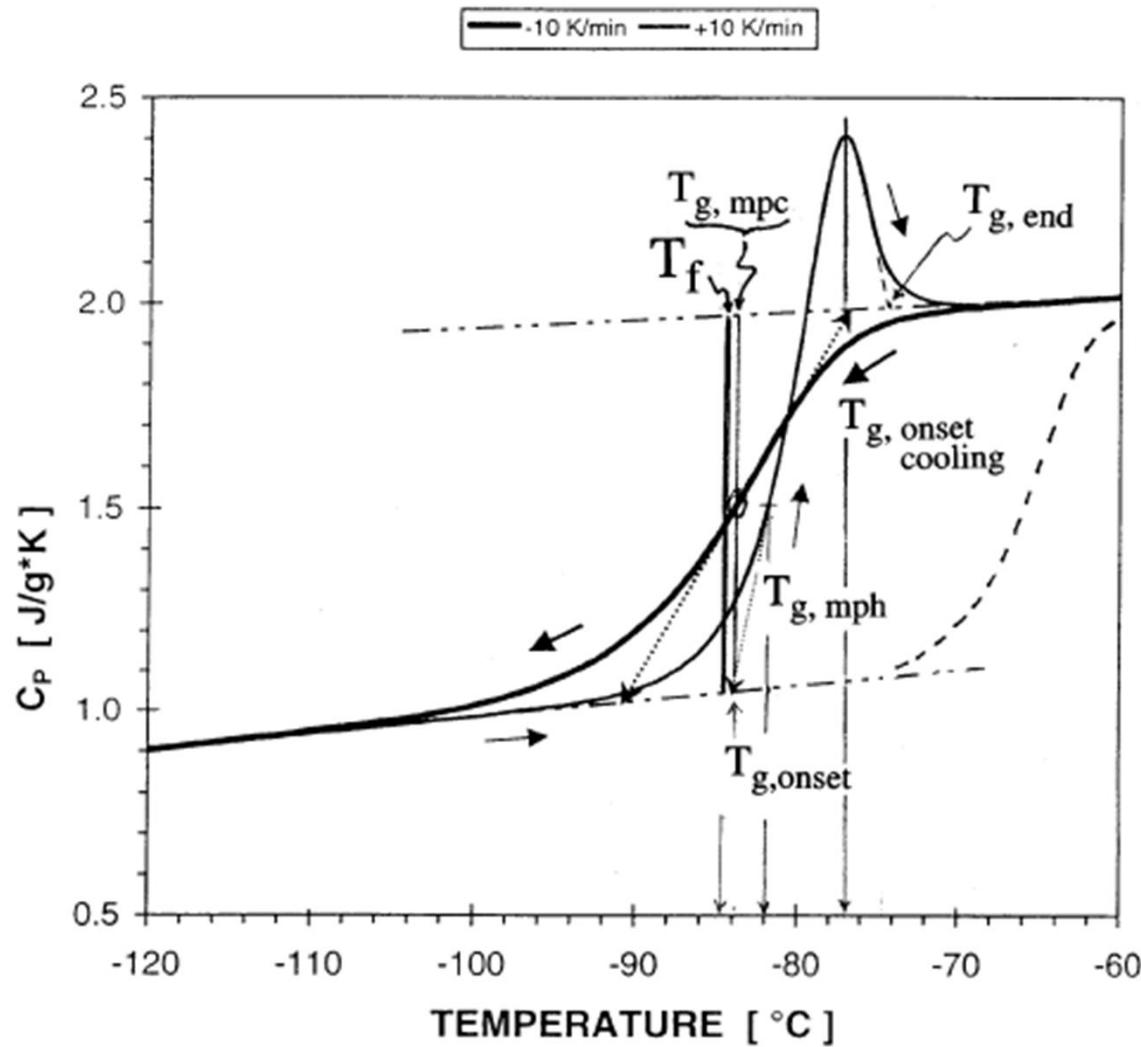


# **RELAXATION DYNAMICS GLASS TRANSITION**

# **CALORIMETRIC GLASS TRANSITION**

**LDA**

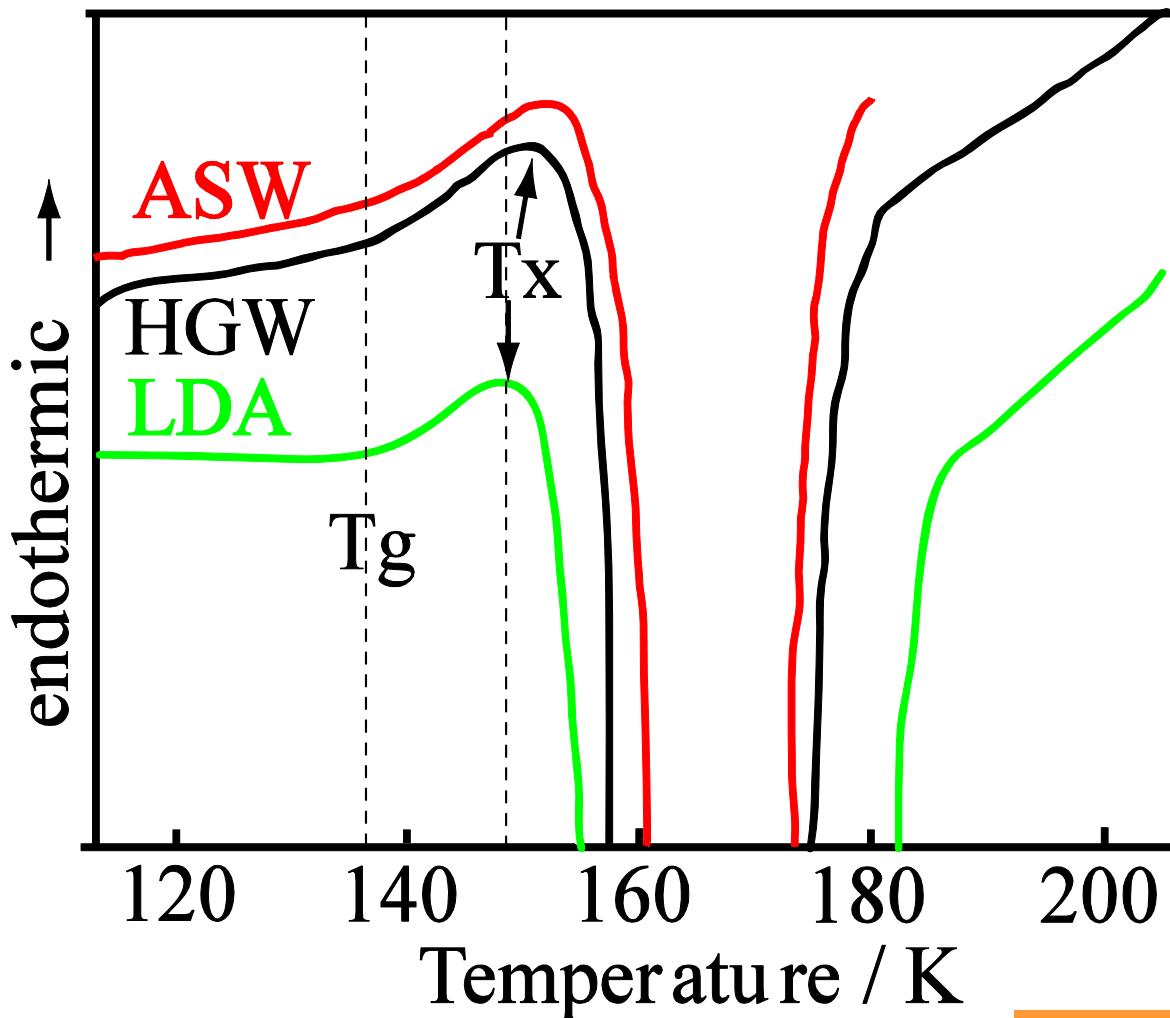
# The Glass→Liquid transition



glycerol (DSC)

C.A. Angell, Chem.Rev. **102**, 2002

# The glass transition at 136 K



Johari et al., *Nature* **330** (1987) 552

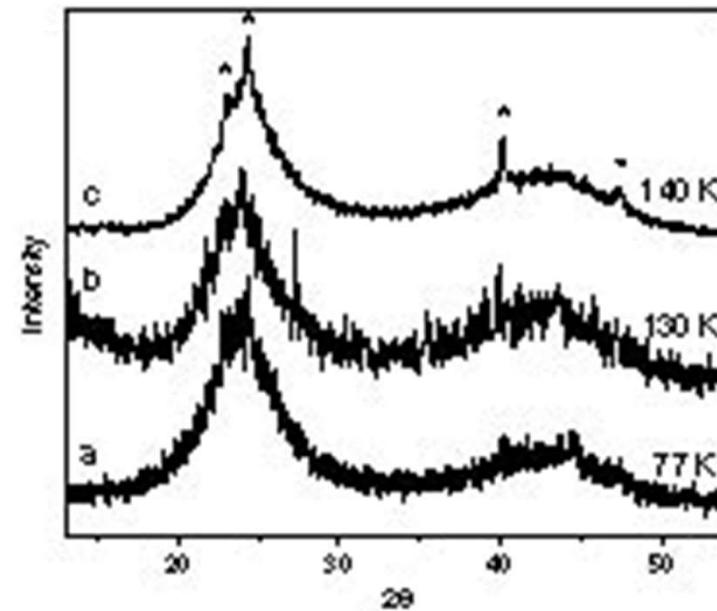
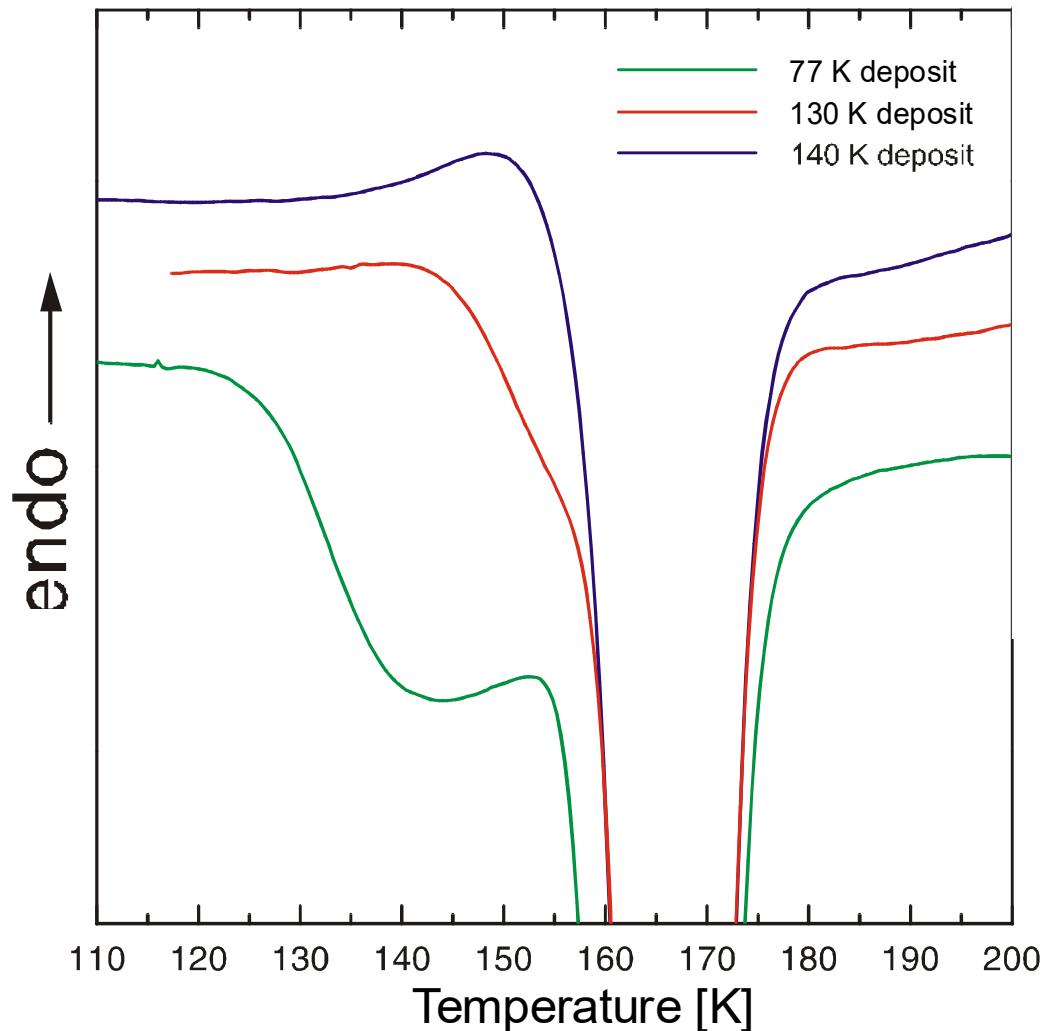
Hallbrucker et al., *JPC* **93** (1989) 4986

ASW, HGW, LDA

$T_g = 136$  K

(heating rate: 30 K/min)

# Glass Transition: HGW at 136 K



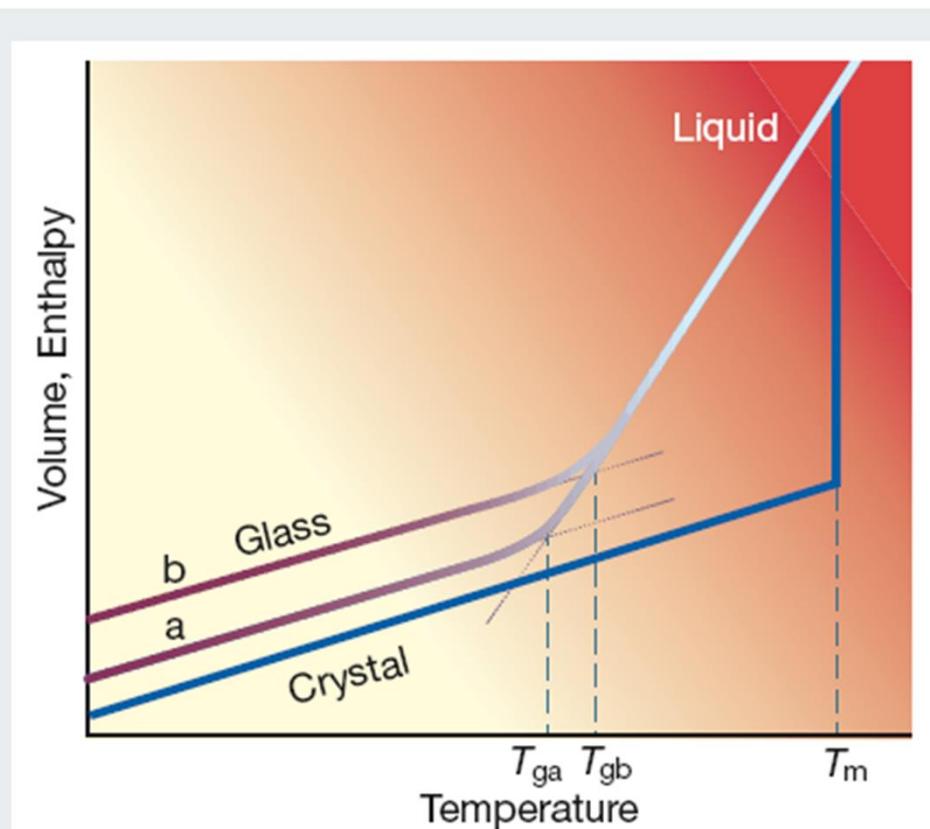
"Water Behaviour: Glass transition in hyperquenched water?", I. Kohl, L. Bachmann, A. Hallbrucker, E. Mayer, T. Loerting, **Nature** 435 (2005).

# **VOLUMETRIC GLASS TRANSITION**

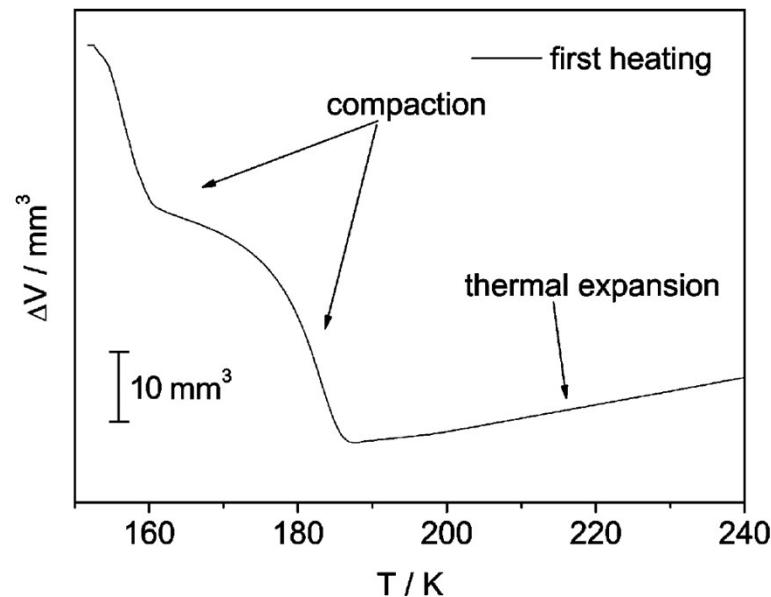
**LDA - HDA**

# The Glass→Liquid transition

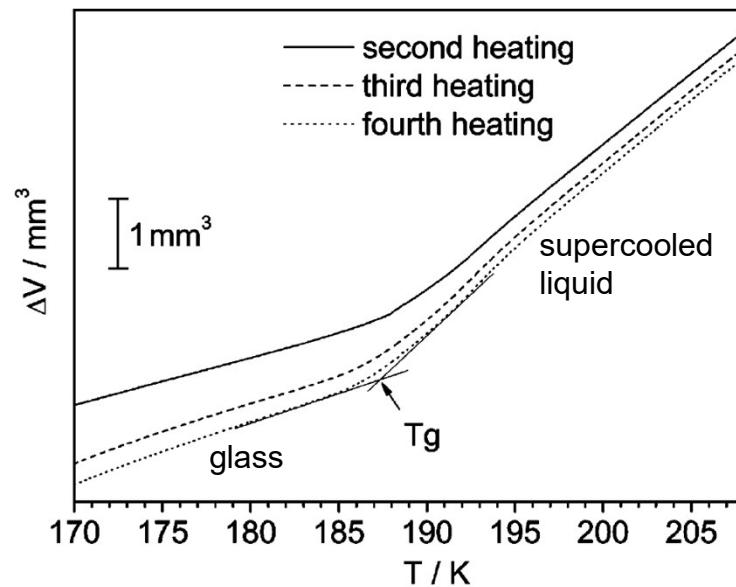
**Figure 1** Temperature dependence of a liquid's volume  $v$  or enthalpy  $h$  at constant pressure.  $T_m$  is the melting temperature. A slow cooling rate produces a glass transition at  $T_{ga}$ ; a faster cooling rate leads to a glass transition at  $T_{gb}$ . The thermal expansion coefficient  $\alpha_p = (\partial \ln v / \partial T)_p$  and the isobaric heat capacity  $c_p = (\partial h / \partial T)_p$  change abruptly but continuously at  $T_g$ .



### Glycerol for benchmarking the method (0.05 GPa) [1]



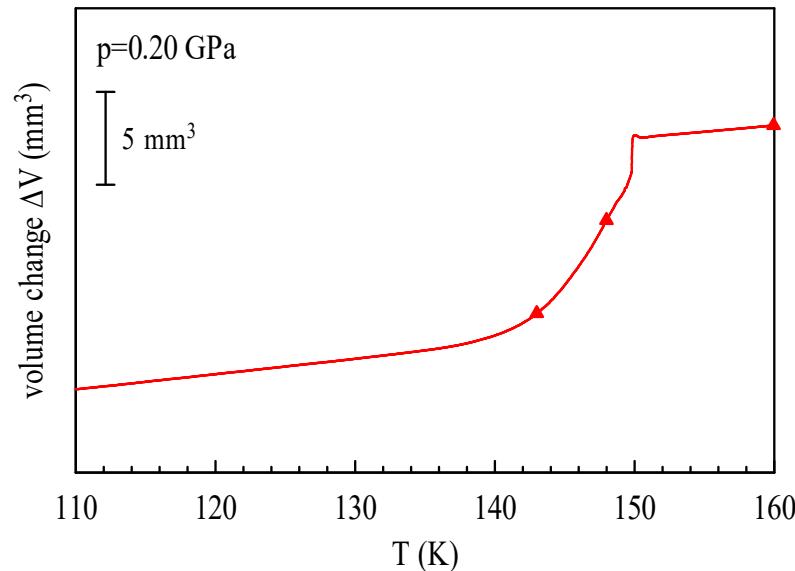
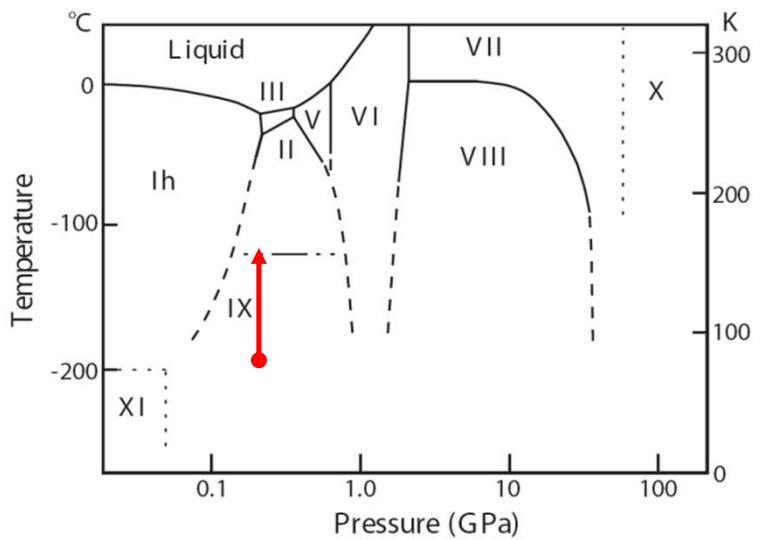
- heating rate:  $\approx 1\text{--}3 \text{ K/min}$
- cooling rate:  $\approx 25 \text{ K/min}$



$T_g$  ... glass transition temperature

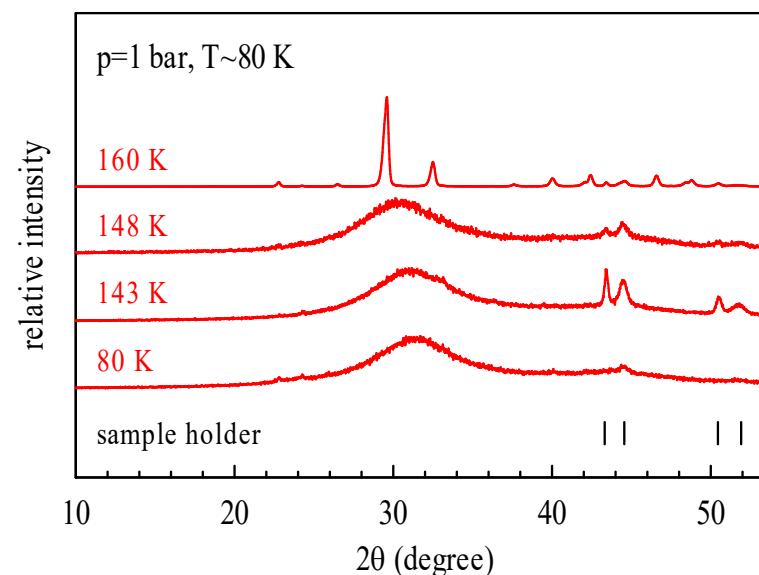
[1] M. S. Elsaesser et al., **J. Phys. Chem. B** 111 (2007) 8038.

# HDA: Volumetric measurements at 0.2 GPa

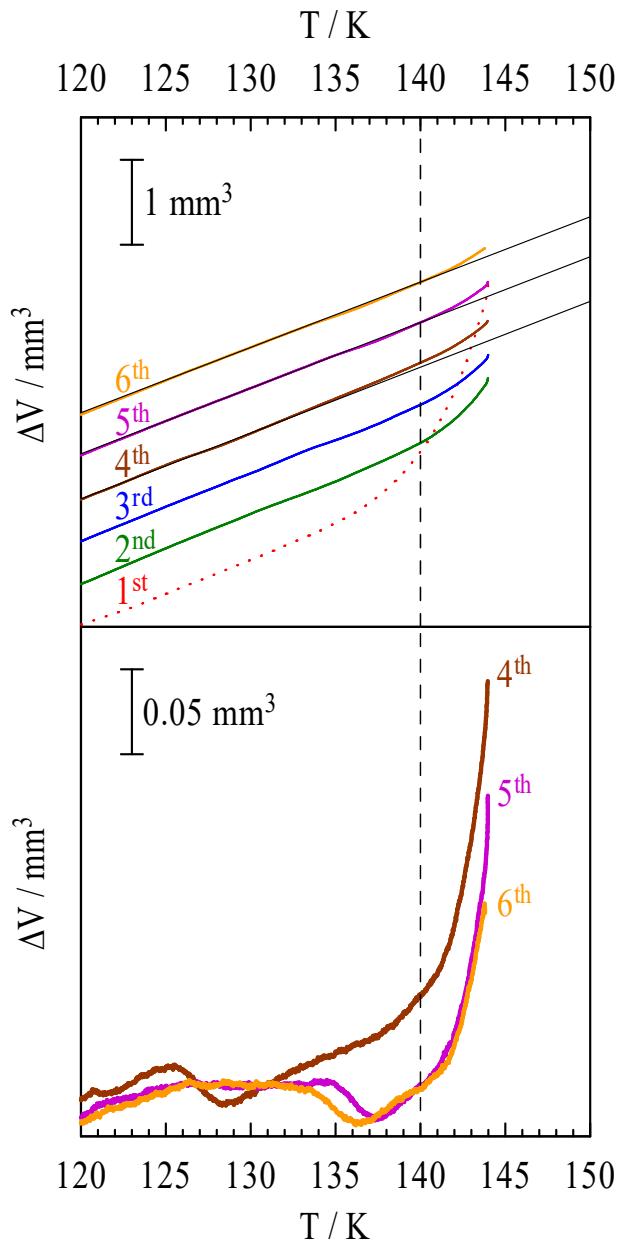


Full crystallization (160 K):  
eHDA  $\rightarrow$  ice IX

Onset of crystallization >148 K



# HDA: Volumetric glass transition at 0.2 GPa

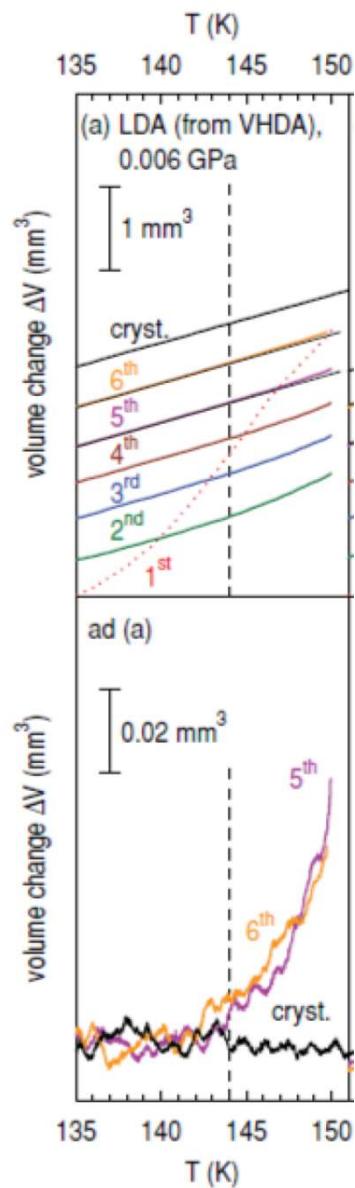


Reversibility:  
sample was heated 6x to 144 K

Heating rate: 2 K/min  
Cooling rate: 2 K/min

Onset of volumetric  $T_g$ :  
= deviation from linearity

# LDA: Volumetric glass transition at 0.006 GPa

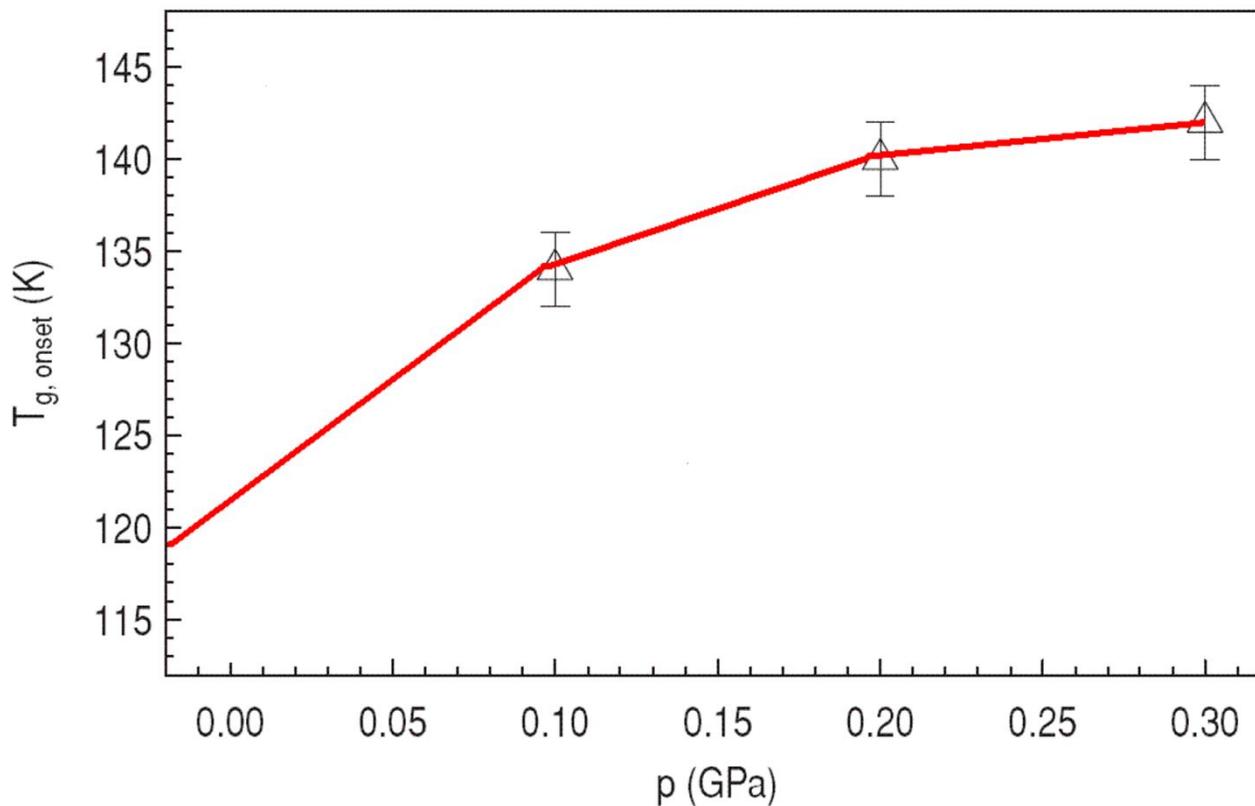


Reversibility:  
sample was heated 6x to 149 K

Heating rate: 2 K/min  
Cooling rate: 2 K/min

Onset of volumetric Tg:  
= deviation from linearity

## Pressure dependence of the glass transition in HDA

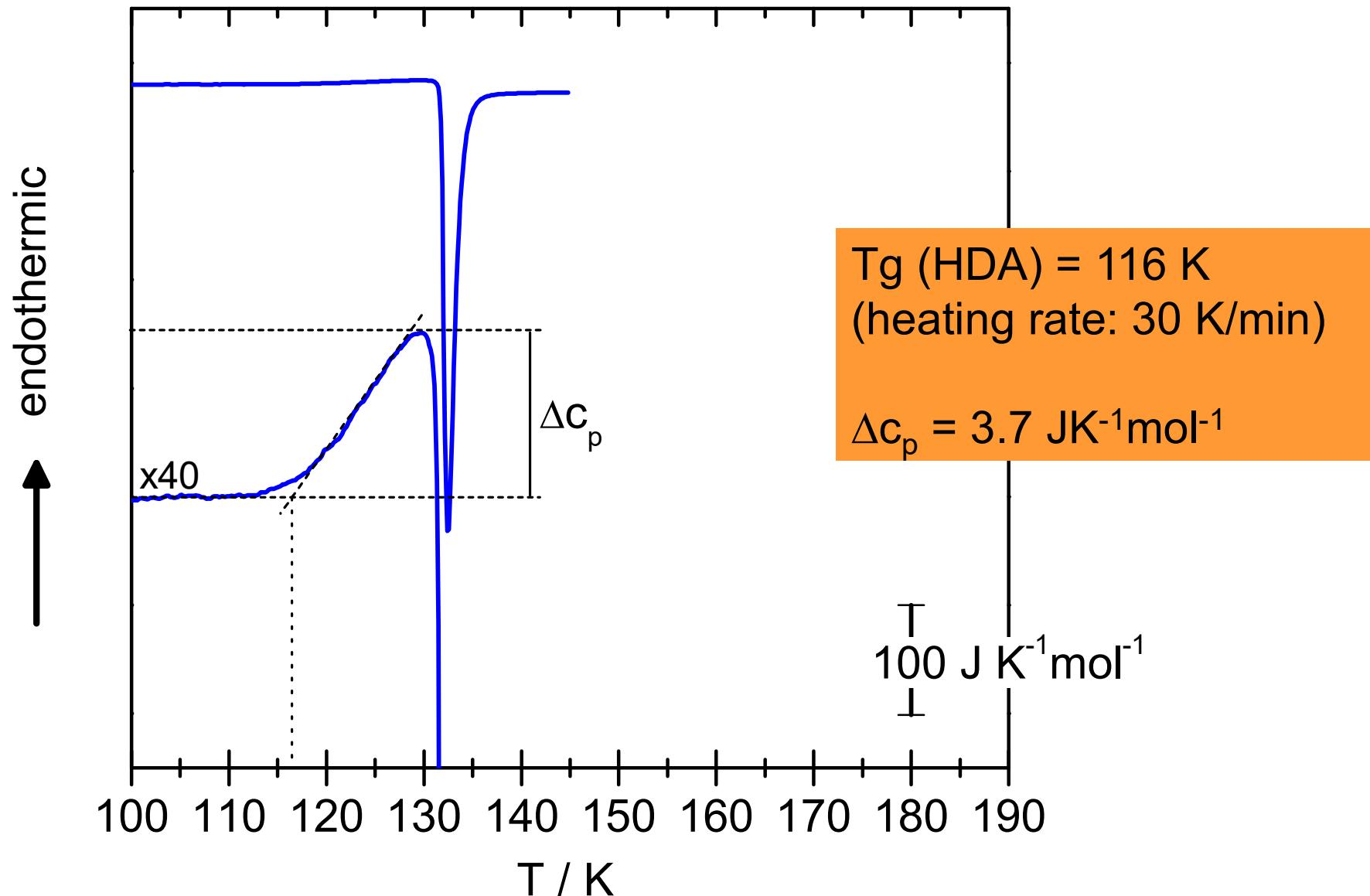


M. Seidl et al., PRB, **83**, 100201, 2011

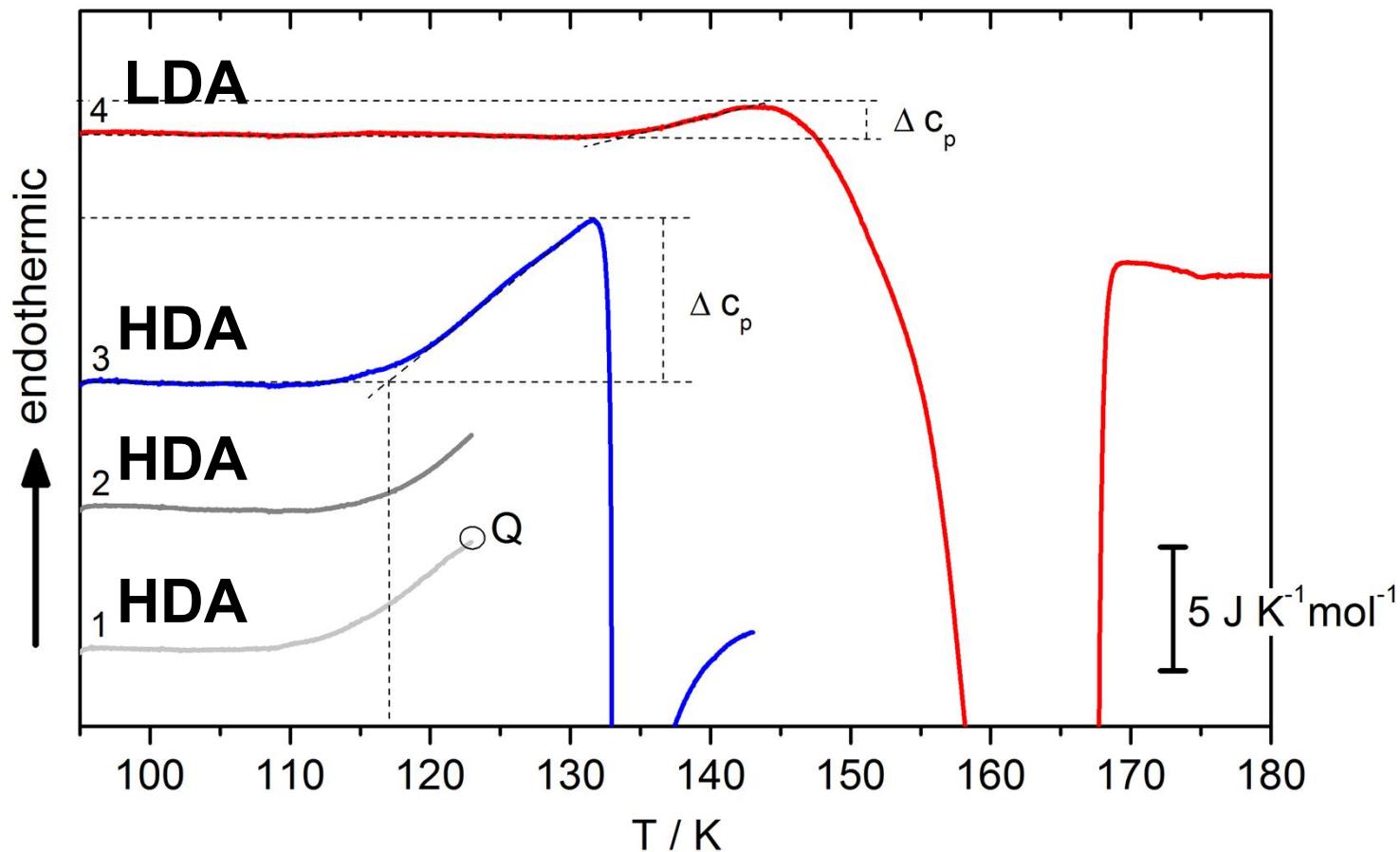
# **CALORIMETRIC GLASS TRANSITION**

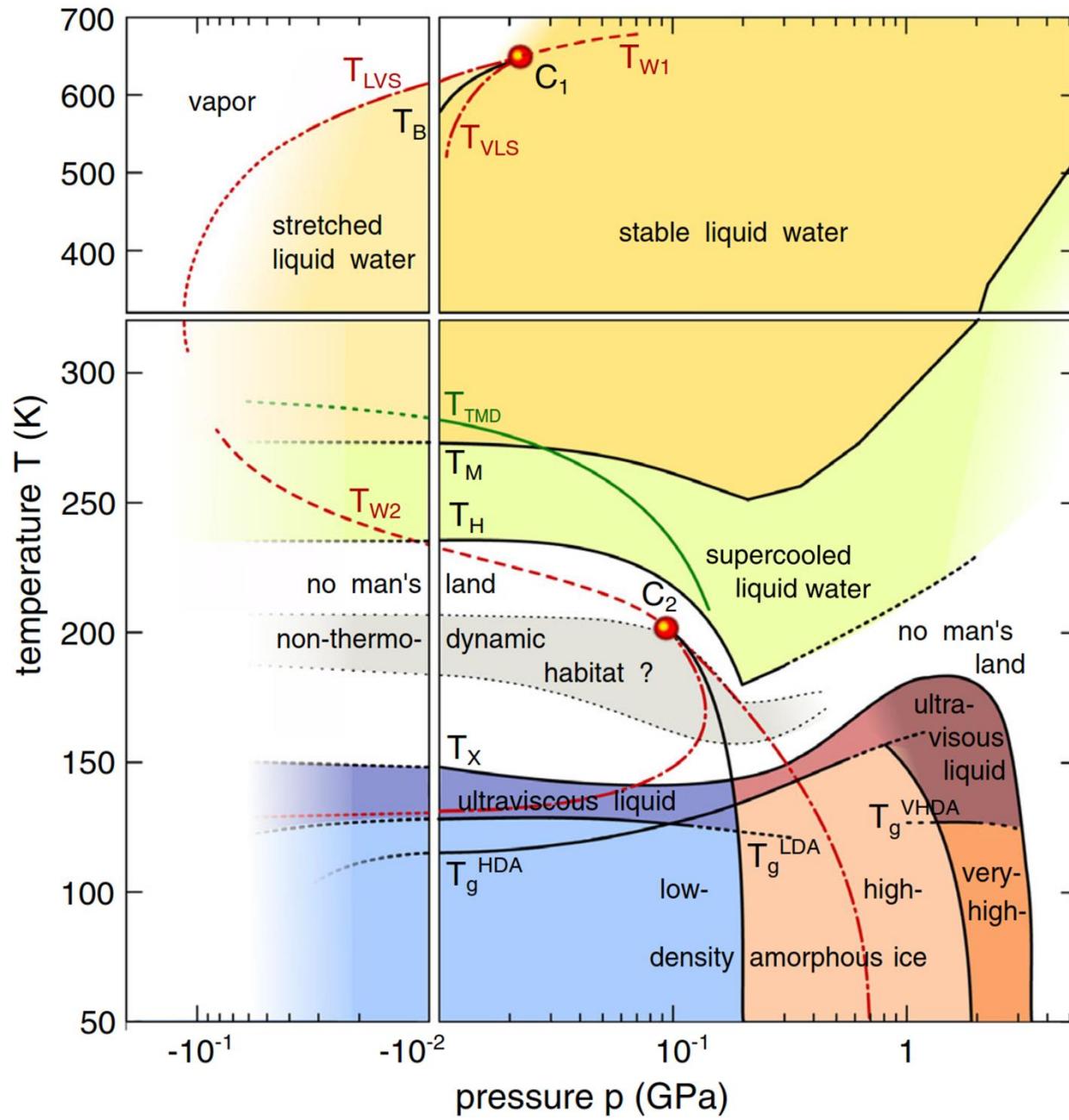
**HDA**

# The glass → liquid transition : HDA – HDL



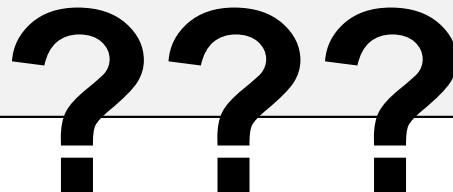
## Two Glass Transitions in Water





- Two calorimetric glass transitions in water

$\Delta C_p$  very small



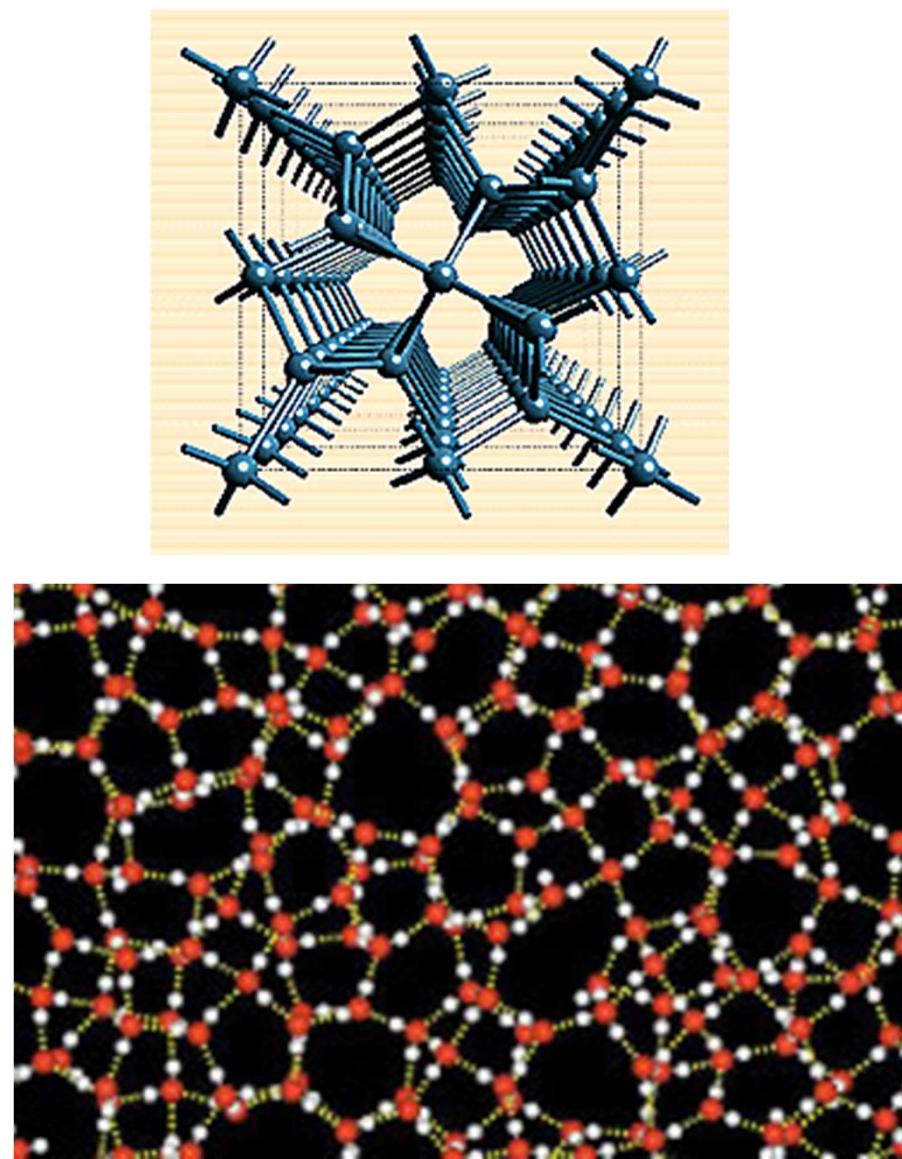
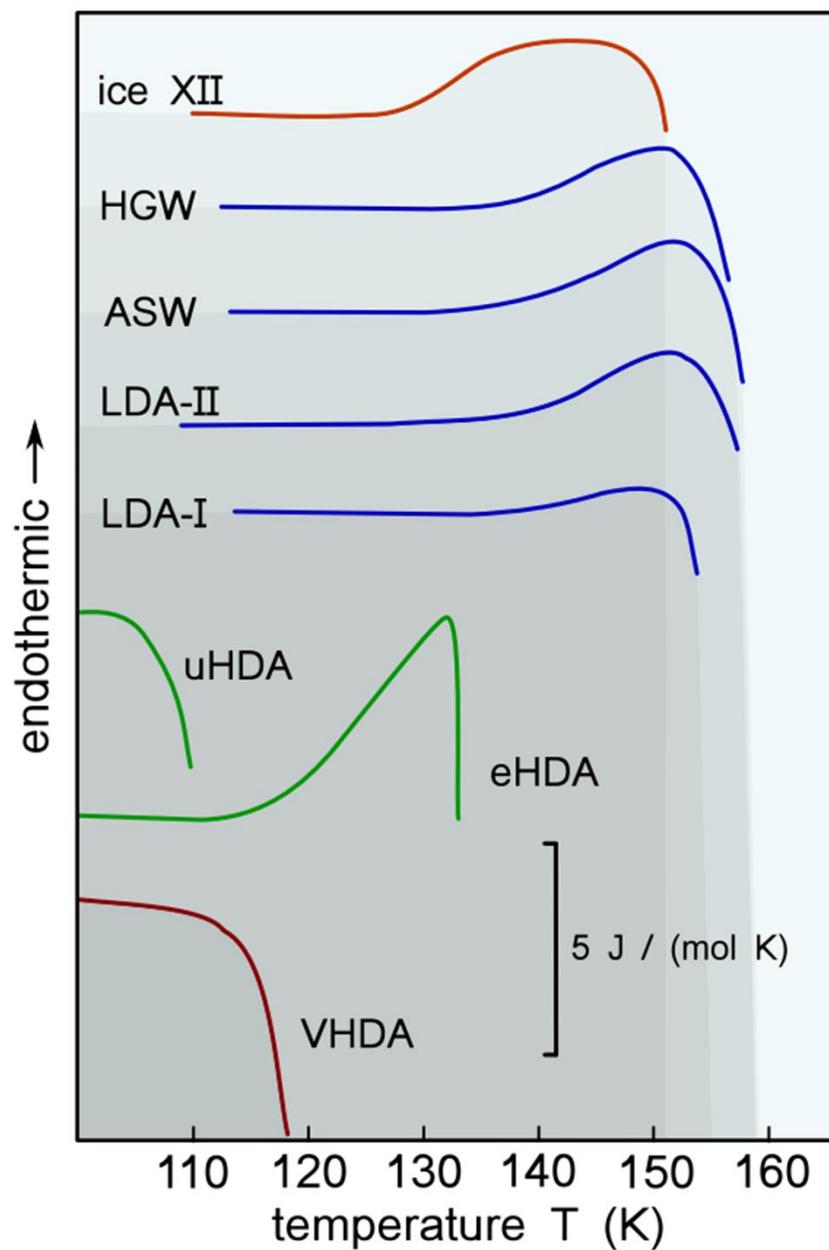
Glass-Liquid Transition at  $T_g$  ???

Solid-Solid Transition at  $T_g$  ???

- Dielectric measurements at 1 kHz  
(Johari, Hallbrucker, Mayer, JCP 95, 1991)
- ASW – isotope intermixing  
in thin films:  $T_g < T_x$  (160 K)  
(Smith, Kay, Nature 398, 1999)
- Glass-forming aqueous mixtures  
(Capacciolo, Ngai, JCP 135, 2011)
- Penetration of LDA  
(Johari, JPCB 102, 1998)

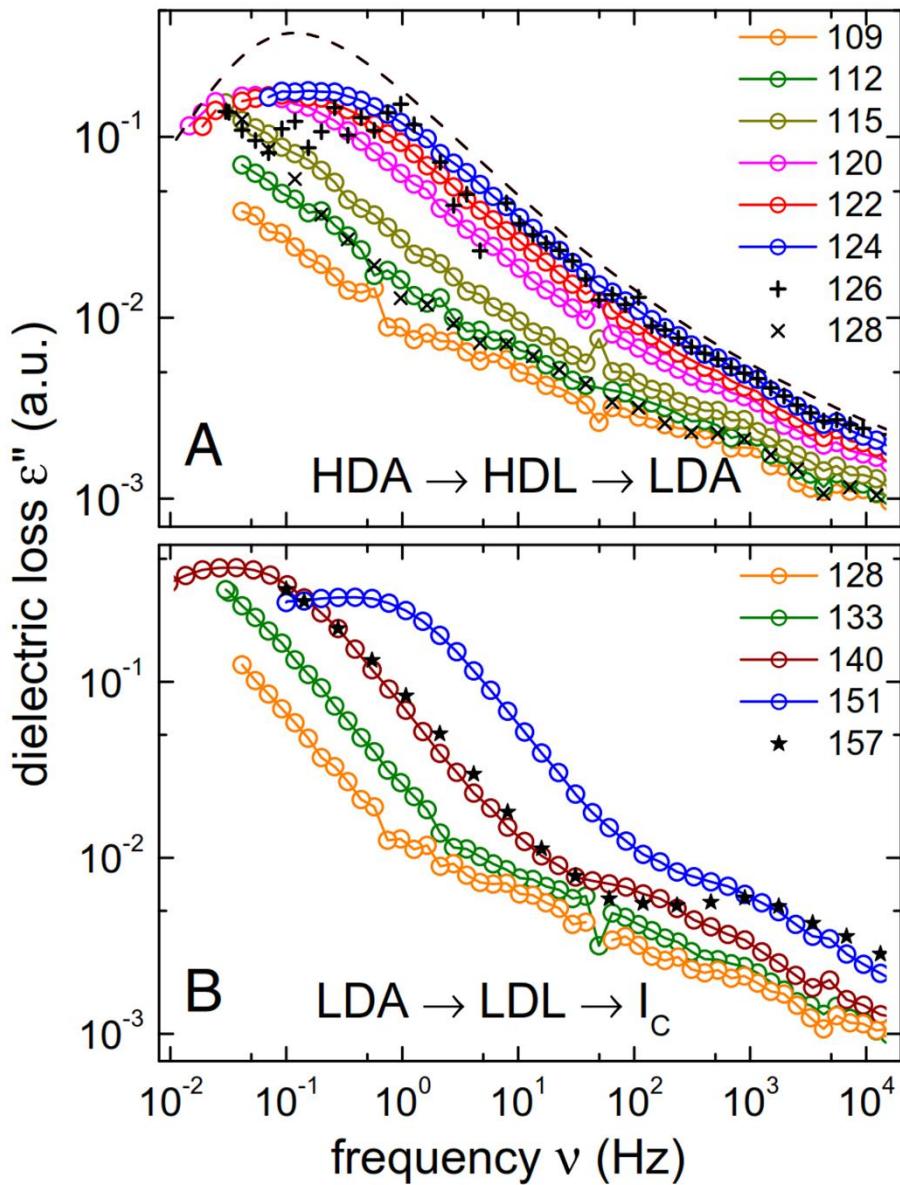
- „shadow“ of the real glass transition  
(Yue, Angell, *Nature* 427, 2004)
- $T_g$  of the proton sub-lattice  
(Fisher, Devlin, JPC 99, 1995)  
Salzmann et al., PCCP 13, 2011)
- Impurity/Interface Effect  
(McCartney/Sadtchenko, JCP 138 2013)  
Chonde/Brinzda/Sadtchenko JCP 125 2006)

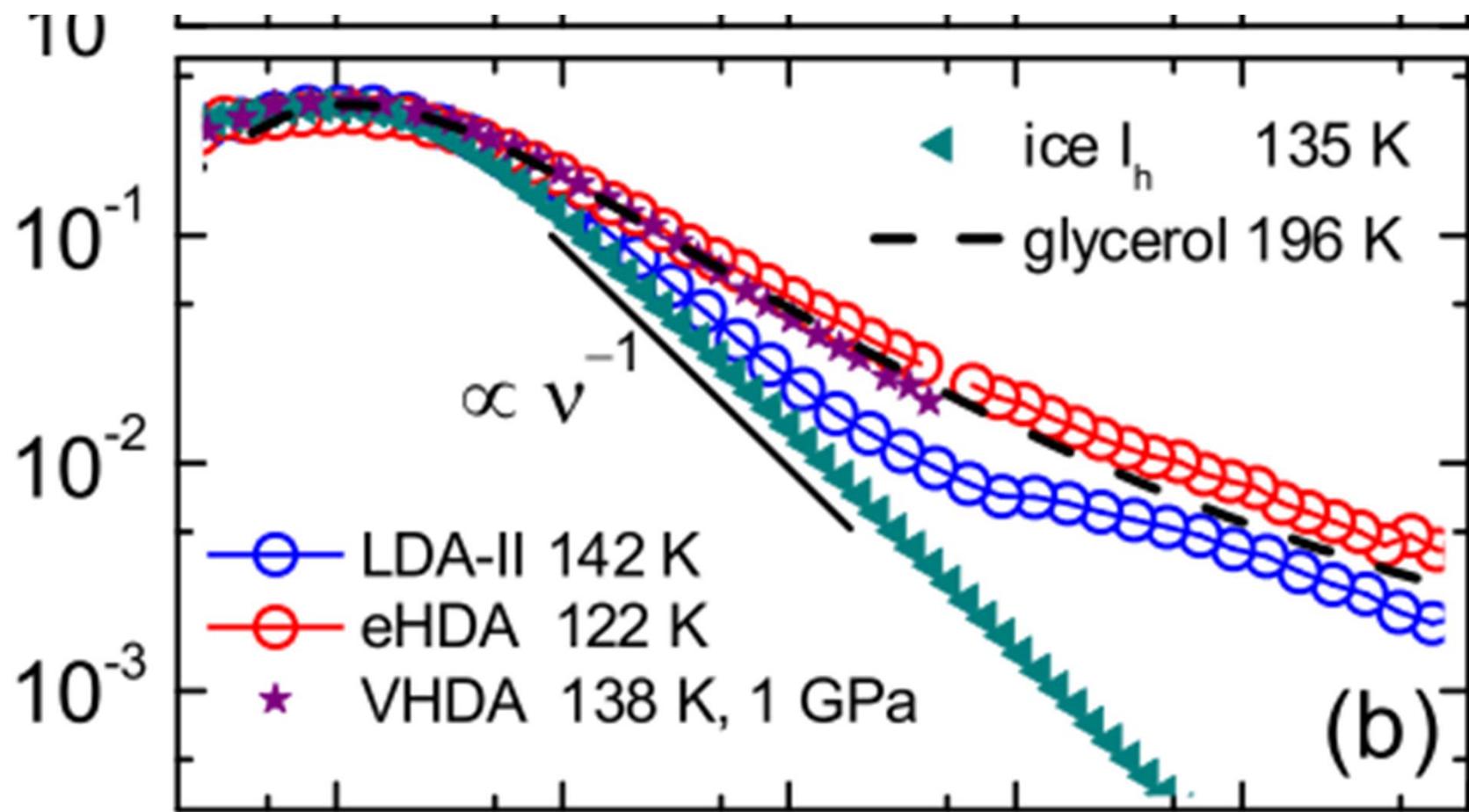
# Calorimetric glass transitions in water

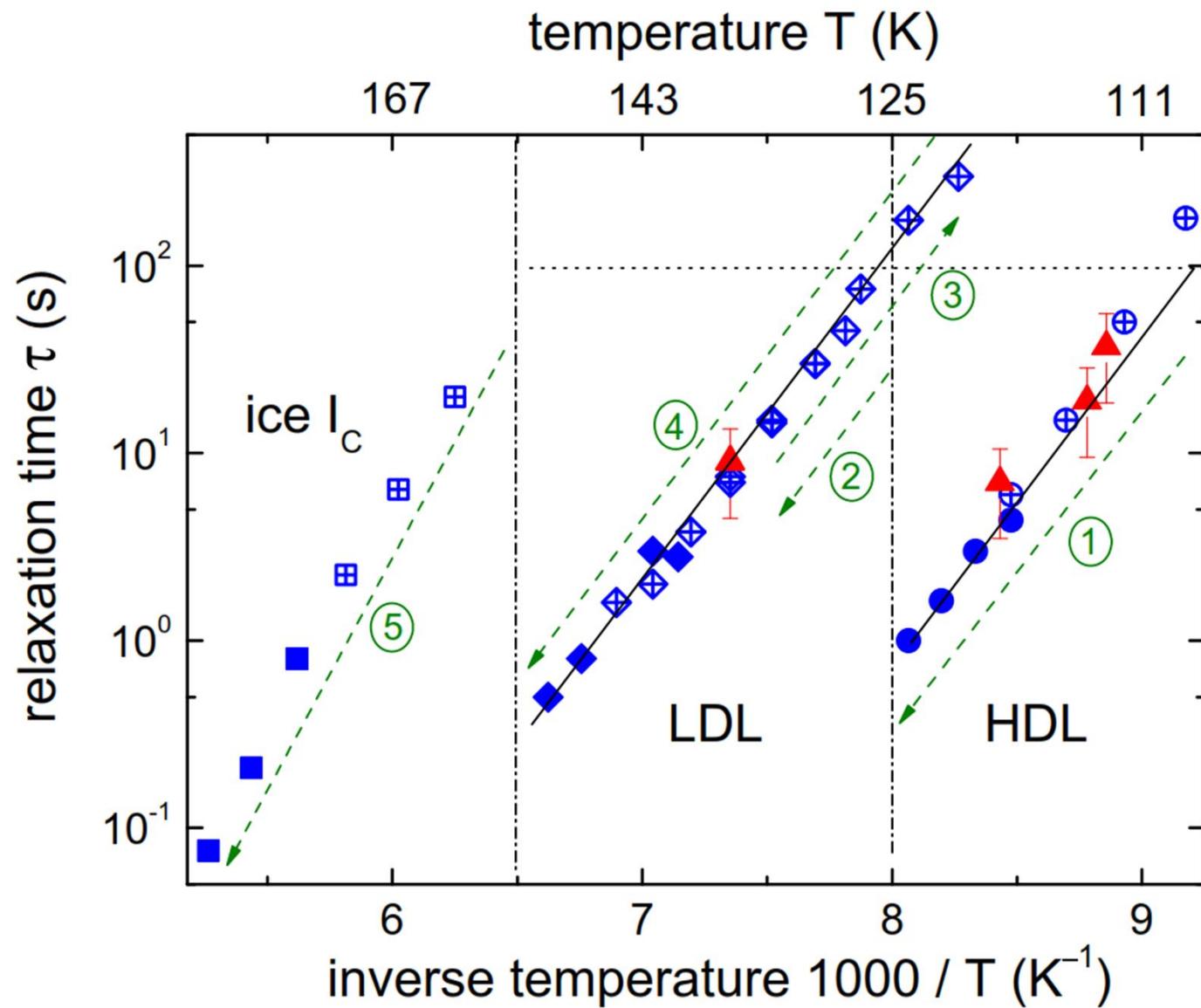


# **DIELECTRIC GLASS TRANSITION**

**LDA - HDA**





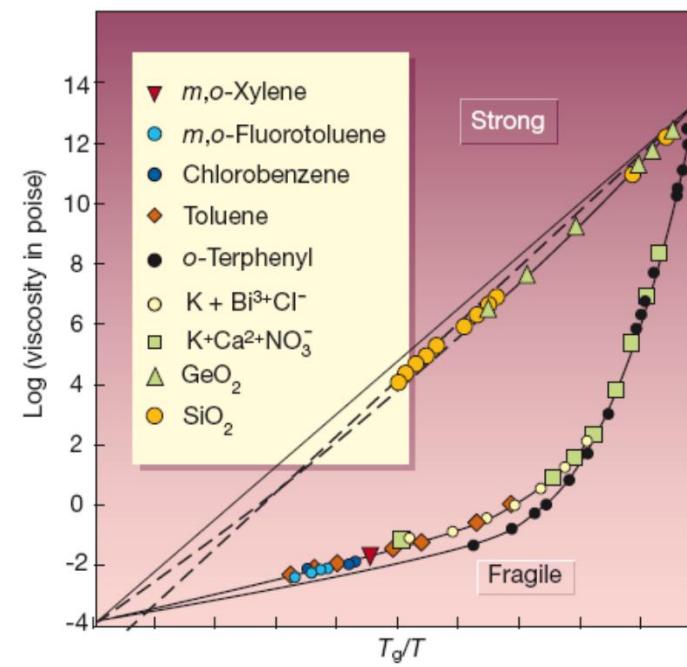
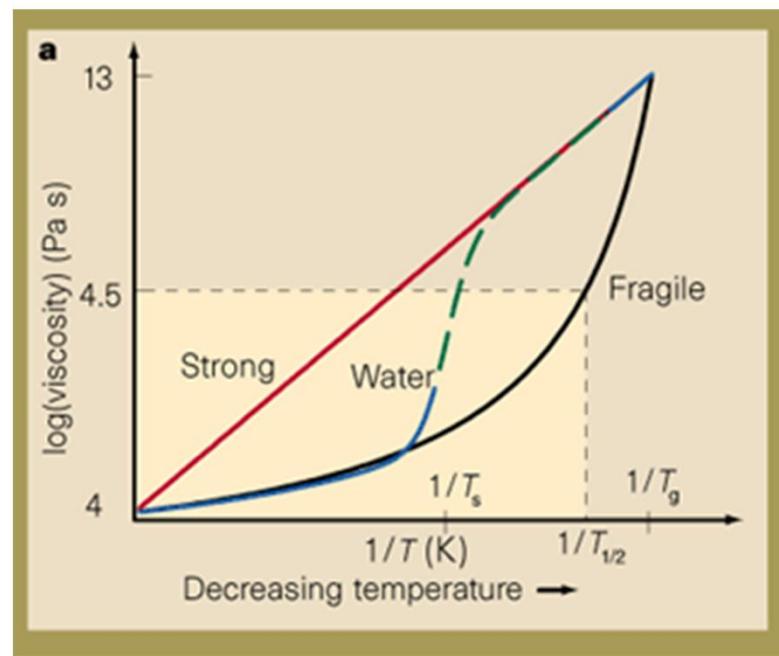


Fragility:

LDL „superstrong“ m=14

HDL „strong“ m=20-25

# Fragile-Strong Transition

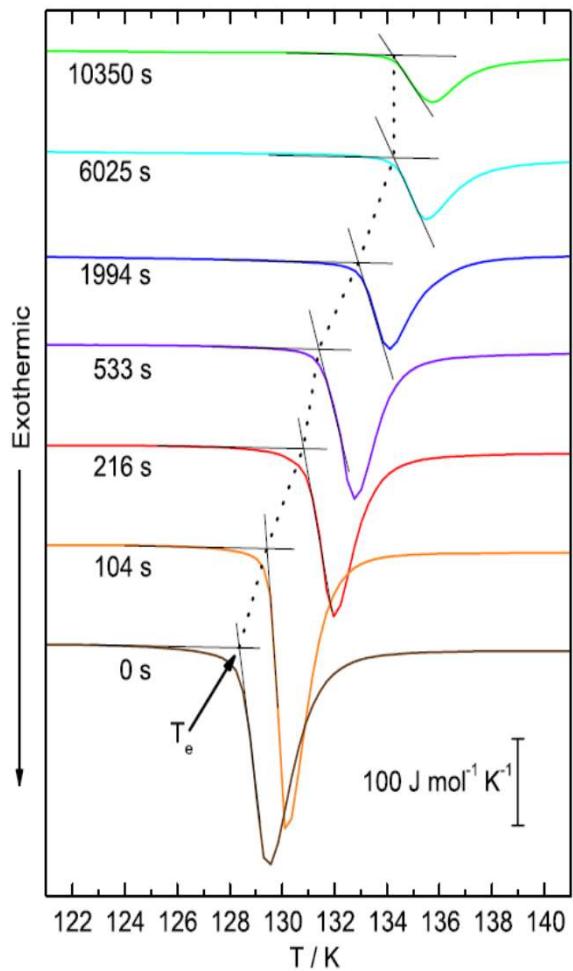


P.G. Debenedetti, F.H. Stillinger, *Nature* **410**, 259 – 267, 2001

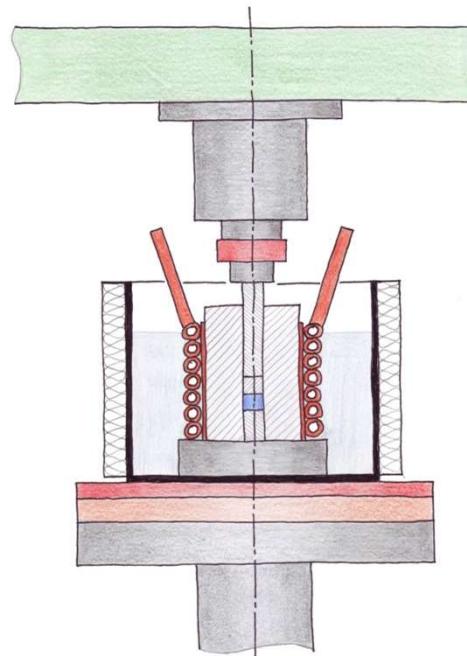
# **STRUCTURAL RELAXATION TIMES**

**HDA - VHDA**

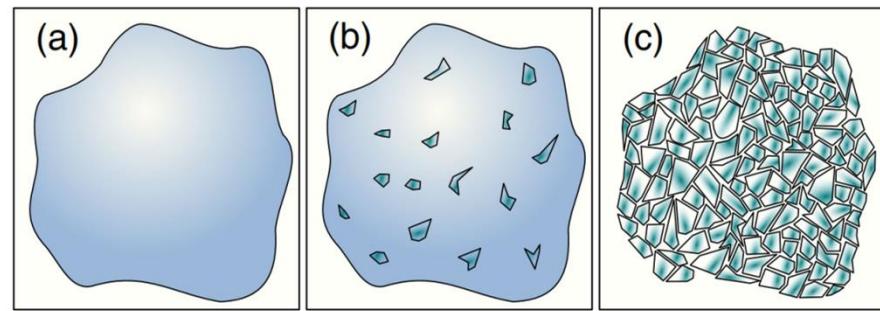
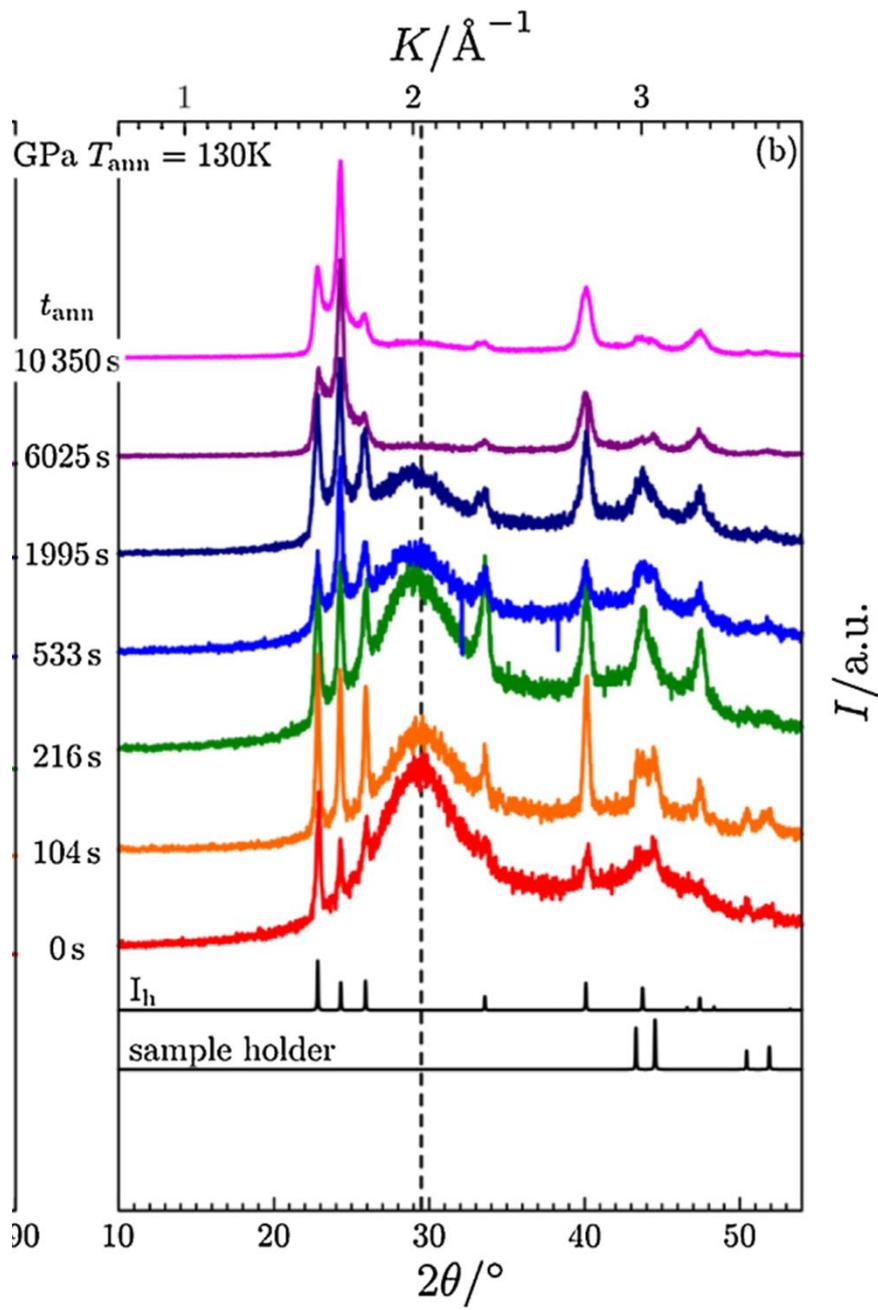
# Relaxing/Equilibrating HDA



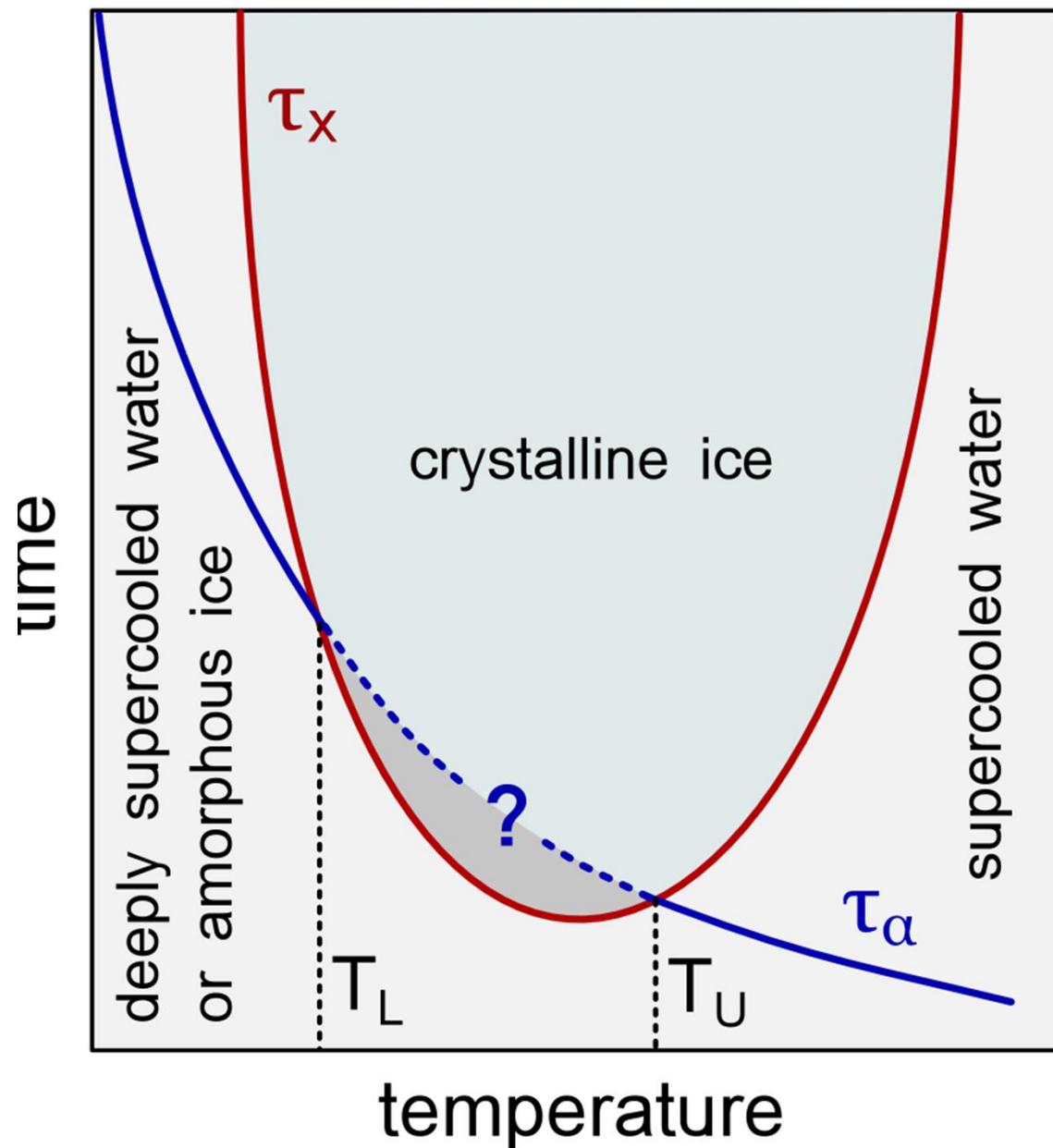
Isothermal/isobaric waiting experiment at 0.1 GPa/130 K



$$T_e(t) = T_{e,\infty} + (T_{e,0} - T_{e,\infty}) e^{-(t/\tau)^n} \quad \tau = 2980 \text{ s}$$



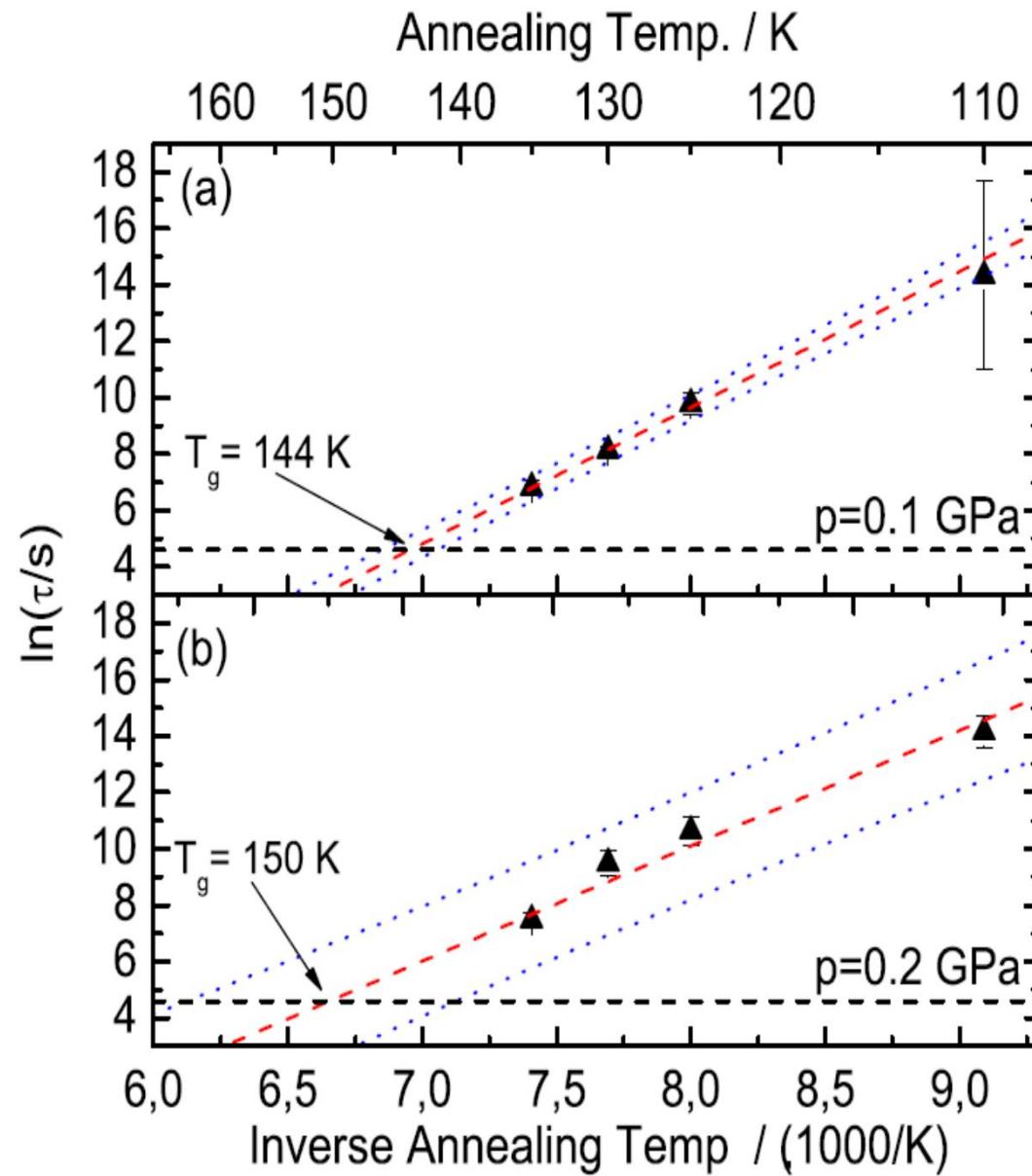
**uHDA**



uHDA can be equilibrated at 130 K/0.1 GPa;  
eHDA = eqHDA

timescale: one hour (i.e., solid)

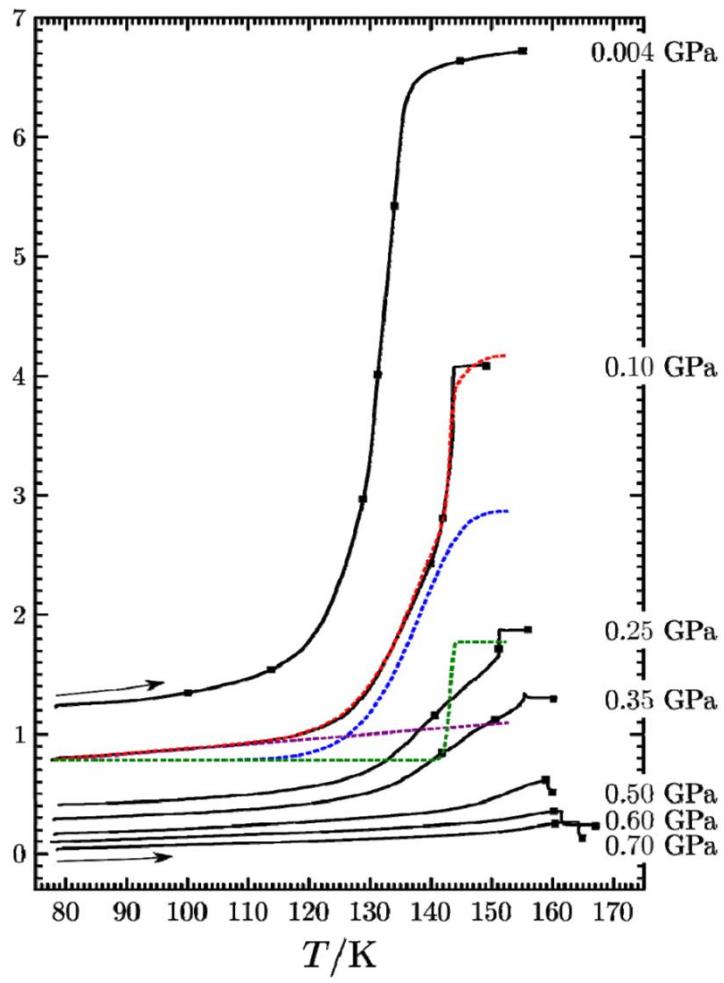
uHDA cannot be equilibrated at 145 K/0.1 GPa (interference of crystal growth)



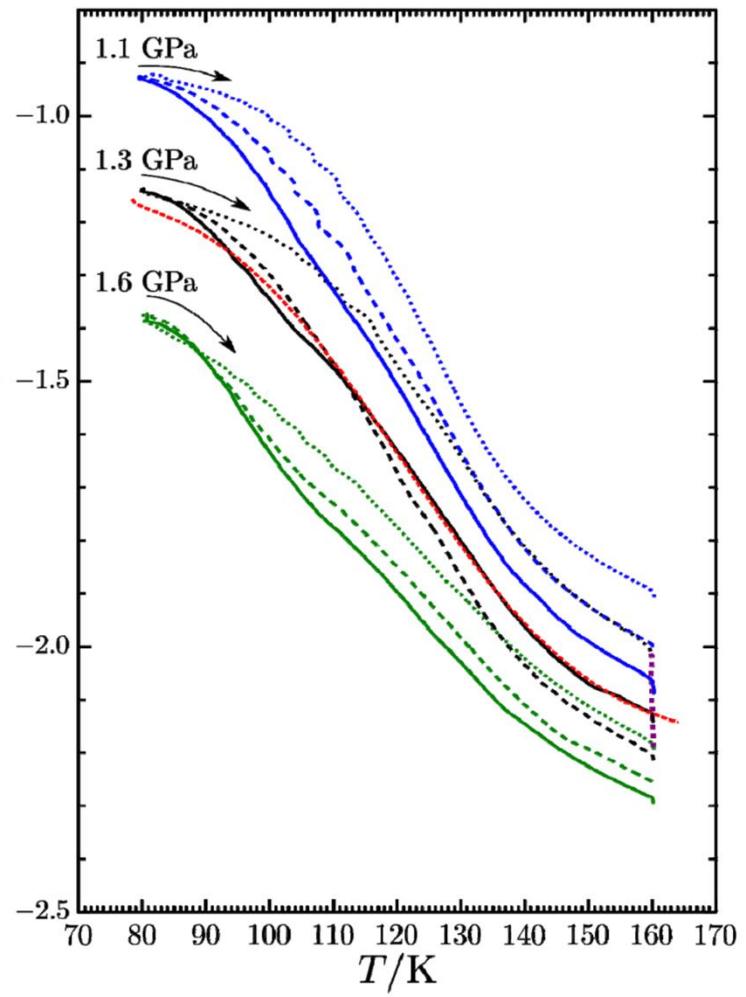
# **VOLUME RELAXATION TIMES**

## **HDA - VHDA**

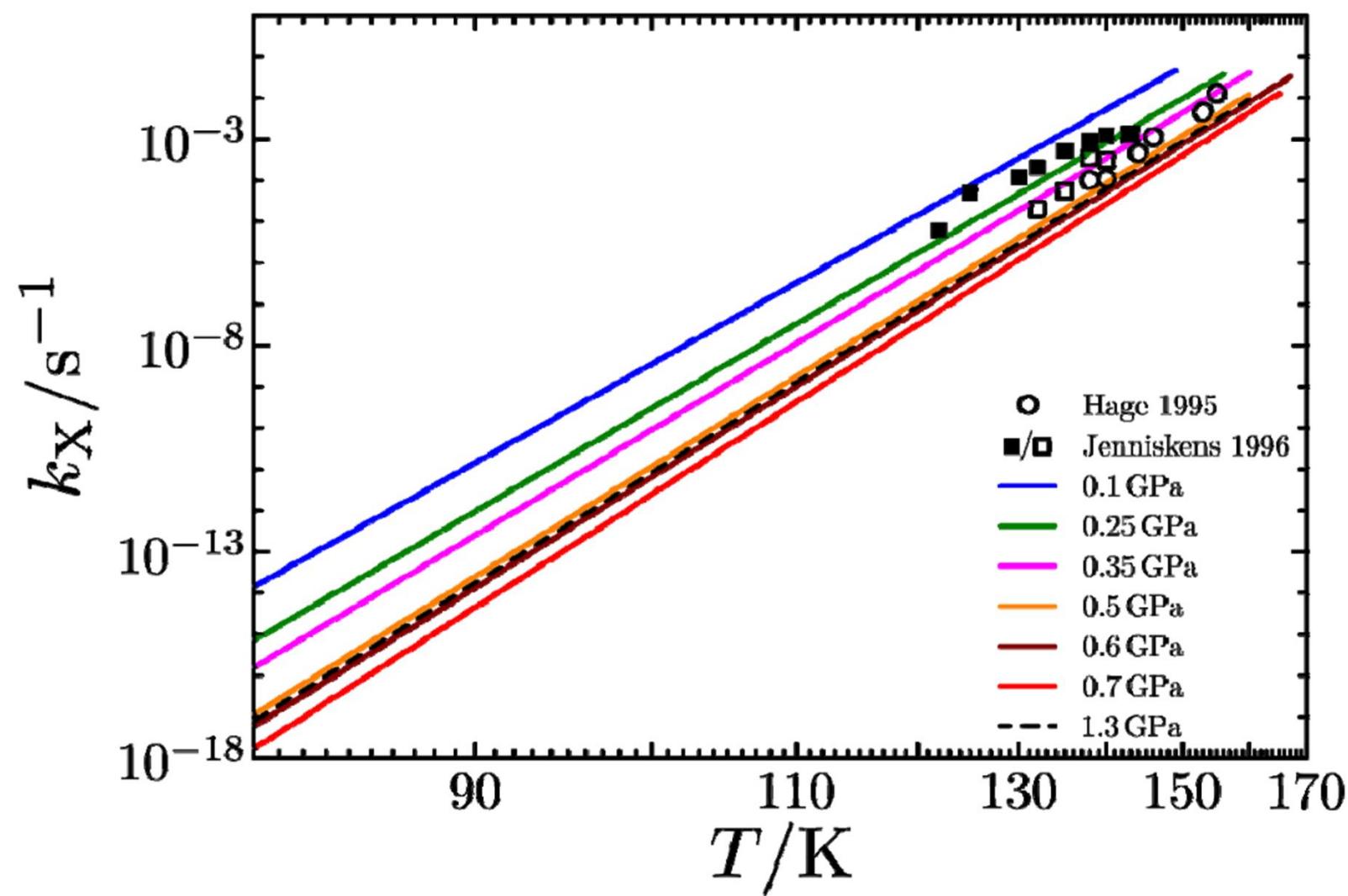
Volume change relative to VHDA  
at 1.1 GPa and 77 K /  $\text{cm}^3 \text{mol}^{-1}$

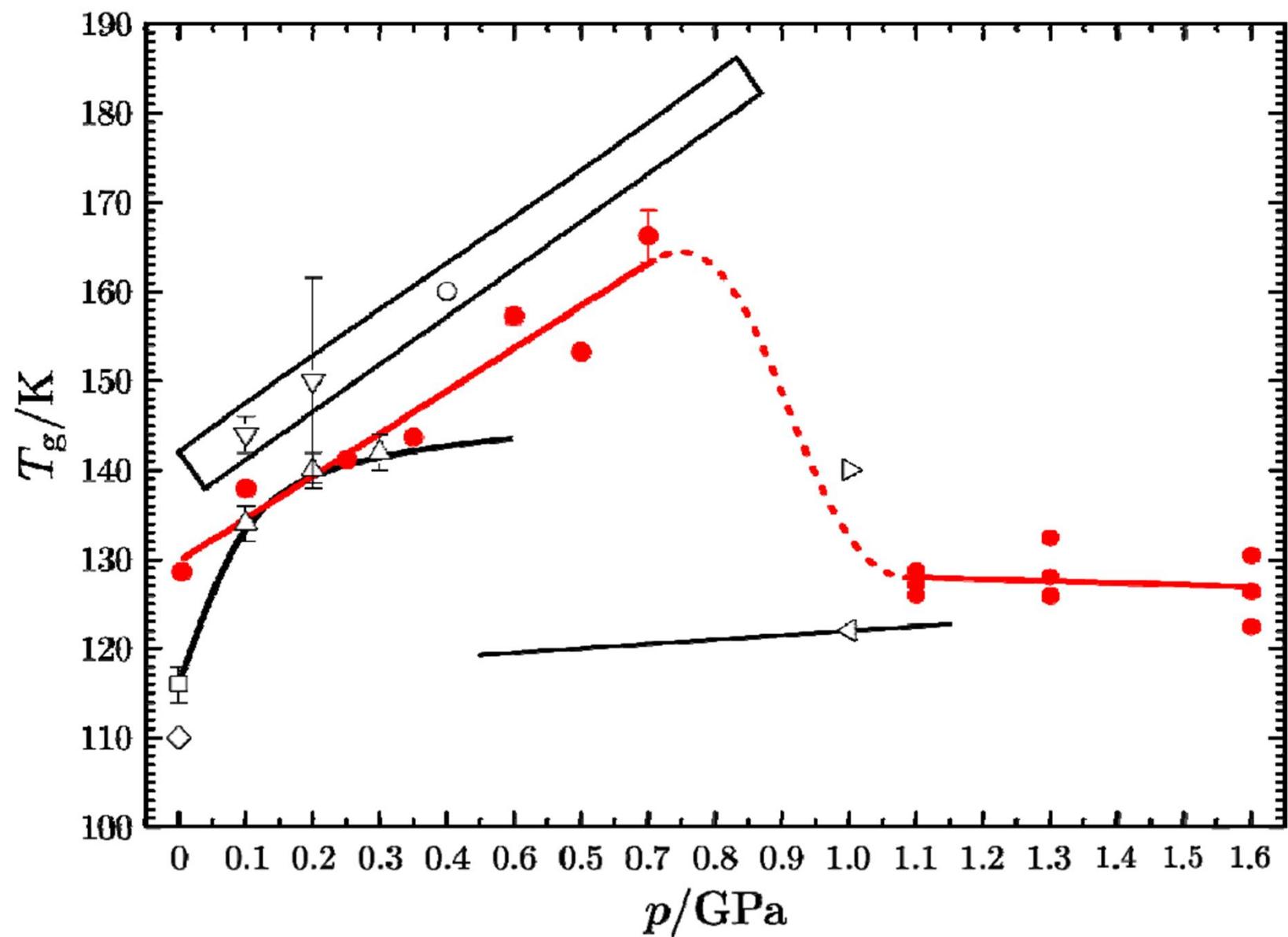


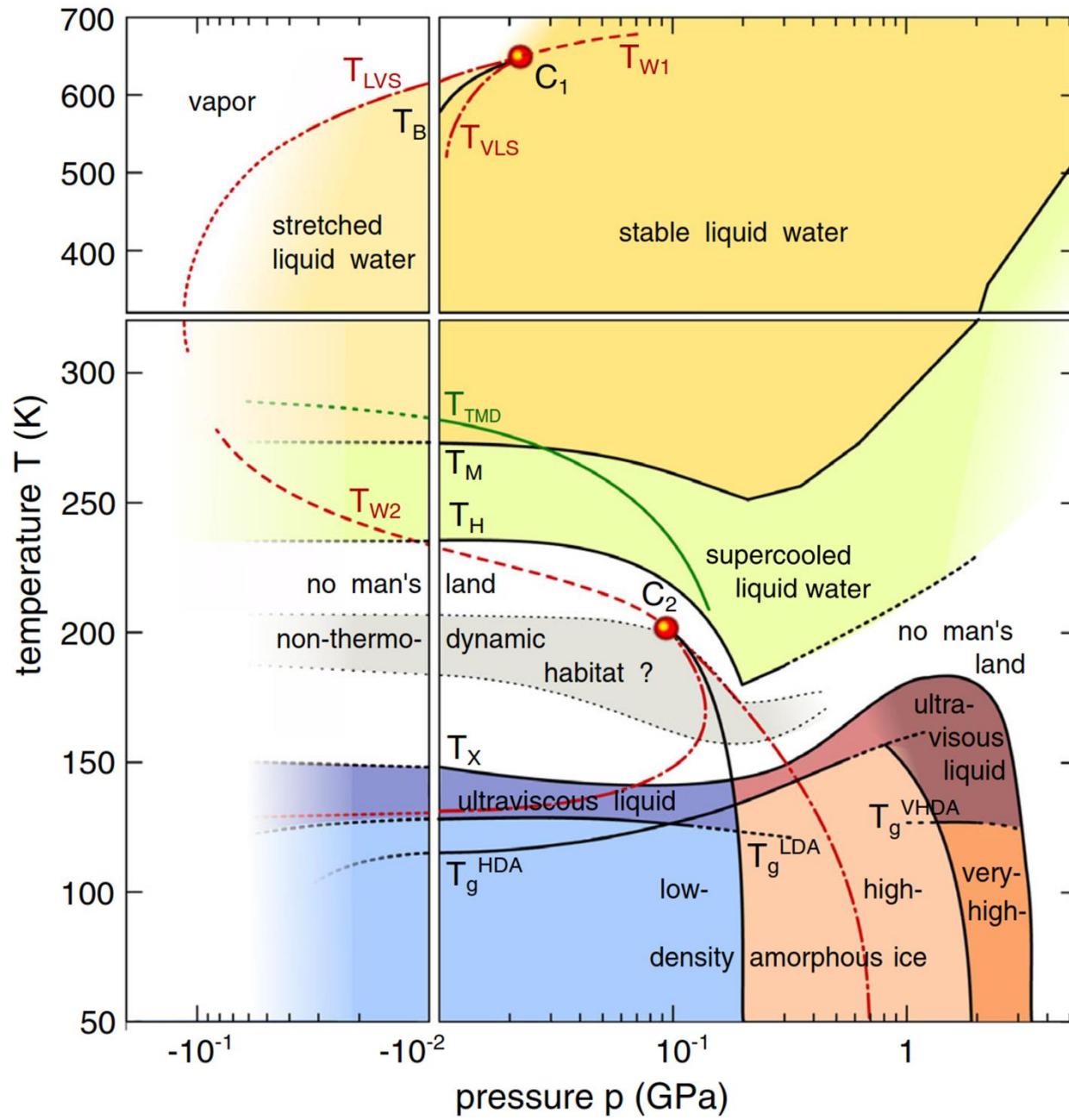
Volume change relative to eHDA  
at 0.1 GPa and 77 K /  $\text{cm}^3 \text{mol}^{-1}$

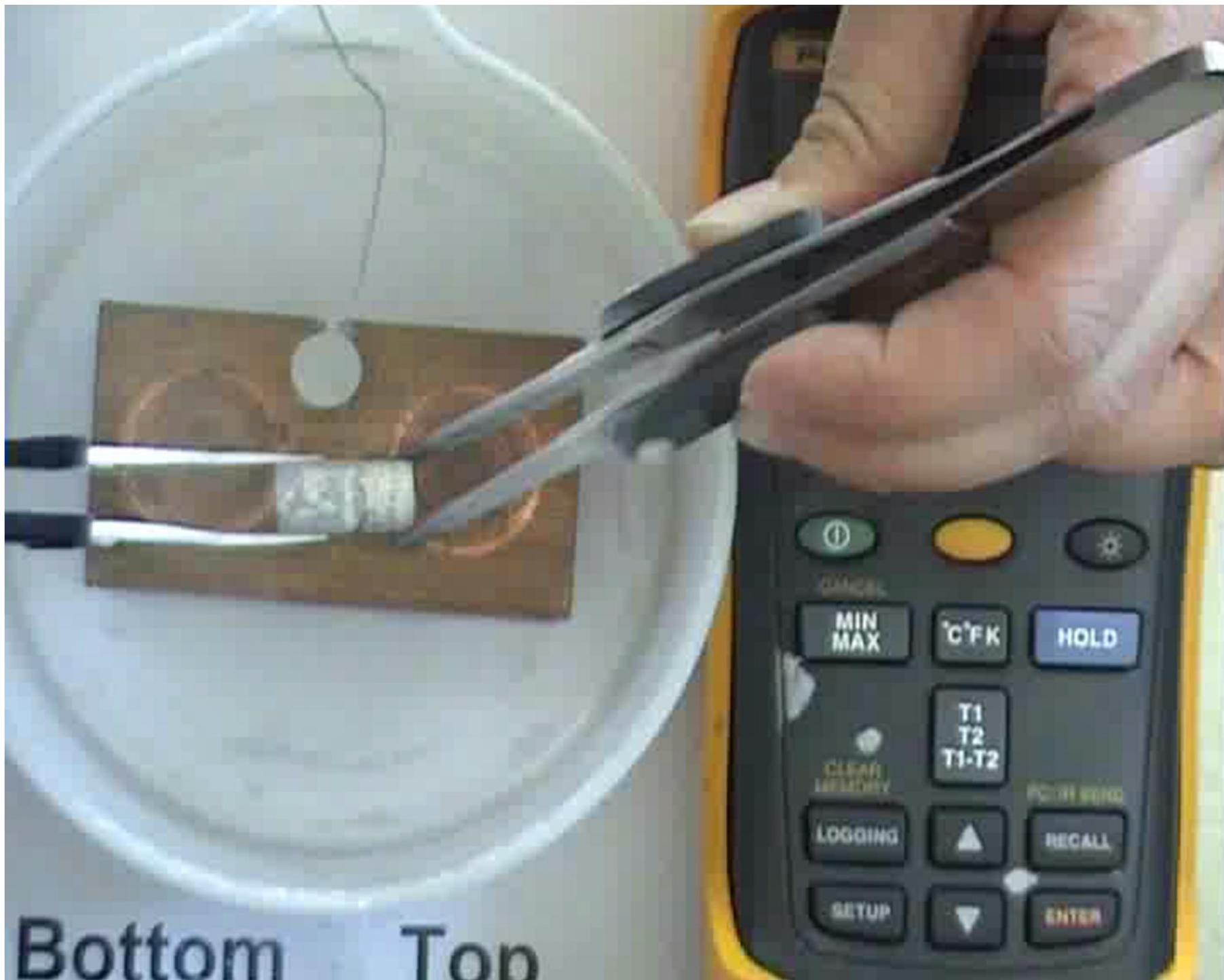


$$\Delta V_m(t) = \sum_i \Delta_e V_{m,i} \left( 1 - e^{-\left(\frac{\Xi_i(t)}{Rq\tau_{R,\infty,i}}\right)^{\beta_{p,i}^{V_m}}} \right) + \alpha_p^{V_m} (T(t) - T_0).$$









Bottom Top

# Ehrenfest Relation

$$\frac{\Delta C_p}{TV} = \Delta\alpha \frac{dp}{dT}$$

**HDA:**

$dT_g/dp = 200 \text{ K/GPa}$ ;  $dp/dT_g = 5 \cdot 10^6 \text{ Pa/K}$  (ambient pressure)

$\Delta c_p = 4 \text{ J/Kmol}$  (ambient pressure)

$\Delta\alpha = 0.00048/\text{K}$  (0.1 GPa)

$T_g = 116 \text{ K}$  (ambient pressure)

$V = 15.7 \cdot 10^{-6} \text{ m}^3/\text{mol}$  (ambient pressure)

**Fulfilled (only 10% deviation!)**

**LDA:**

$dT_g/dp = -20 \text{ K/GPa}$ ;  $dp/dT_g = -5 \cdot 10^7 \text{ Pa/K}$  (ambient pressure)

$\Delta c_p = 1 \text{ J/Kmol}$  (ambient pressure)

$\Delta\alpha = 0.00008/\text{K}$  (0.006 GPa)

$T_g = 136 \text{ K}$  (ambient pressure)

$V = 19.5 \cdot 10^{-6} \text{ m}^3/\text{mol}$  (ambient pressure)

**Not Fulfilled (wrong sign - Delta alpha!)**