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# Diffraction and Instruments for Neutron Diffraction

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Neutron School SoNS Francesco Paolo Ricci, Erice 28 July – 4 August 2015

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15-08-11

# Who am I?



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- University education (solid-state chemist)
  - Chemistry Degree (with supplementary Bio-chemistry)
  - D. Phil. in Solid State Chemistry “Fullerene Intercalation Compounds”
  - 7 years Post Doctoral experience
    - High-pressure, zeolites, magnetic materials, superconductors, pigments, isotopes
- Instrument scientist (powder diffraction)
  - 5 Years as co-responsible for D20 at ILL, Grenoble
  - 2.5 Years responsible E9 at HZB, Berlin
  - Since March 2011 responsible for powder diffraction at ESS, Lund
  - Since May 2013 Adjunct Professor in Neutron Scattering at CTH, Göteborg
- Research interests
  - Hydrogenous materials and neutrons
  - In-situ sample environment development
  - Materials research
  - Neutron diffraction community development

# Outline



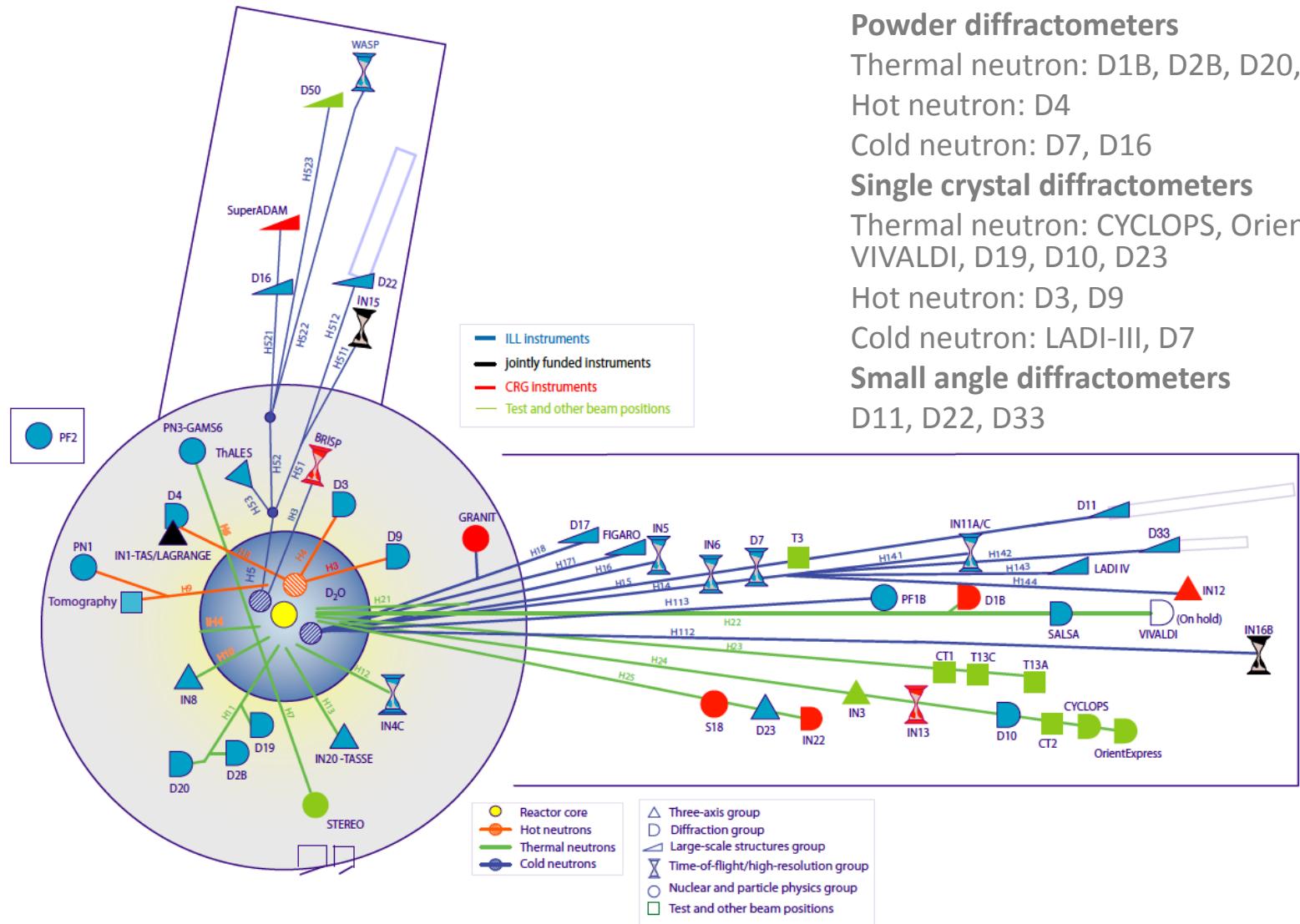
- Diffraction and structure
- Diffraction instruments at large-scale facilities
- Principles of diffraction
- X-rays v neutrons
- Data collection and analysis
- Total scattering (PDF methods)
- TOF v Monochromatic for diffraction
- Examples of neutron diffractometers
- Design of next generation diffraction instruments
- Examples of uses of diffraction
- Final comments

# Diffraction and structure



- Diffraction is the tool we use to determine structure
- Structure determines the physical properties of a material
- To tailor physical properties we must understand structure
- Neutron and X-ray diffraction are complementary tools
- Most diffraction measurements use powders. Why?
  - Many materials are difficult to make as single crystals
  - Practical uses require bulk materials
  - Functional materials may require non-perfect crystals
  - Phase transitions destroy or fracture single crystals

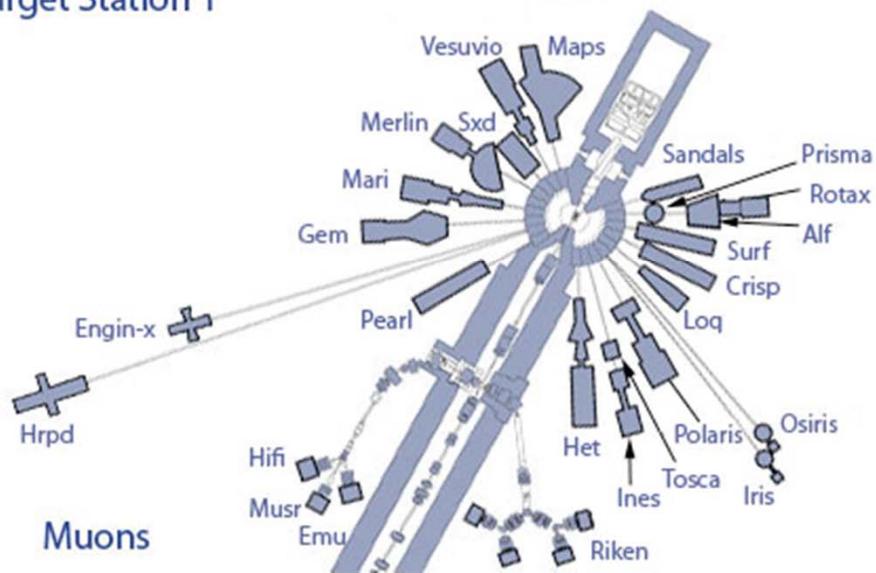
# Diffraction instruments at ILL



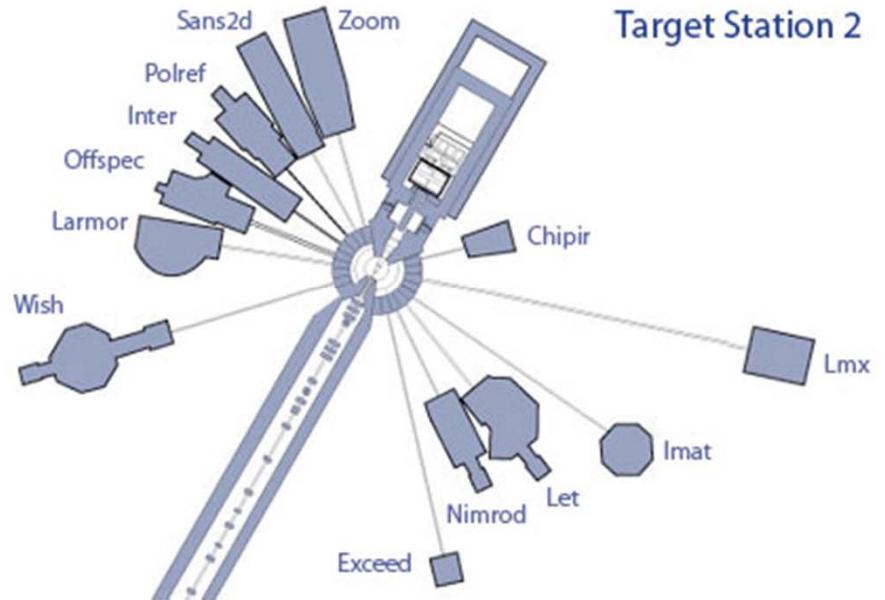
# Diffraction instruments at ISIS



Target Station 1



Target Station 2



# Principles of Diffraction



- The lattice
- Crystal systems
- Centering
- 3-D lattice types
- Miller indices/planes
- Bragg equation
- Ewald Sphere
- Reciprocal lattice
- Conditions for observing diffraction
- Laue diffraction

# Lattices & Unit Cells: 1-D



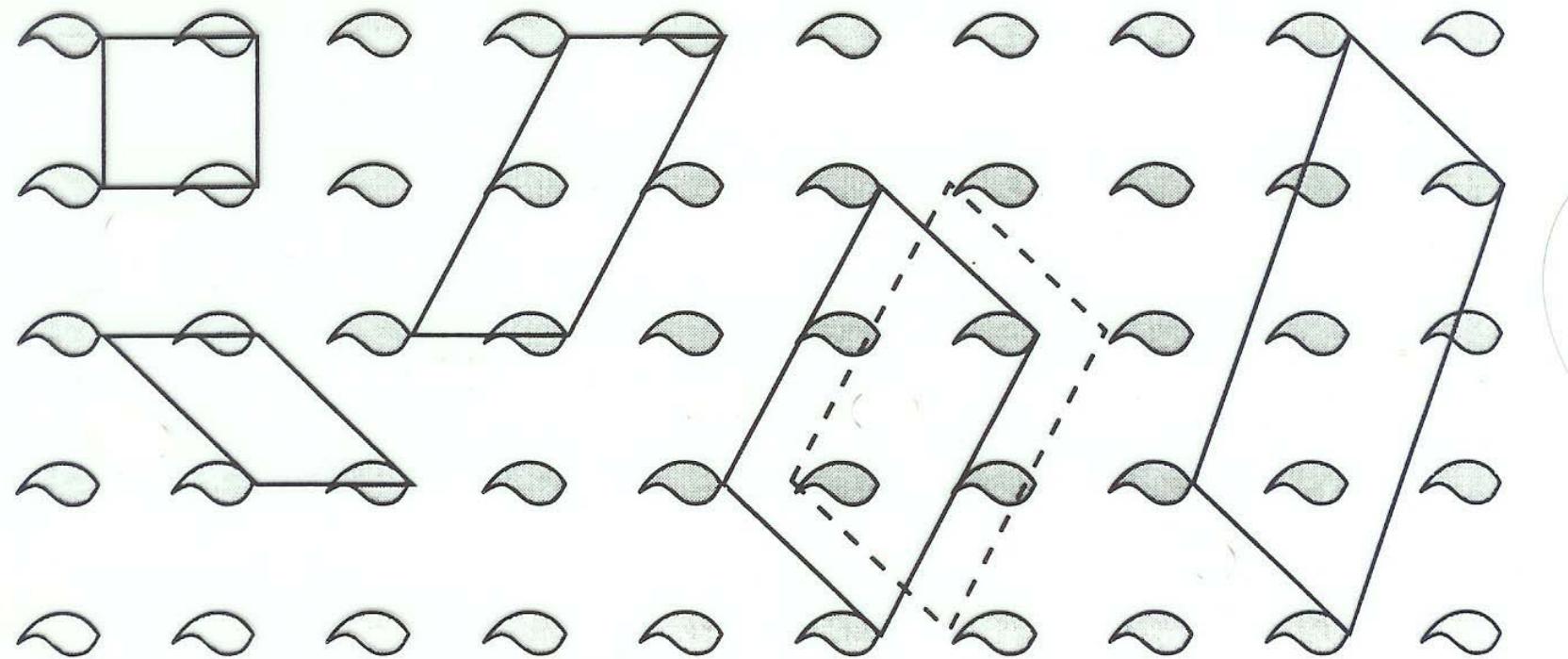
Lattice + Motif = Structure

The motif can be an atom, molecule, part of a molecule or several molecules are atoms

# Lattices & Unit Cells: 2-D

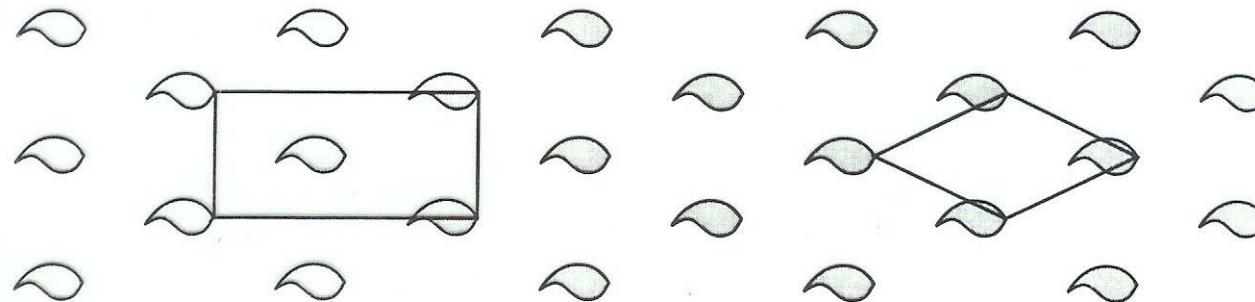


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All the cells highlighted are equally valid. All will reproduce the 2-D lattice array. The convention is to choose the smallest cell that also represents the symmetry of the structure.

# Lattices & Unit Cells: Centering

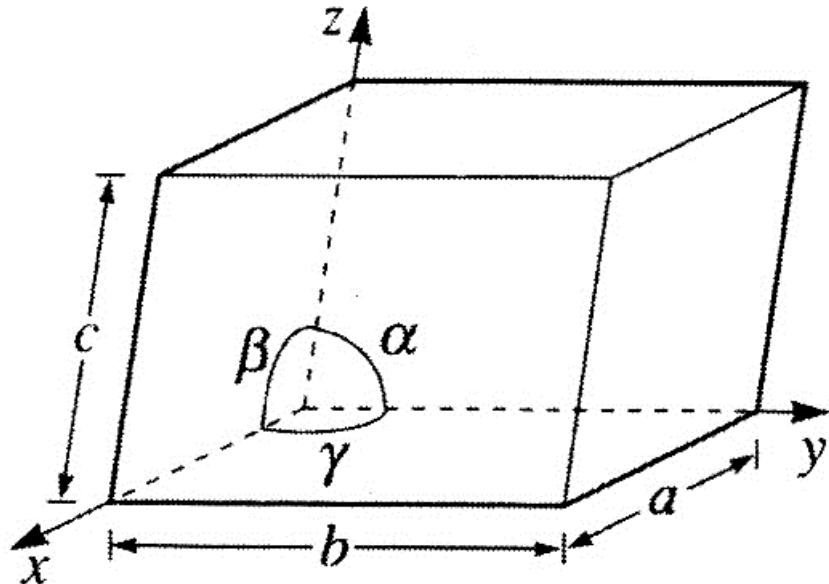


Centred v Primitive unit cell

Rules for unit cell selection:

- Unit cell should show the symmetry of the crystal
- Origin should be a geometrically unique point, priority given to inversion centre.
- Basic vectors should be as short as possible and the angle between them as close to  $90^\circ$  as possible.
- ALL angles diverting from  $90^\circ$  should be larger or smaller (convention is larger)

# Lattices & Unit Cells: 3-D



## Conventions

- cell parameters are in Å or pm
- Angles are in °

The unit cell has lattice parameters defined by the cell length  $a$ ,  $b$ , and  $c$ , and the cell angles  $\alpha$ ,  $\beta$ , and  $\gamma$ :

- $\gamma$  is angle between  $a$  and  $b$
- $\beta$  is angle between  $a$  and  $c$
- $\alpha$  is angle between  $b$  and  $c$

Atomic positions are given as xyz coordinates:

- $x$  is fraction of  $a$  axis
- $y$  is fraction of  $b$  axis
- $z$  is fraction of  $c$  axis

# Lattices & Unit Cells: 3-D crystal systems

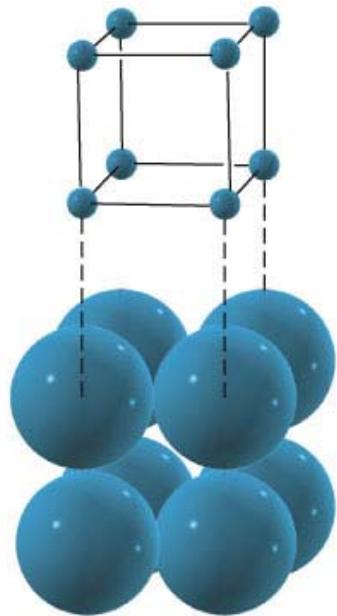


Triclinic	$a \neq b \neq c$	$\alpha \neq \beta \neq \gamma \neq 90^\circ$
Monoclinic	$a \neq b \neq c$	$\alpha = \gamma = 90^\circ \quad \beta \neq 90^\circ$
Orthorhombic	$a \neq b \neq c$	$\alpha = \beta = \gamma = 90^\circ$
Trigonal	$a = b = c$	$\alpha = \beta = \gamma \neq 90^\circ$
Hexagonal	$a = b \neq c$	$\alpha = \beta = 90^\circ \quad \gamma = 120^\circ$
Tetragonal	$a = b \neq c$	$\alpha = \beta = \gamma = 90^\circ$
Cubic	$a = b = c$	$\alpha = \beta = \gamma = 90^\circ$

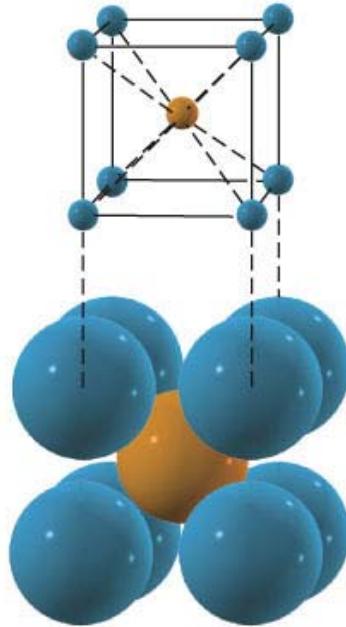
# Lattices & Unit Cells: 3-D Cell Setting

Primitive      Body-Centred      Face-Centred      Side-Centred

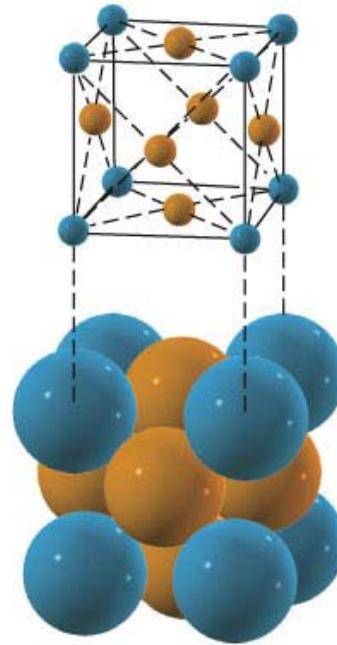
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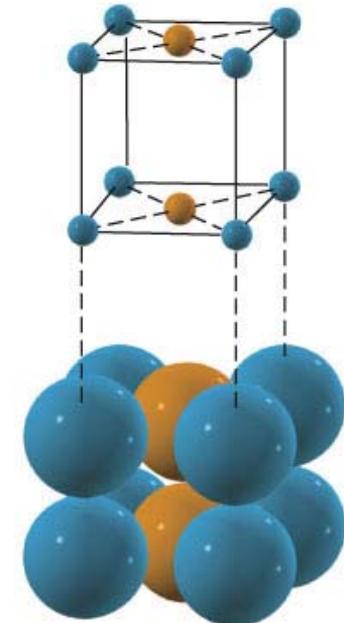
I



F



C



Atoms are identical even though coloured differently.

# Lattices & Unit Cells: 3-D lattice types

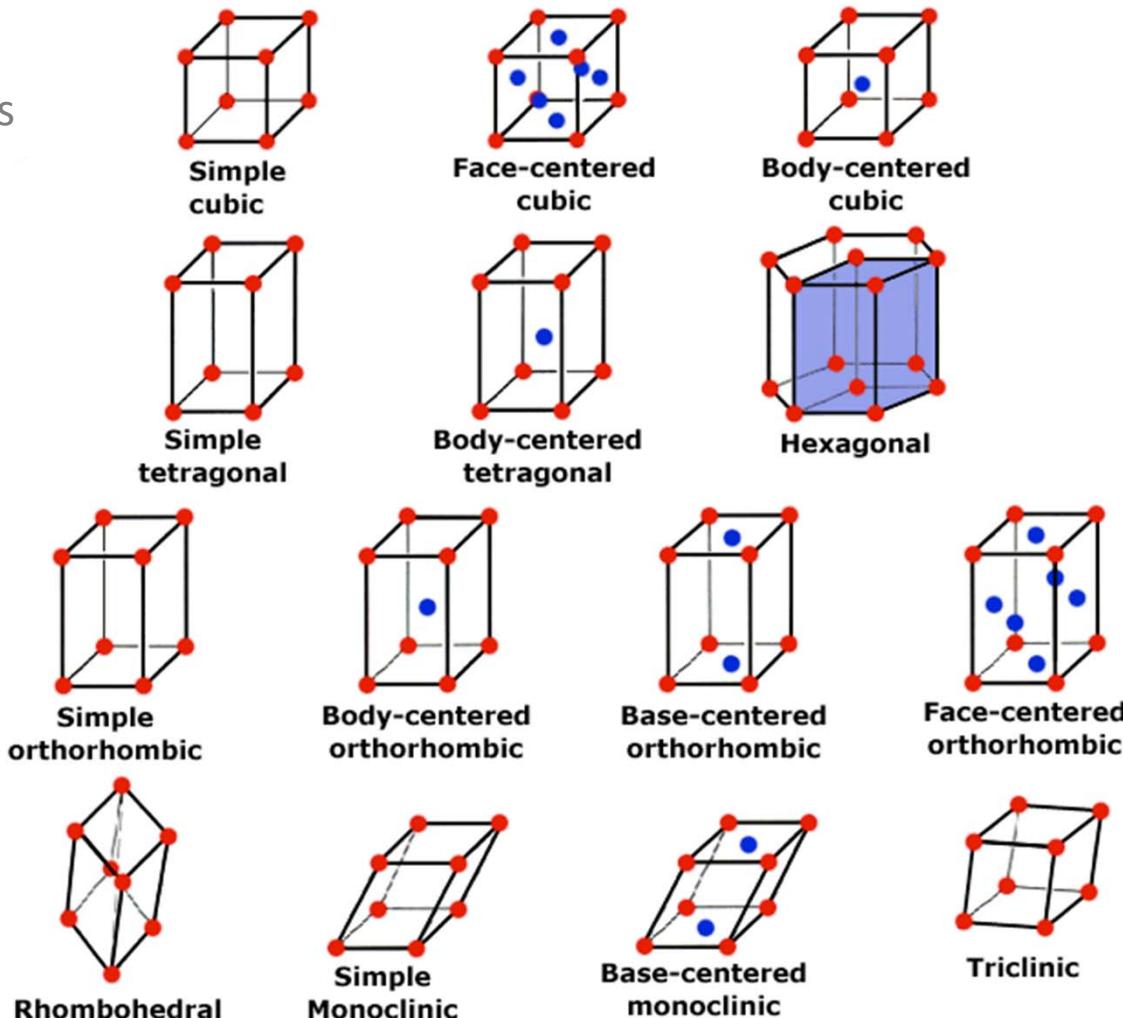


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7 crystal classes

14 Bravais Lattice types

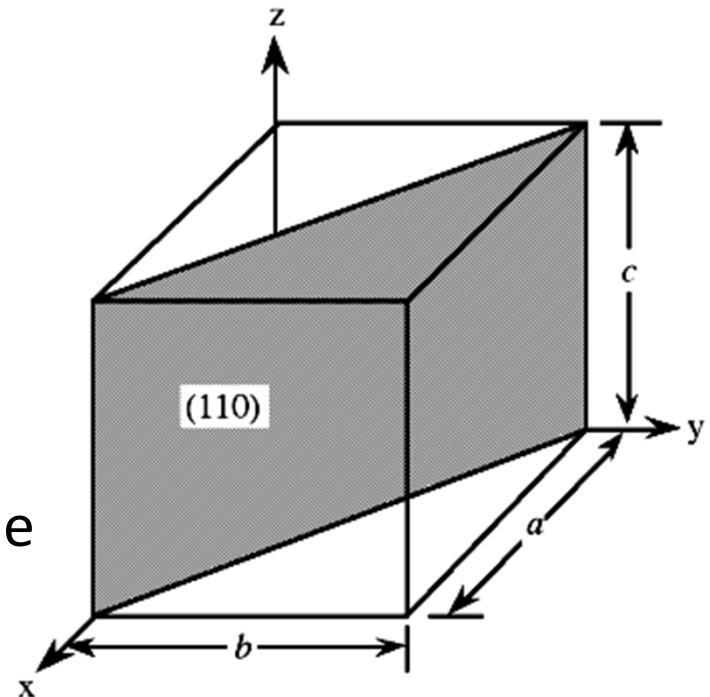
230 space groups



# Miller indices / planes

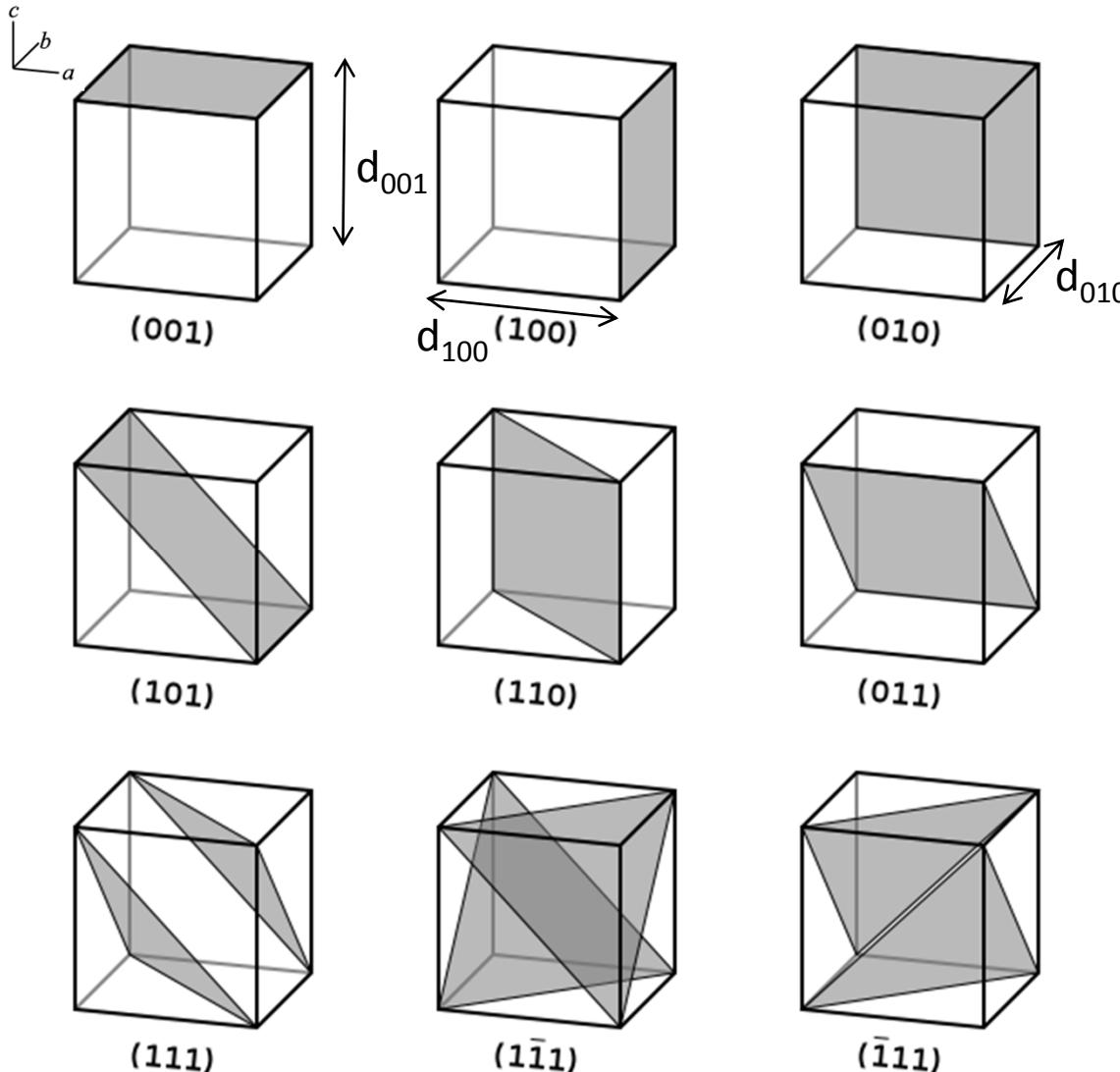
Unit cell planes can be defined by the notation called Miller indices. The Miller index is given as a hkl number where  $h$ ,  $k$ , and  $l$  are reciprocals of the plane with the  $x$ ,  $y$ , and  $z$  axes.

To obtain the Miller indices of a given plane requires the following steps:

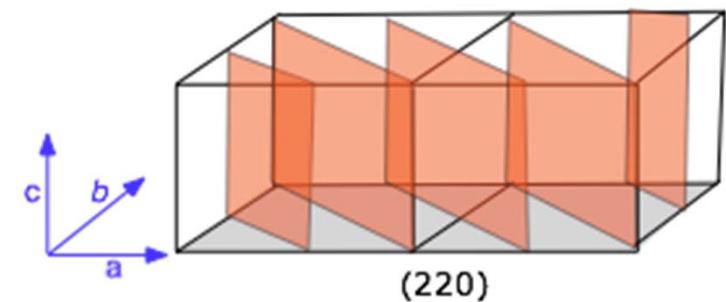


- Step 1. The plane in question is placed on a unit cell.
- Step 2. Find its intercepts with each of the crystal axes.
- Step 3. The reciprocal of the intercepts are taken.
- Step 4. Multiply by a scalar to get a ratio of integers.

# More Miller indices

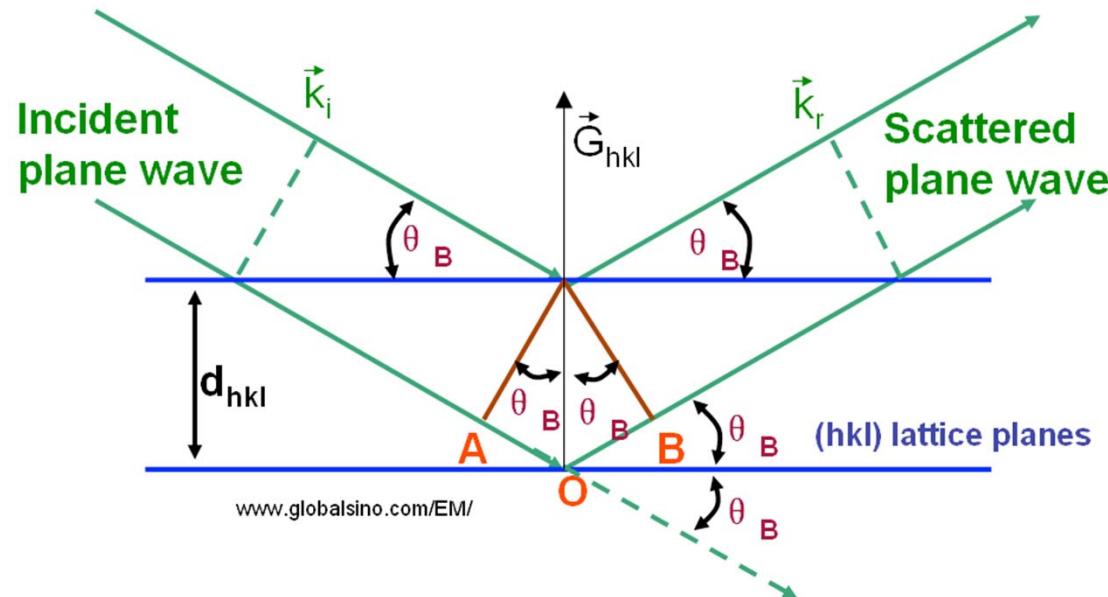


The higher the Miller index the less distance there is between equivalent planes, dividing the unit cell into ever smaller slices



For higher symmetry cells interplane distances are identical  
 $d_{001} = d_{010} = d_{100}$  for cubic

# Diffraction: The Bragg Law



- Constructive interference occurs when the waves reflected from adjacent scattering planes remain in phase – diffraction peak is observed
- The path difference travelled by waves between adjacent planes must be an integral multiple of the wavelength

$$n\lambda = 2d \sin \theta$$

# Distances Between Miller Planes



## d-spacings in different crystal systems

**Crystal system       $d_{hkl}$  as a function of Miller indices and lattice parameters**

Cubic      
$$\frac{1}{d^2} = \frac{h^2 + k^2 + l^2}{a^2}$$

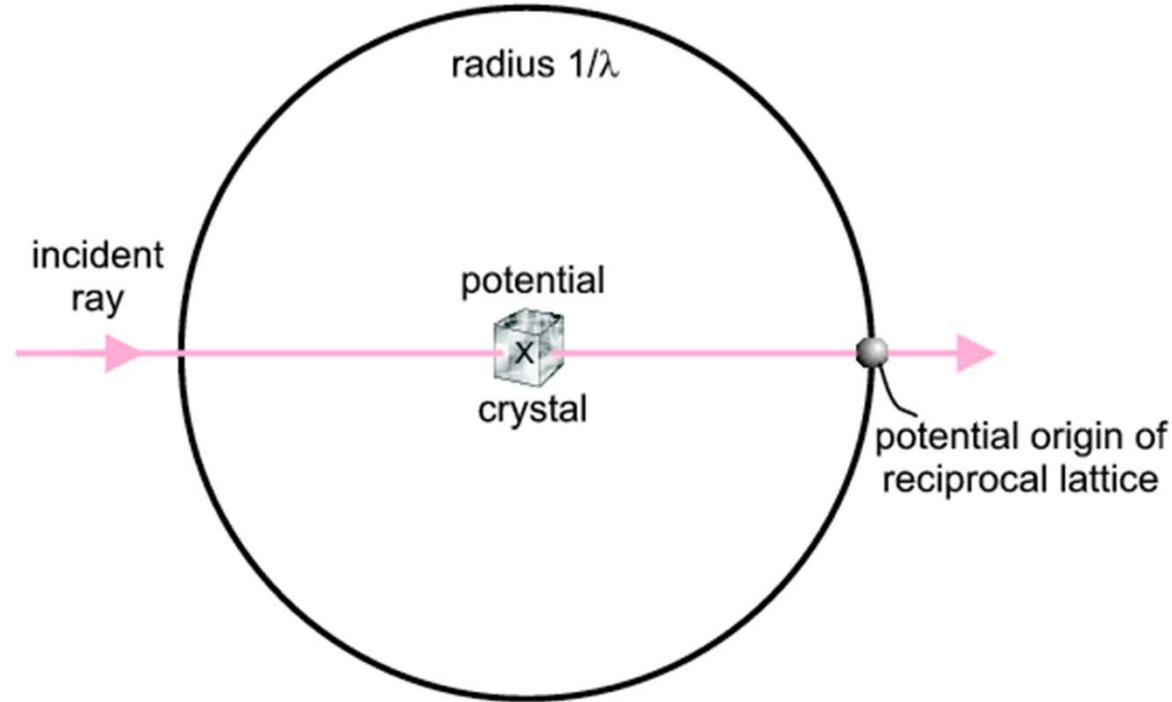
Tetragonal      
$$\frac{1}{d^2} = \frac{h^2 + k^2}{a^2} + \frac{l^2}{c^2}$$

Orthorhombic      
$$\frac{1}{d^2} = \frac{h^2}{a^2} + \frac{k^2}{b^2} + \frac{l^2}{c^2}$$

Hexagonal      
$$\frac{1}{d^2} = \frac{4}{3} \left( \frac{h^2 + hk + k^2}{a^2} \right) + \frac{l^2}{c^2}$$

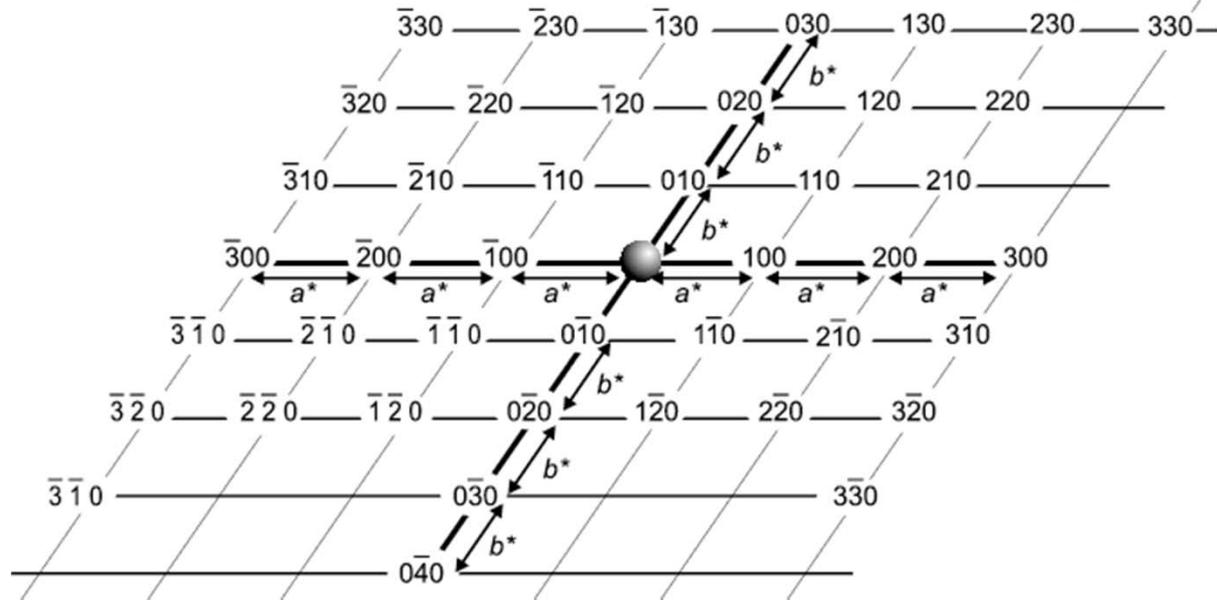
Monoclinic      
$$\frac{1}{d^2} = \frac{1}{\sin^2 \beta} \left( \frac{h^2}{a^2} + \frac{k^2 \sin^2 \beta}{b^2} + \frac{l^2}{c^2} - \frac{2hl \cos \beta}{ac} \right)$$

# The Ewald Sphere



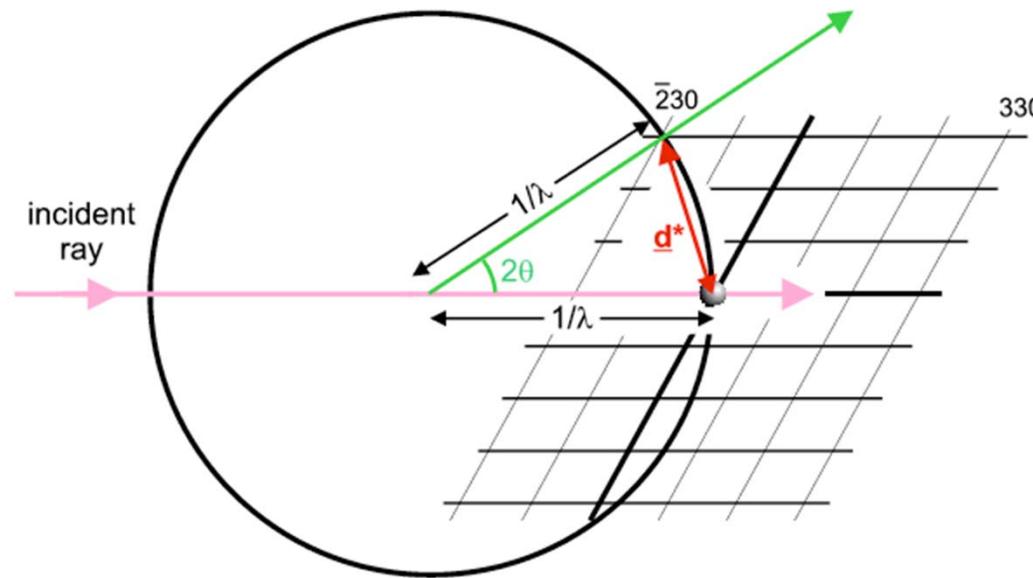
- Convenient visualisation tool especially for single crystal diffraction
- A sphere of radius  $1/\lambda$  (2-D projection shown above)
- Potential diffracted X-rays/neutrons can be along any radius from the centre of the sphere to the circumference (including out of plane in the projection above). This represents the experimental possibilities ( $\lambda$ , possible  $2\theta$ s)

# The Reciprocal Lattice



- Alternative view of the crystal structure ( $hk0$  plane illustrated)
- The reciprocal lattice consists of points which represent diffraction possibilities
- Each point can be labelled with a Miller index
- The units of this lattice are  $a^*$ ,  $b^*$  and  $c^*$  and any point can be reached using the vector equation  $d^* = ha^* + kb^* + lc^*$

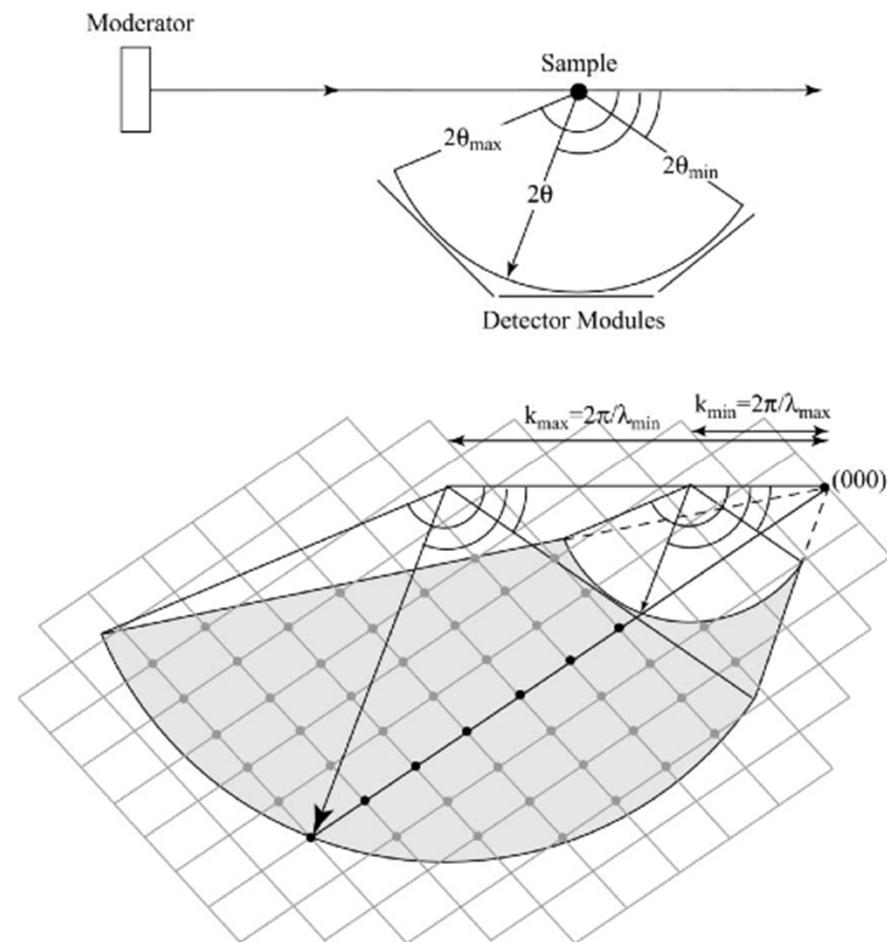
# Condition for Observing Bragg Diffraction



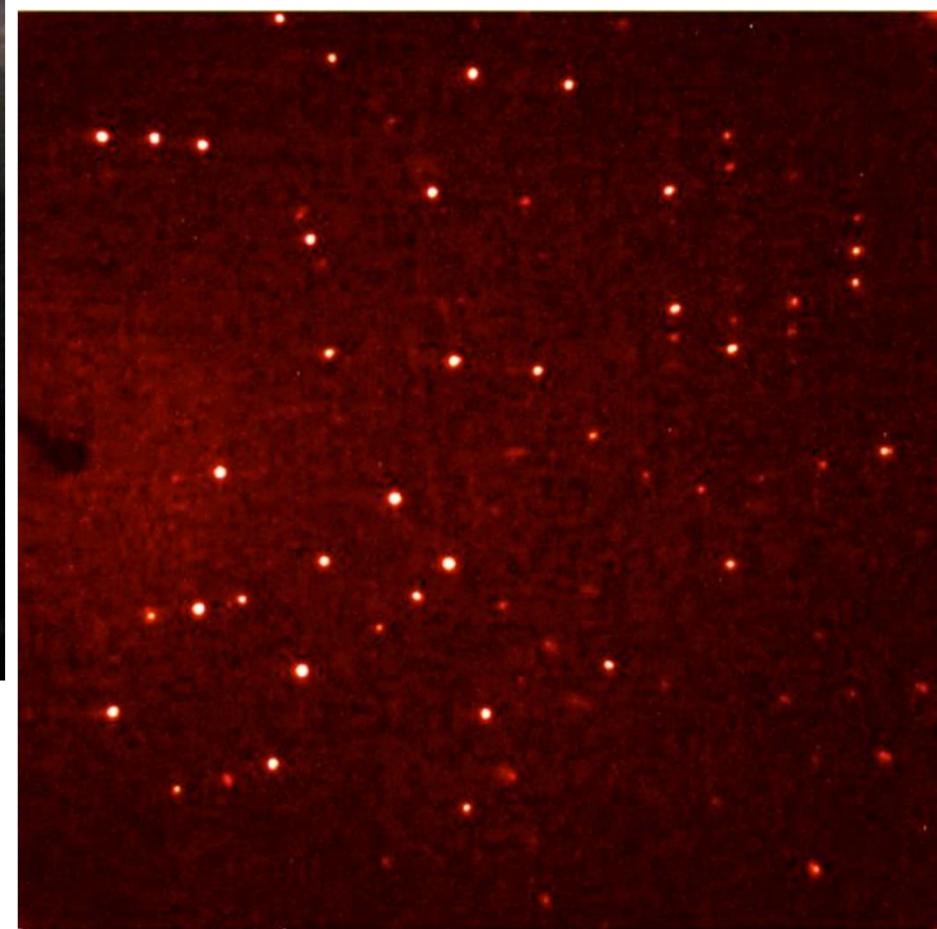
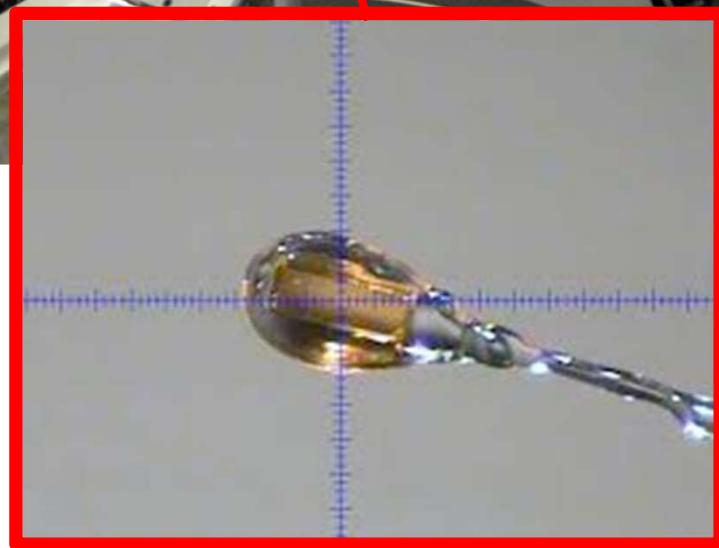
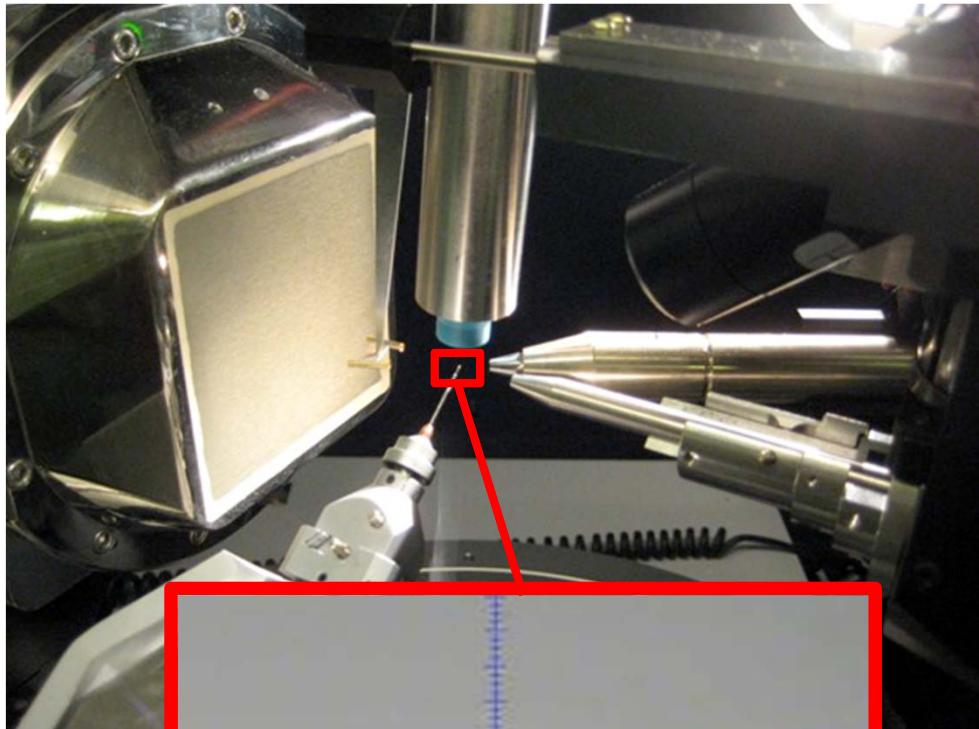
- Diffraction is observed whenever a reciprocal lattice point intersects the Ewald sphere (when Bragg condition is satisfied). Rotating the crystal will bring different lattice points into contact with the Ewald sphere.
- The direction of the diffracted ray is indicated in green
- The vector from origin to lattice point is  $d^*$  (reciprocal lattice spacing) is red – it is exactly equal to  $1/d$  and its direction is perpendicular to the  $hkl$  plane

# The Laue method

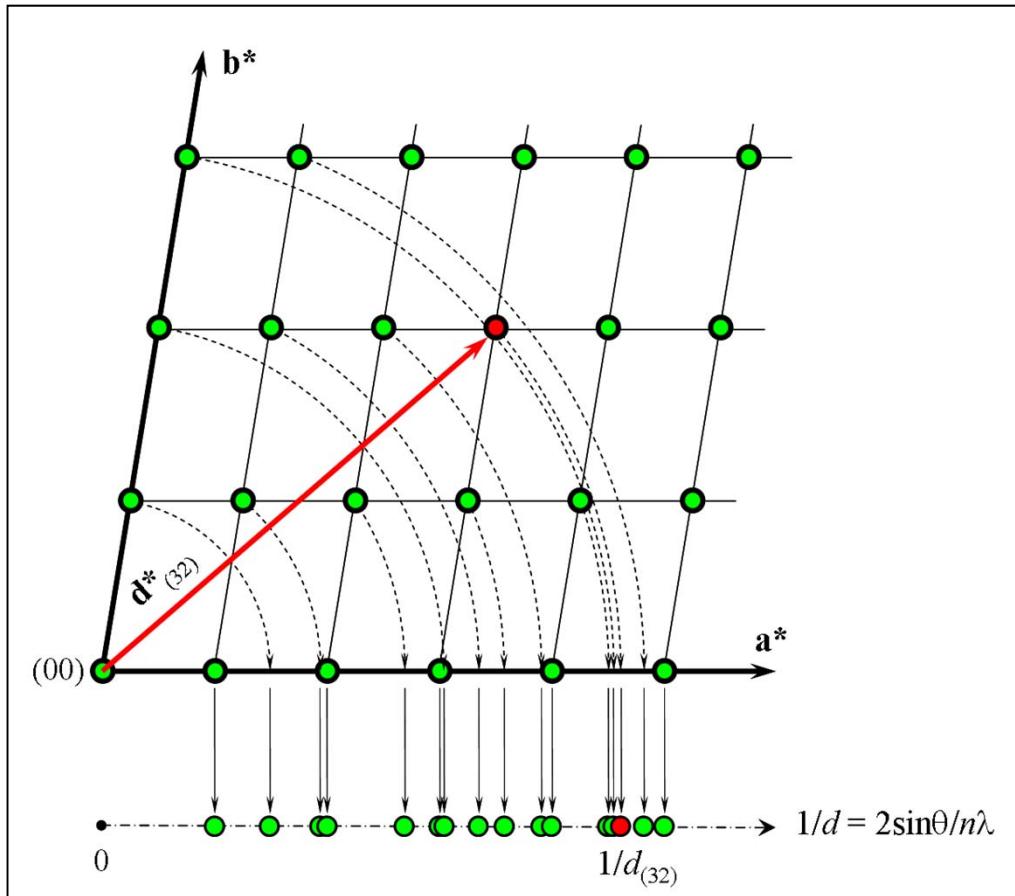
- Use a wavelength band to sample larger volume of reciprocal space
- A wide wavelength band covers a large reciprocal space volume
- Limits are  $\lambda_{\min}$ ,  $\lambda_{\max}$ , the accessible scattering angle of the instrument and the diffraction limit of the crystal
- All reciprocal lattice points that lie in the shaded region will be sampled simultaneously
- More chance of spatial overlap of reflections, particularly with large unit cells
- Detector technology becomes paramount – image plate v continuous output
- Wavelength band must be well characterised for data normalisation



# Diffraction set-up for a single crystal



# Powder diffraction in reciprocal space

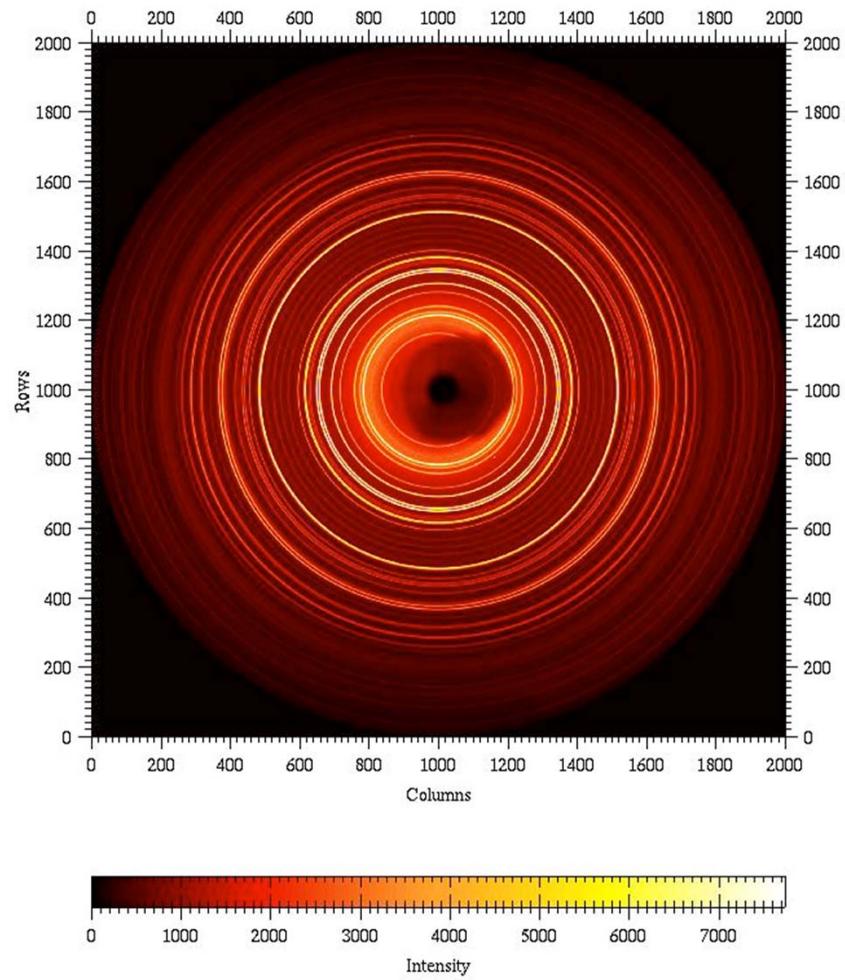
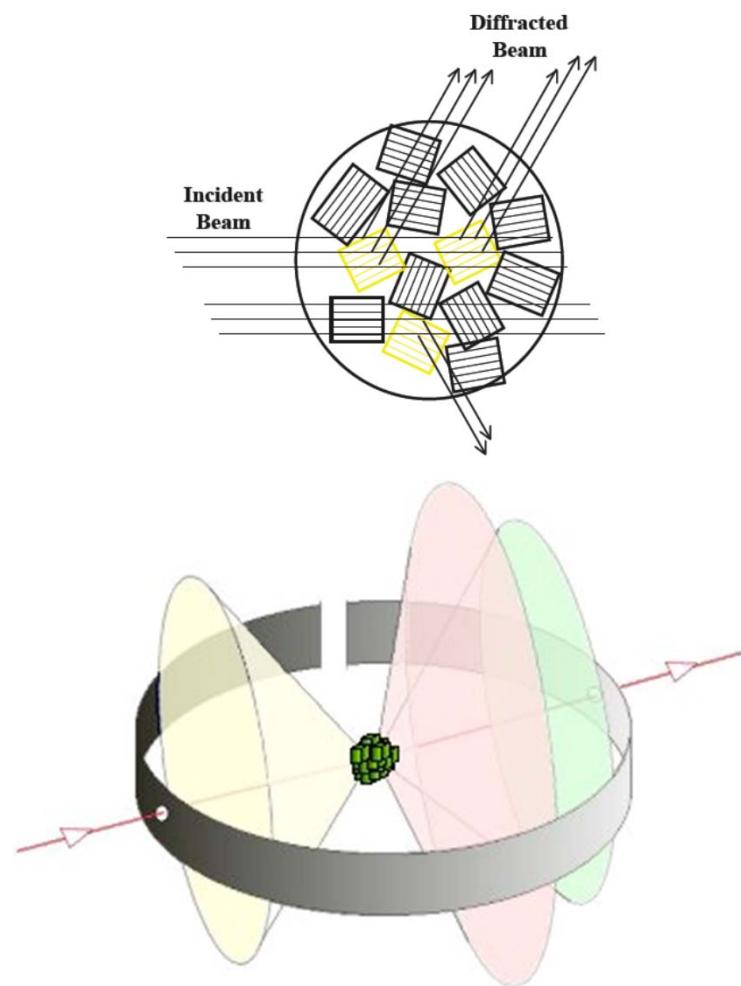


- Many crystallites with random orientation mean that each reciprocal lattice point will occur in every orientation possible, broadening into the surface of a sphere with radius  $d^*$
- The intersection of the Ewald sphere and the reciprocal lattice becomes a cone (intersection of 2 spheres)
- The directions of the vectors are lost and only the lengths of the reciprocal lattice vectors are measurable with powder diffractometers
- 3-D collapsed into 1-D

# Diffraction from a powder



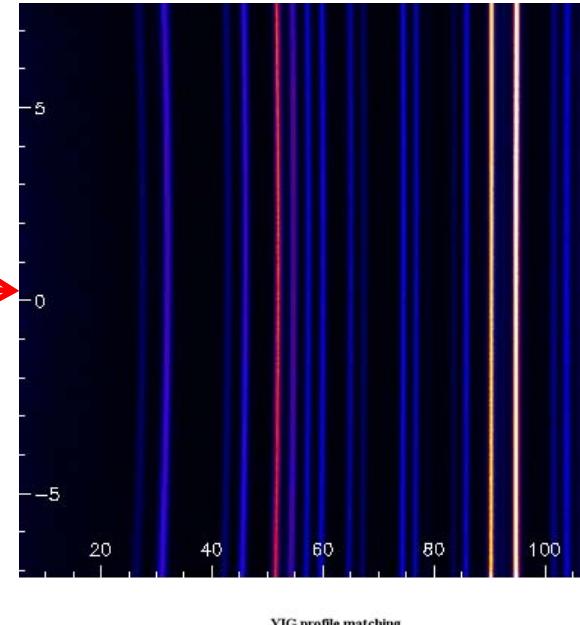
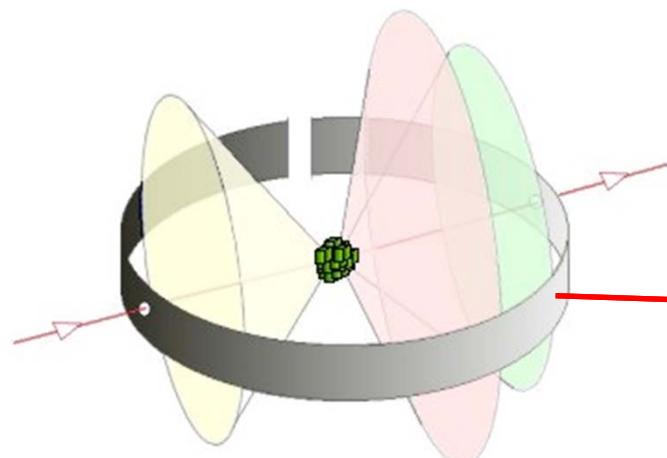
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# Diffraction from a powder

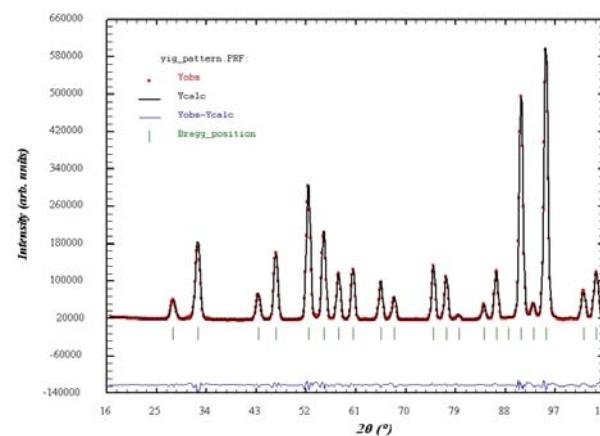


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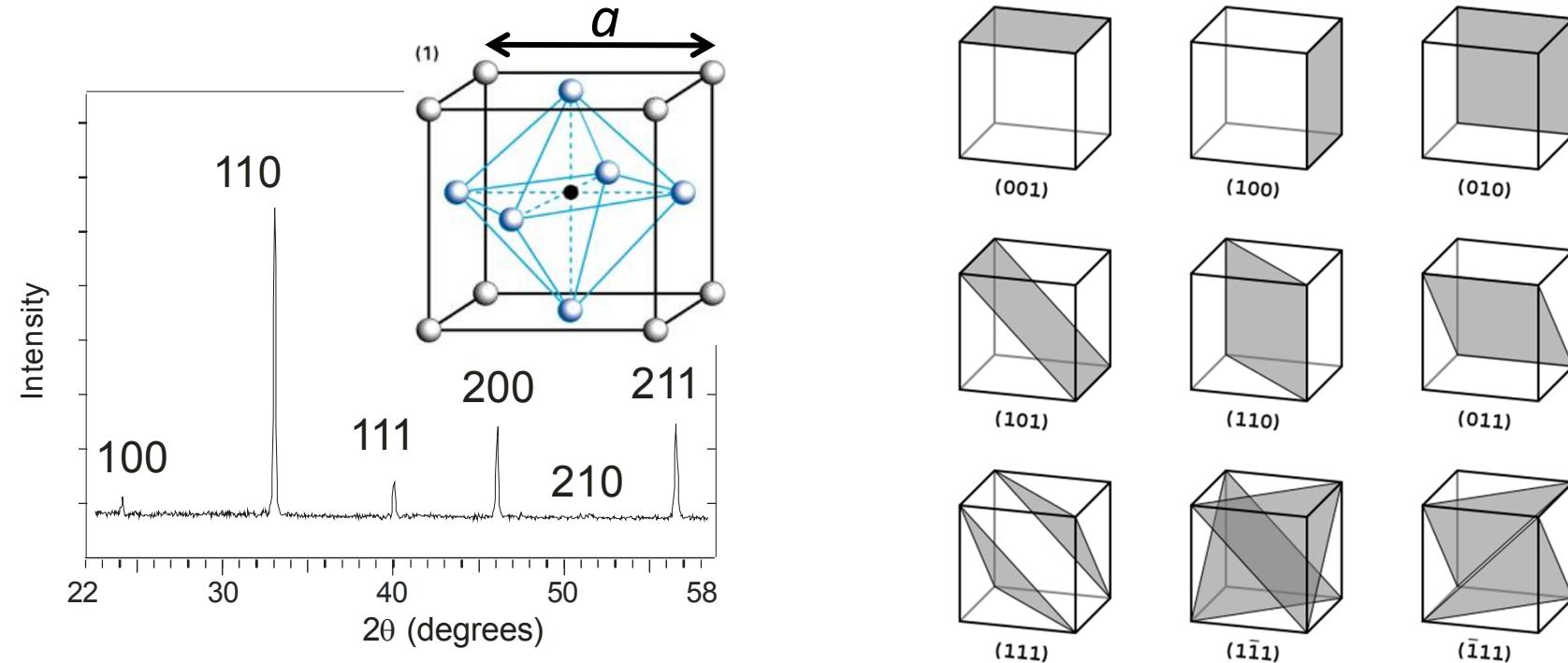


Typical monochromatic powder diffractometer

- Area or point detector and scans scattering angle intersecting the Debye-Scherrer cones
- Collapse into 1-D diffraction pattern



# Miller Planes and Powder Diffraction

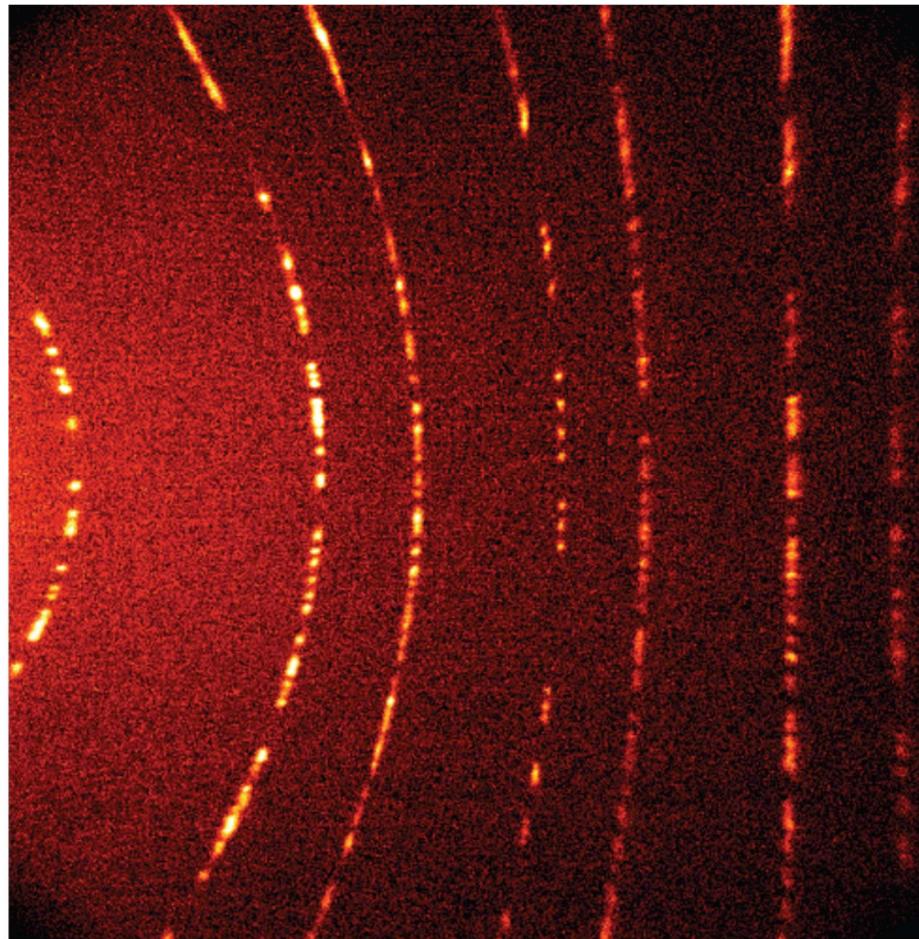


All equivalent planes occur at same scattering angle

All planes separated by the same distance occur at one scattering angle in powder diffraction

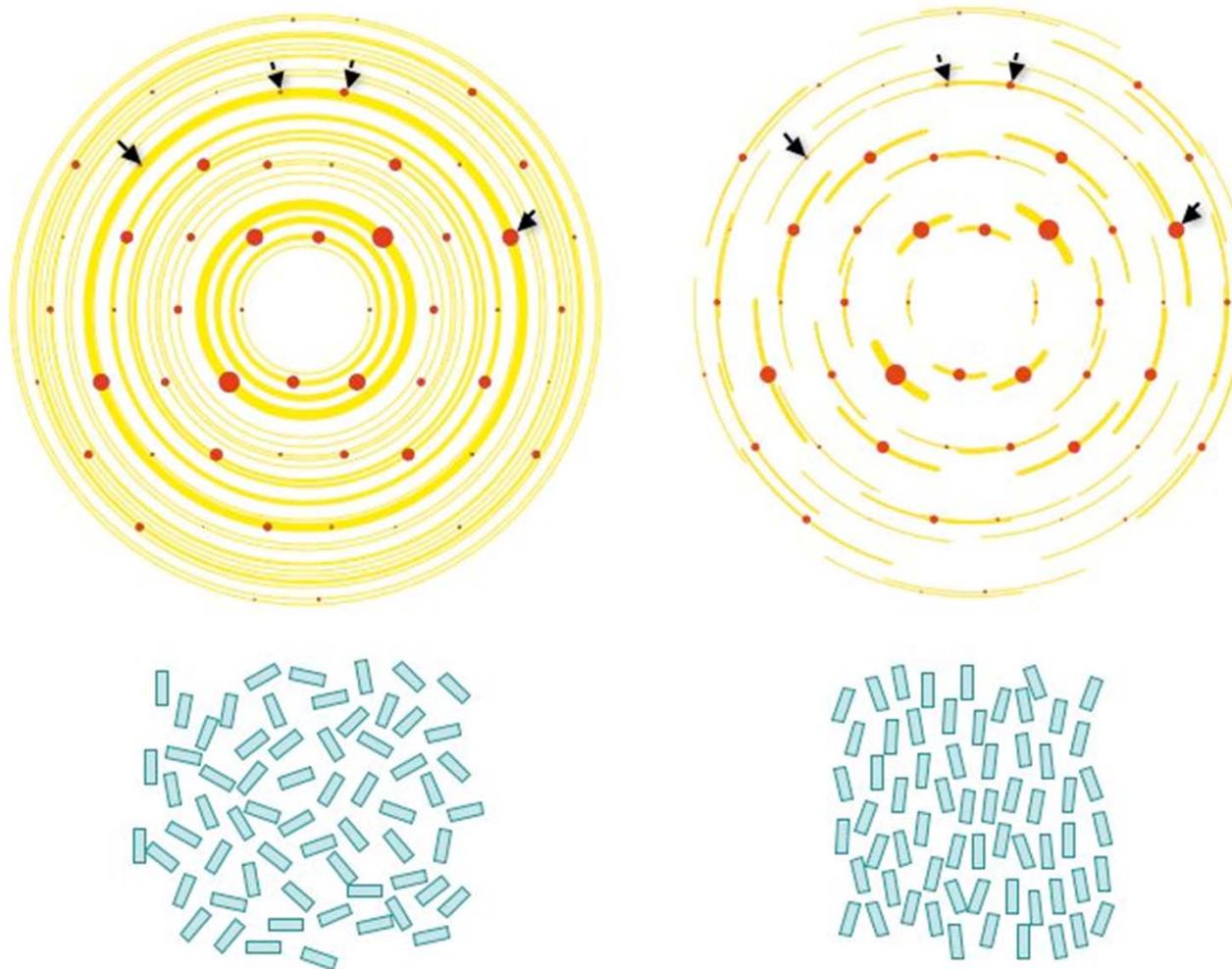
e.g. (511) and (333) occur at same  $2\theta$  for a cubic material

# Diffraction from a few crystals or a non-powder average (preferred orientation)

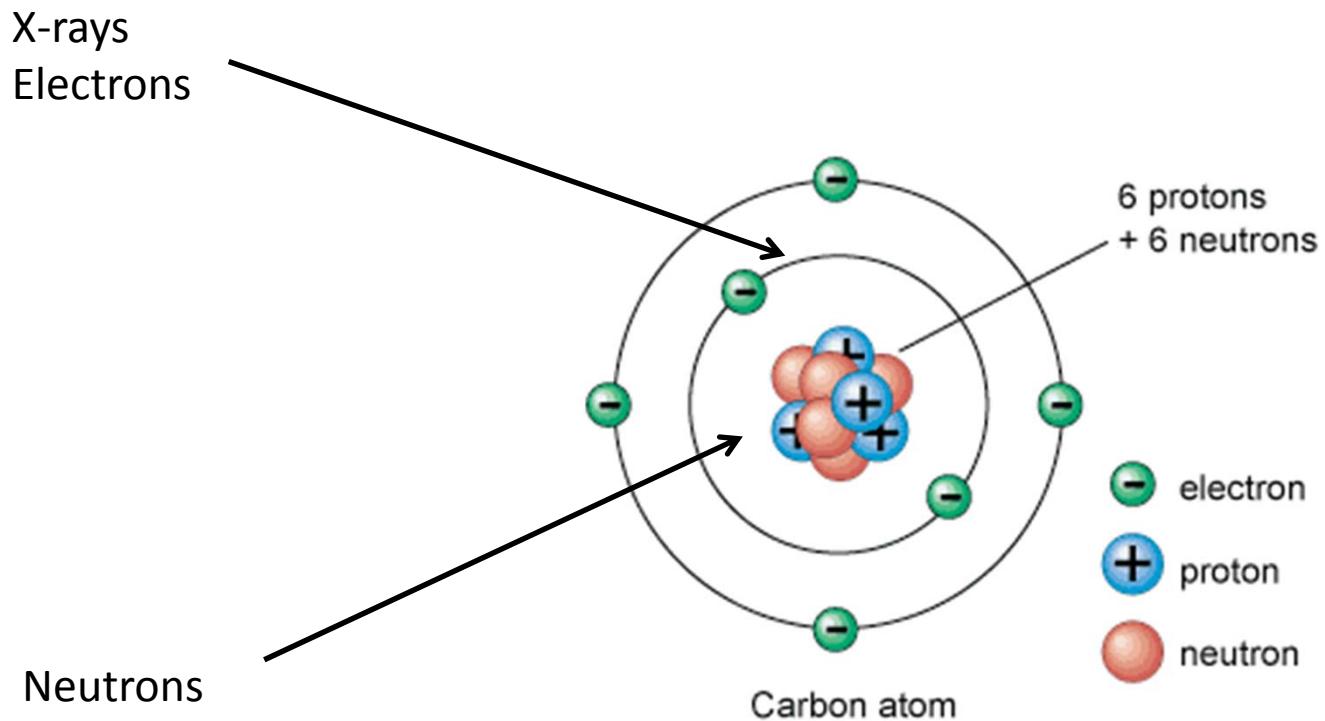


- When number of crystals is too small, the pattern becomes “grainy” -- diffraction from individual crystals dominate.
- Increase sample size
- Grind the sample to decrease domain size
- Oscillate or rotate the sample
- Use area detection & integrate the entire ring.

# Diffraction from a few crystals or a non-powder average (preferred orientation)



# X-rays and Neutrons are Complementary Probes for Diffraction



Neutron diffraction is used for problems that X-rays cannot address or inadequately address

# X-rays vs neutrons for Diffraction



## X-rays

Small samples  
Strong absorption  
High energy ( $1 \text{ \AA} - 12.4 \text{ keV}$ )  
Low penetration depth  
Light elements hard to detect  
Scattering power highly Q dependent  
Neighbouring elements cannot be discriminated  
High availability (lab)  
Cannot distinguish isotopes

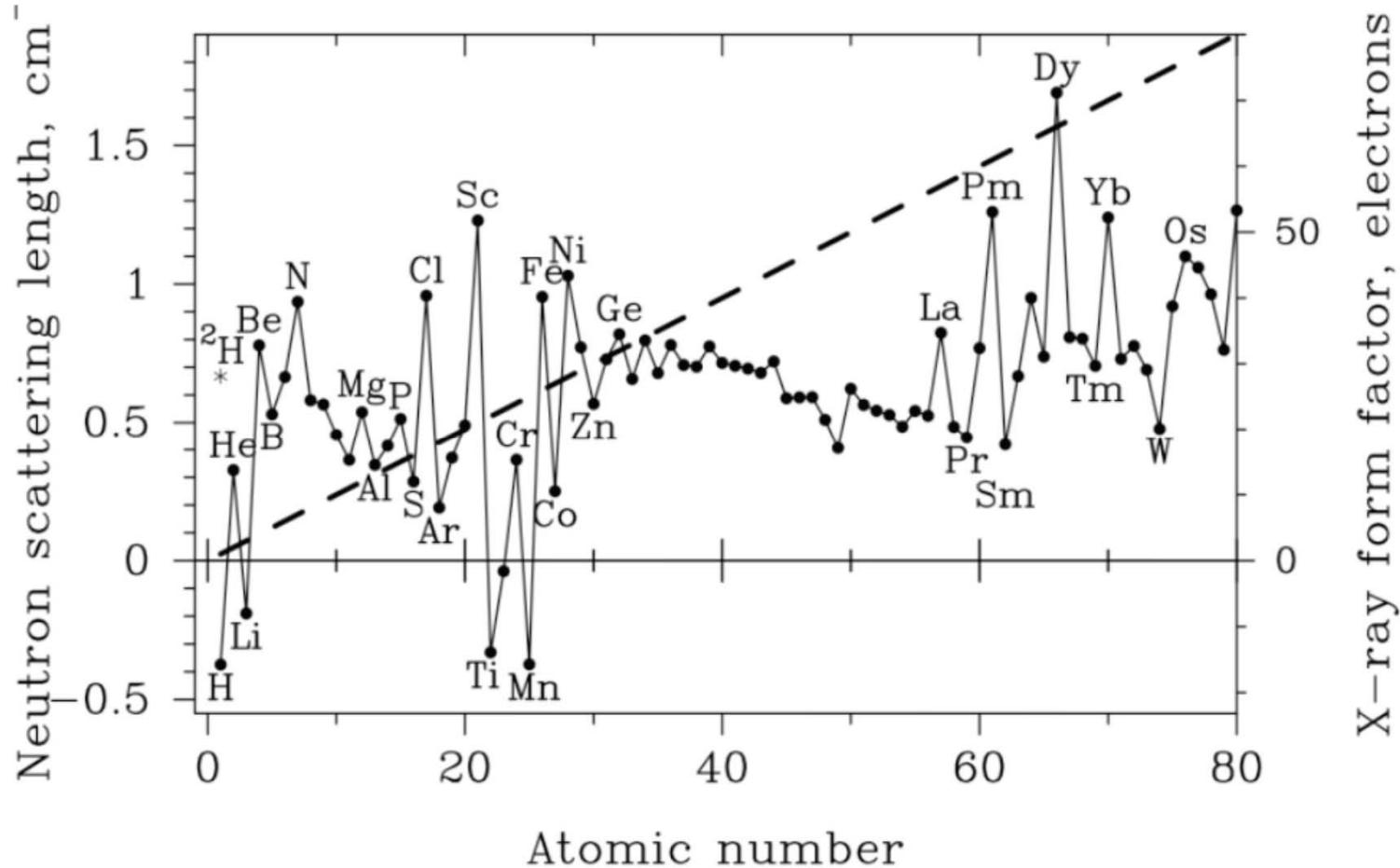
## Neutrons

Large samples  
Low absorption  
Low energy ( $1 \text{ \AA} = 81.81 \text{ meV}$ )  
High penetration depth  
Light elements can be seen  
Scattering power almost Q independent  
Neighbouring elements can be discriminated  
Low availability (large scale fac)  
Isotopes can be distinguished  
Magnetic structures easily probed

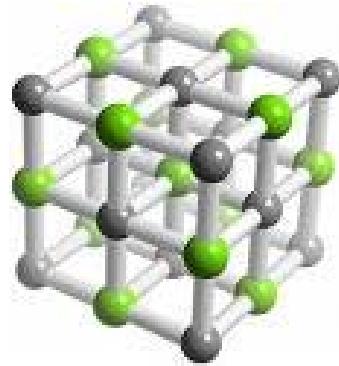
# X-ray vs neutron scattering power



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# Neighbouring Element Discrimination



KCl

Fm-3m  $a = 6.29 \text{ \AA}$

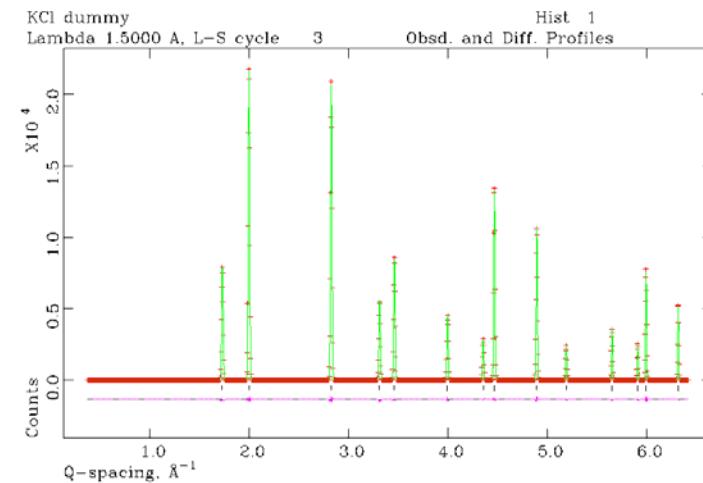
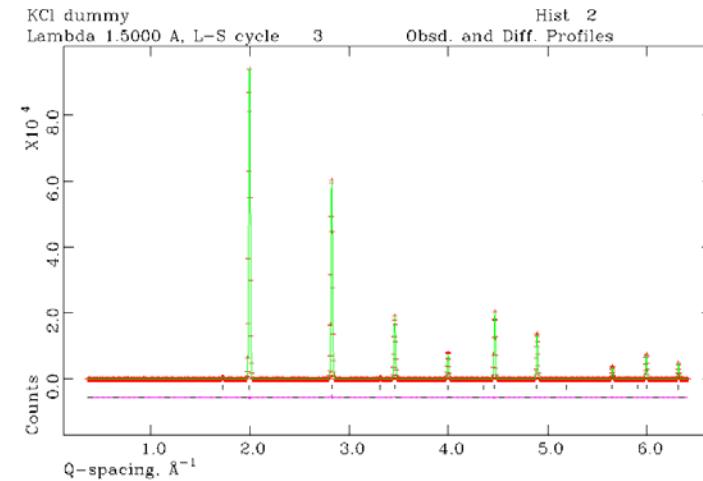
K z = 19

Cl z = 17

But  $K^+ = Cl^- = 18 e^-$

Without care KCl indexes from X-ray data on a cell that is  $\frac{1}{2}$  that from neutron data as elements are identical to X-rays as both have  $18 e^-$

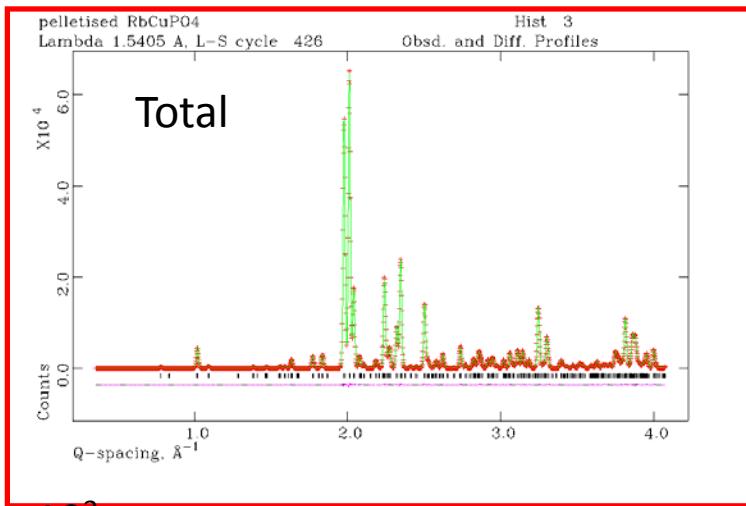
The non-linear relationship of neutron scattering length between neighbouring elements is crucial



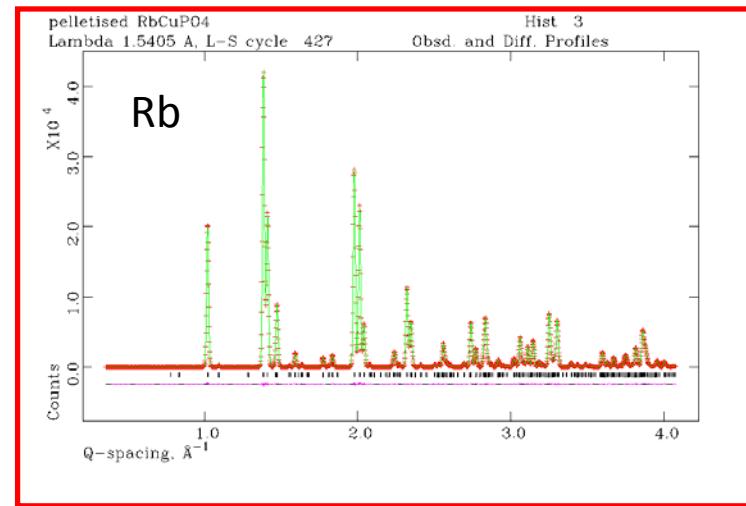
# Scattering contributions RbCuPO<sub>4</sub> (X-rays)



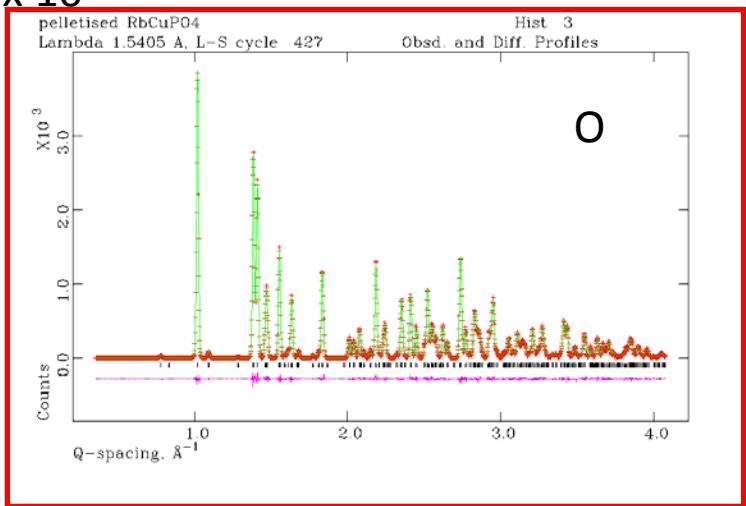
$6 \times 10^4$



$4 \times 10^4$



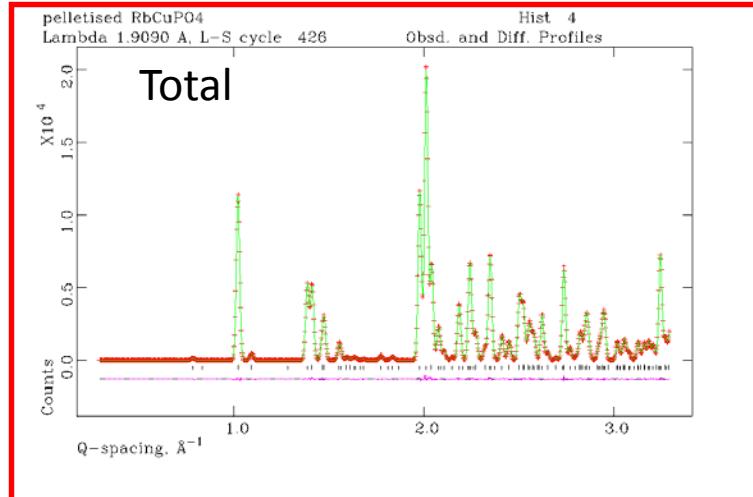
$3.5 \times 10^3$



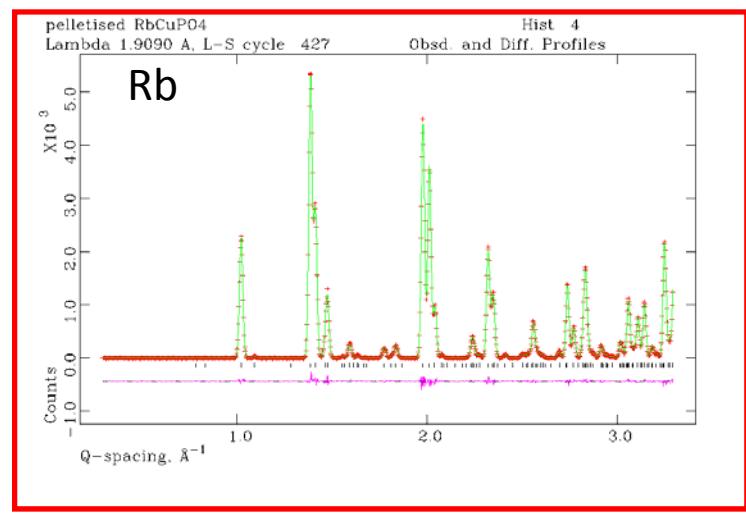
- Rb scattering contribution is factor 10 higher
- Cu and P contributions not shown
- Total is not just a simple sum of the contributions
- Evidence of the differing phase of the Rb and O to F<sub>hkl</sub> hence I<sub>hkl</sub>

# Scattering contributions RbCuPO<sub>4</sub> (neutron)

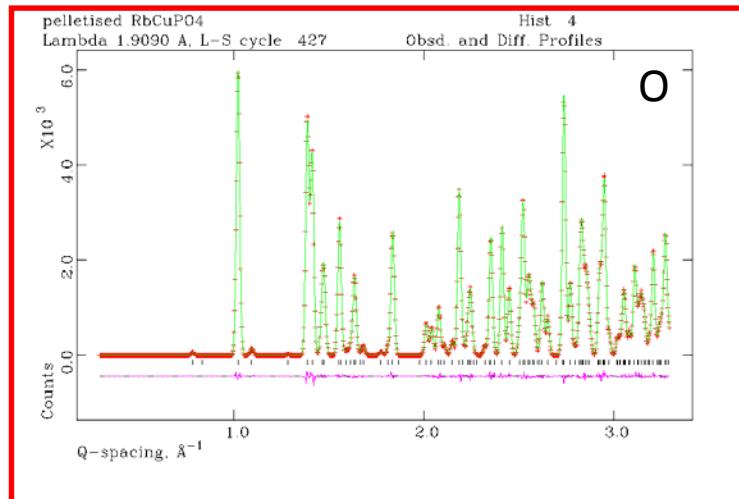
$2 \times 10^4$



$5 \times 10^3$



$6 \times 10^3$

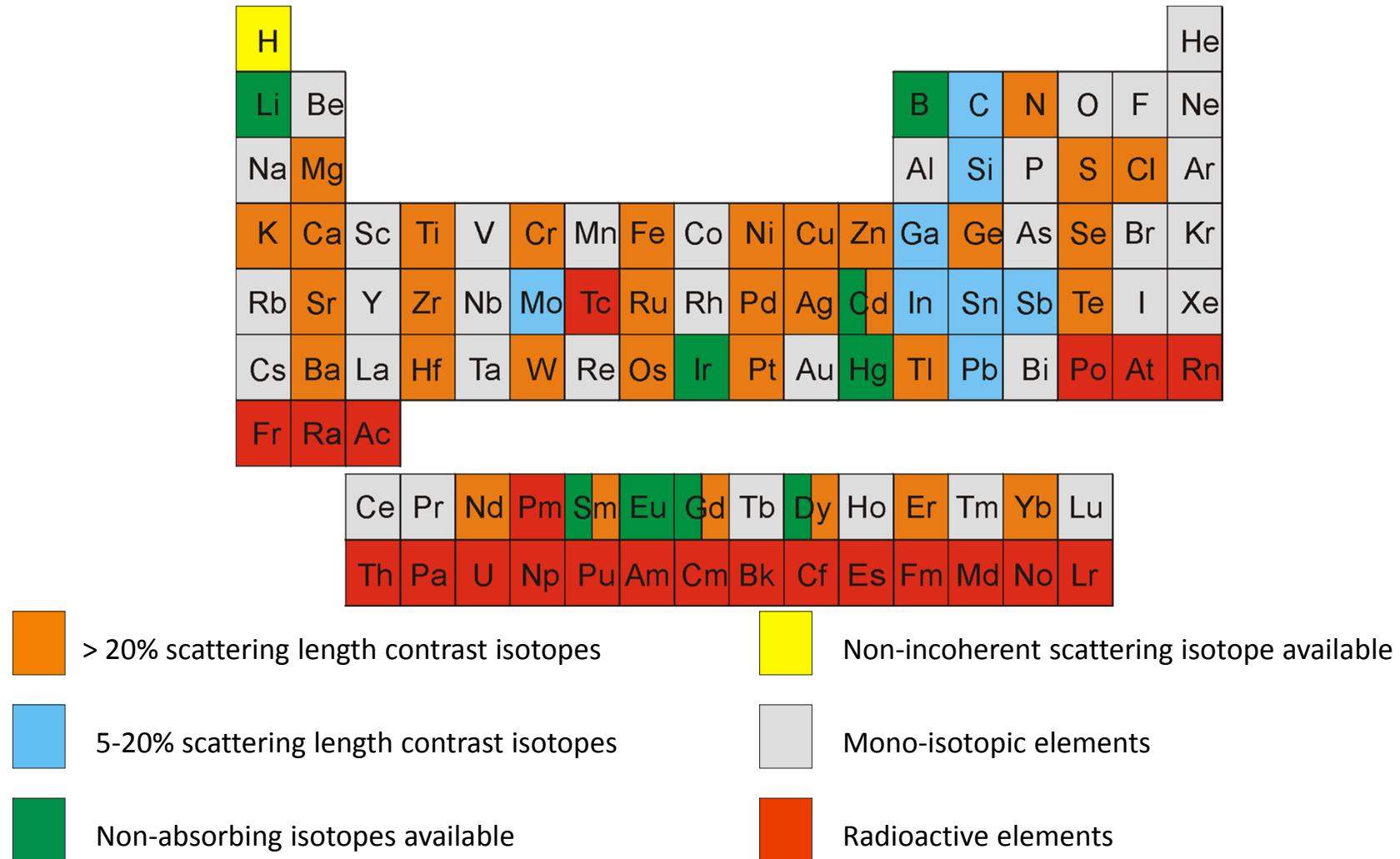


- Rb and O scattering contributions similar
- Cu and P contributions not shown
- Total is not just a simple sum of the contributions
- Evidence of the differing phase of the Rb and O to  $F_{hkl}$  hence  $I_{hkl}$

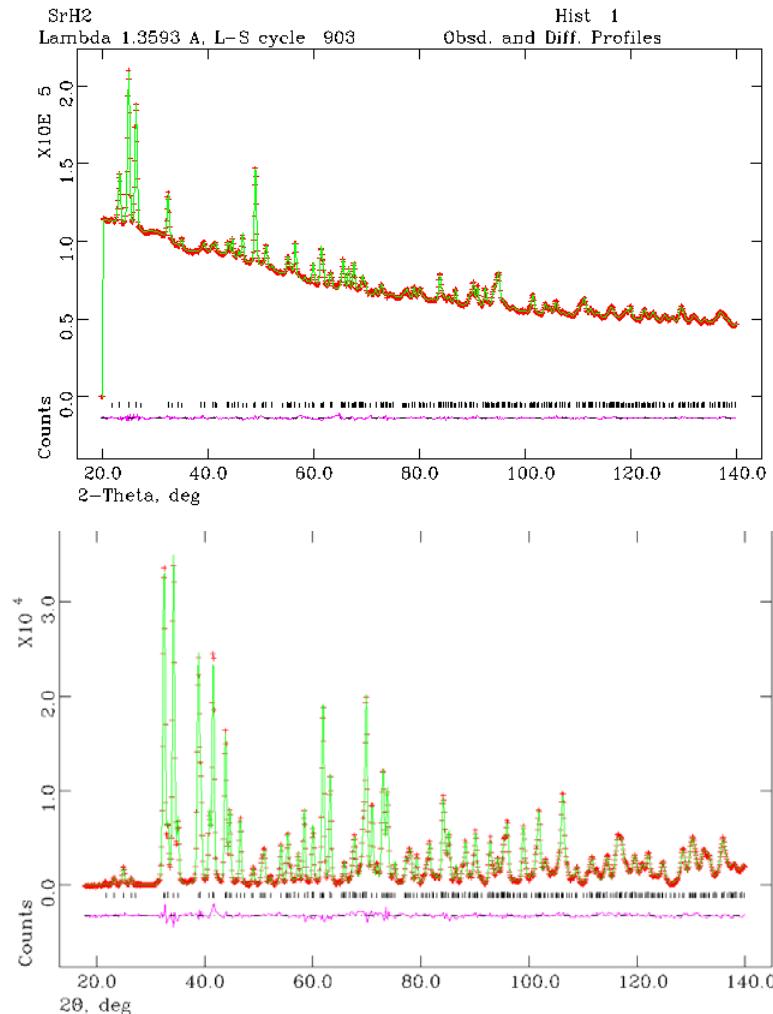
# Scattering contrast isotopes



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# Isotope coherent scattering length contrast



SrH<sub>2</sub> (top) v SrD<sub>2</sub> (bottom)

Structures are identical

Scattering lengths

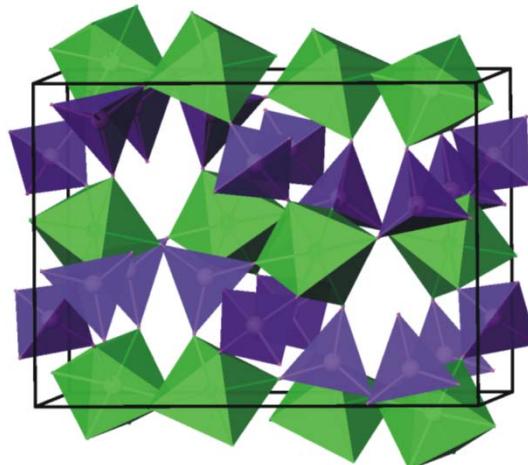
H -3.739 fm

D 6.67 fm

Negative scattering length  
signifies a change in the phase  
of the scattered neutron

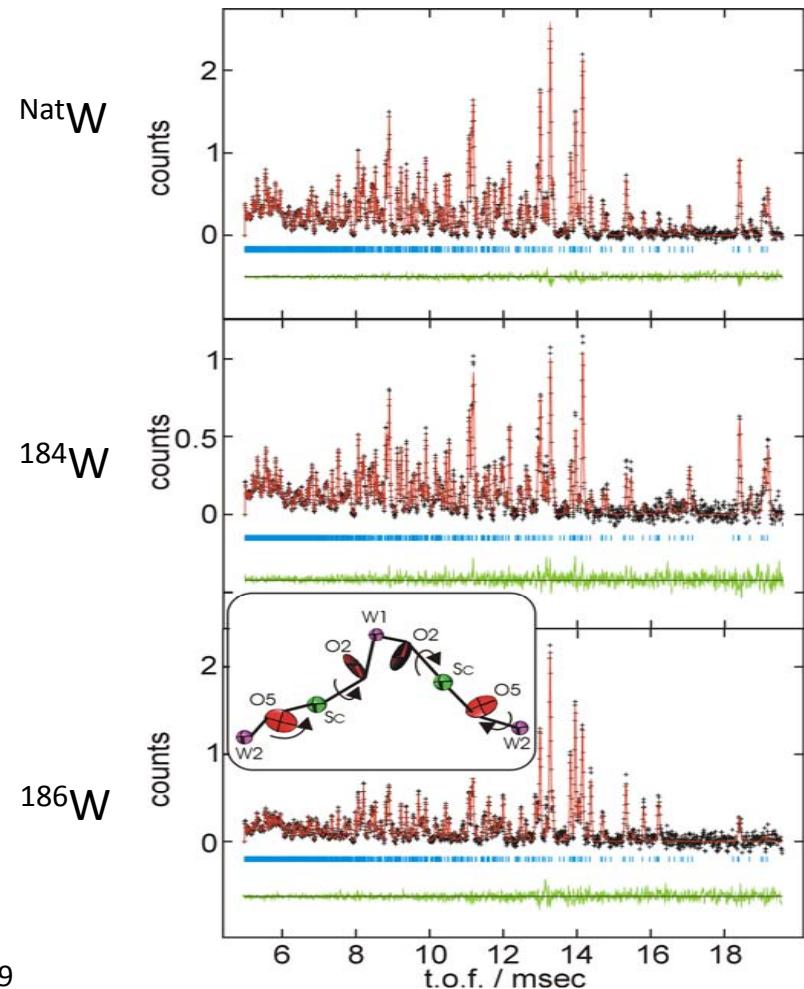
X-ray patterns are identical and  
H contribution is negligible to  
total scattering intensity

# Origin of NTE in $\text{Sc}_2(\text{WO}_4)_3$



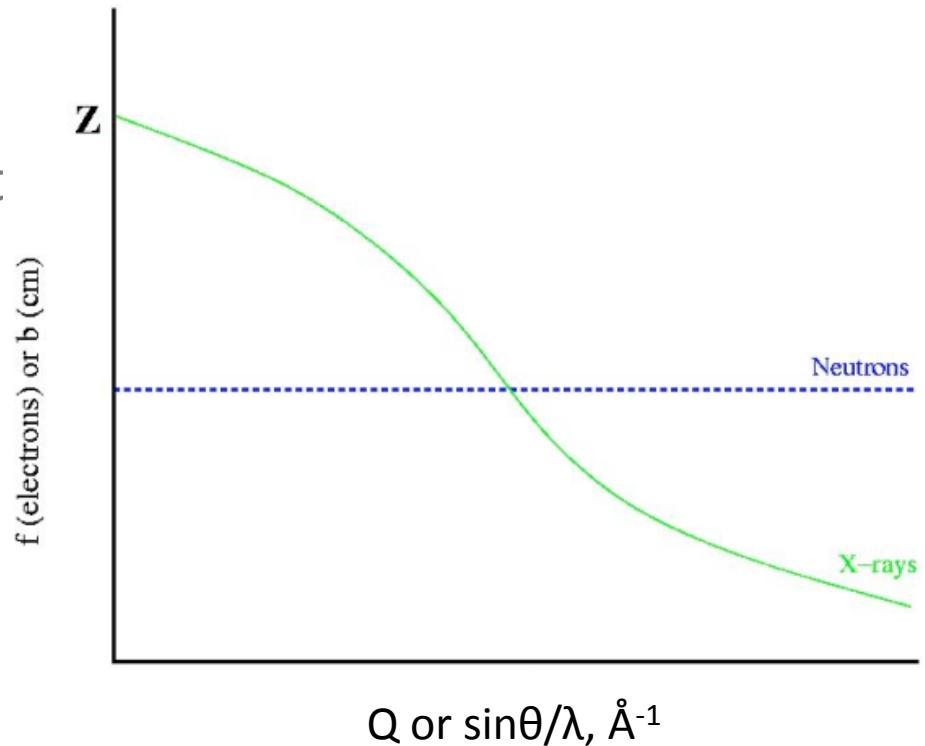
- Resolved co-operative atomic displacements
- First example using PND
- 10 years later same experiment possible without ISND on upgraded instrument HRPD

M.T. Weller, P.F. Henry, C.C. Wilson. *J. Phys. Chem. B* 2000, **105**(51), 12224-12229



# Form factor

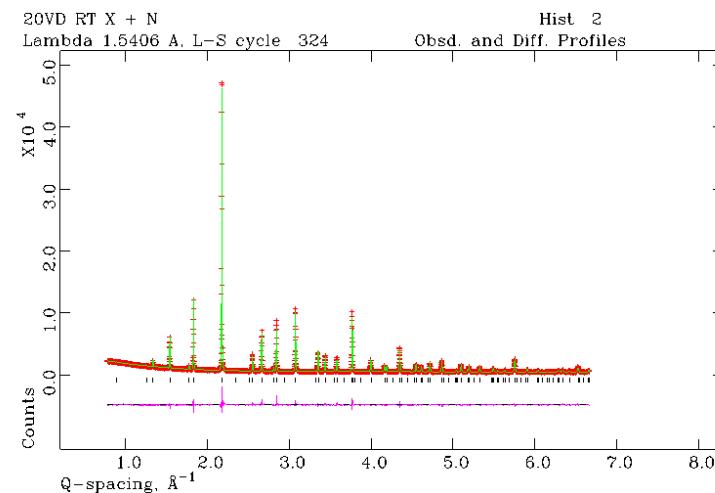
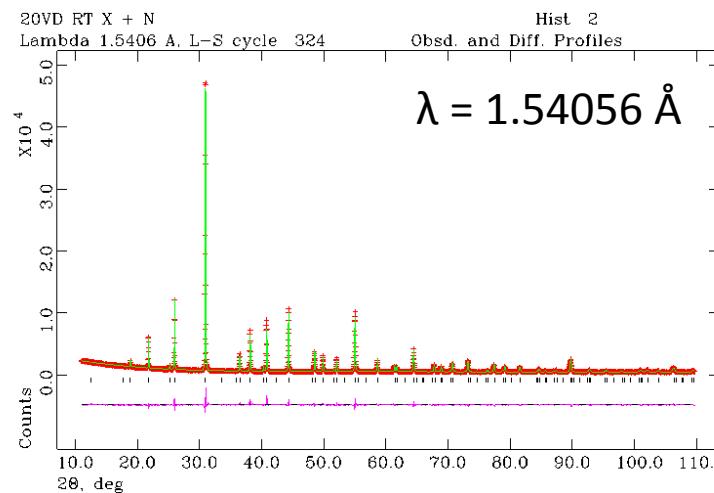
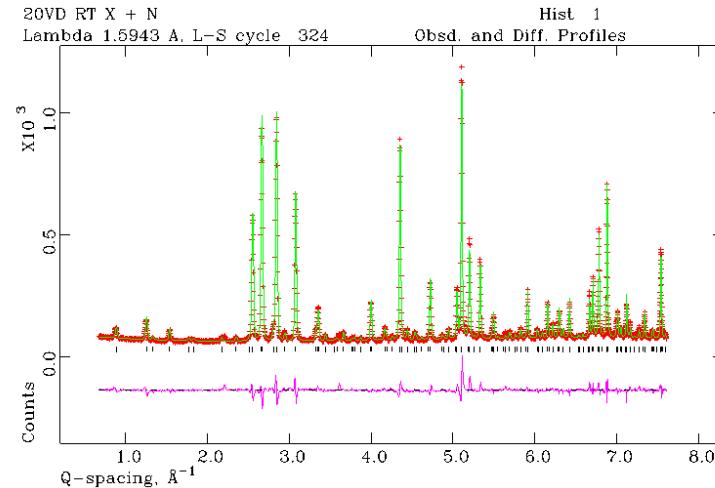
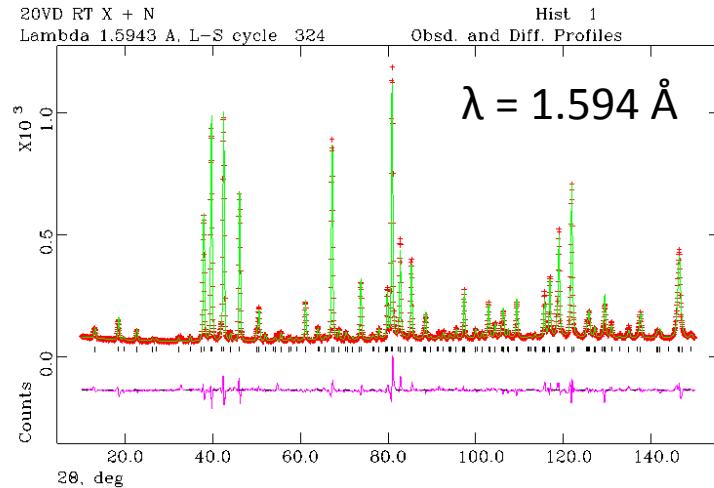
- Neutrons scatter primarily from the nucleus and form factor is almost Q-independent
  - Atom vibrations still reduce scattering at high Q
- The neutron can also interact with unpaired electrons to probe magnetism
  - Q-dependent form factor
  - Magnetic reflections are most intense at low Q



# Form factor, scattering power and complementarity of neutrons and X-rays



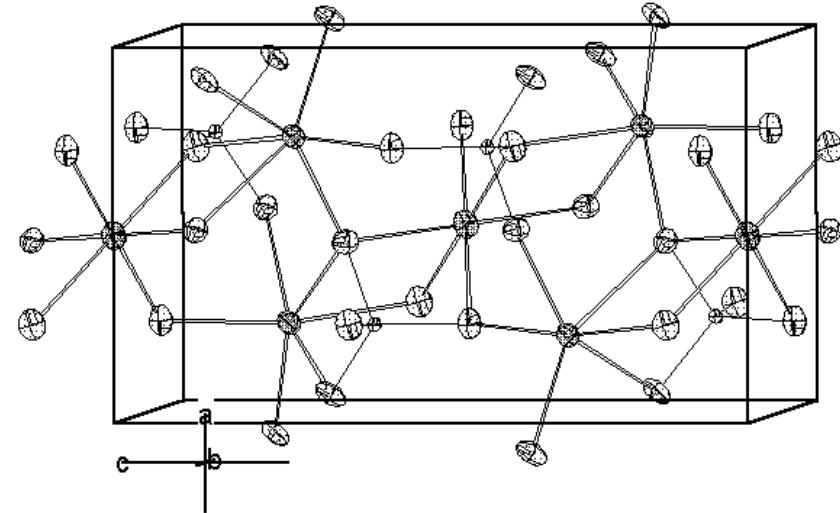
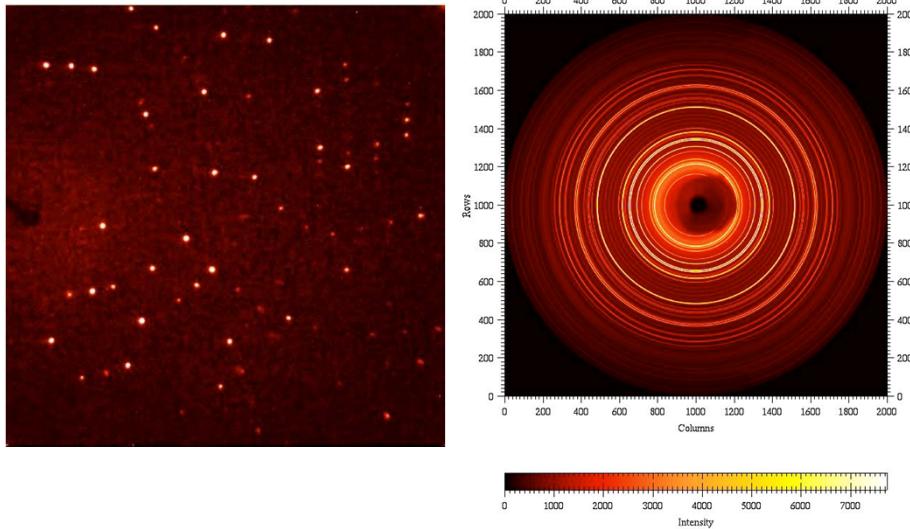
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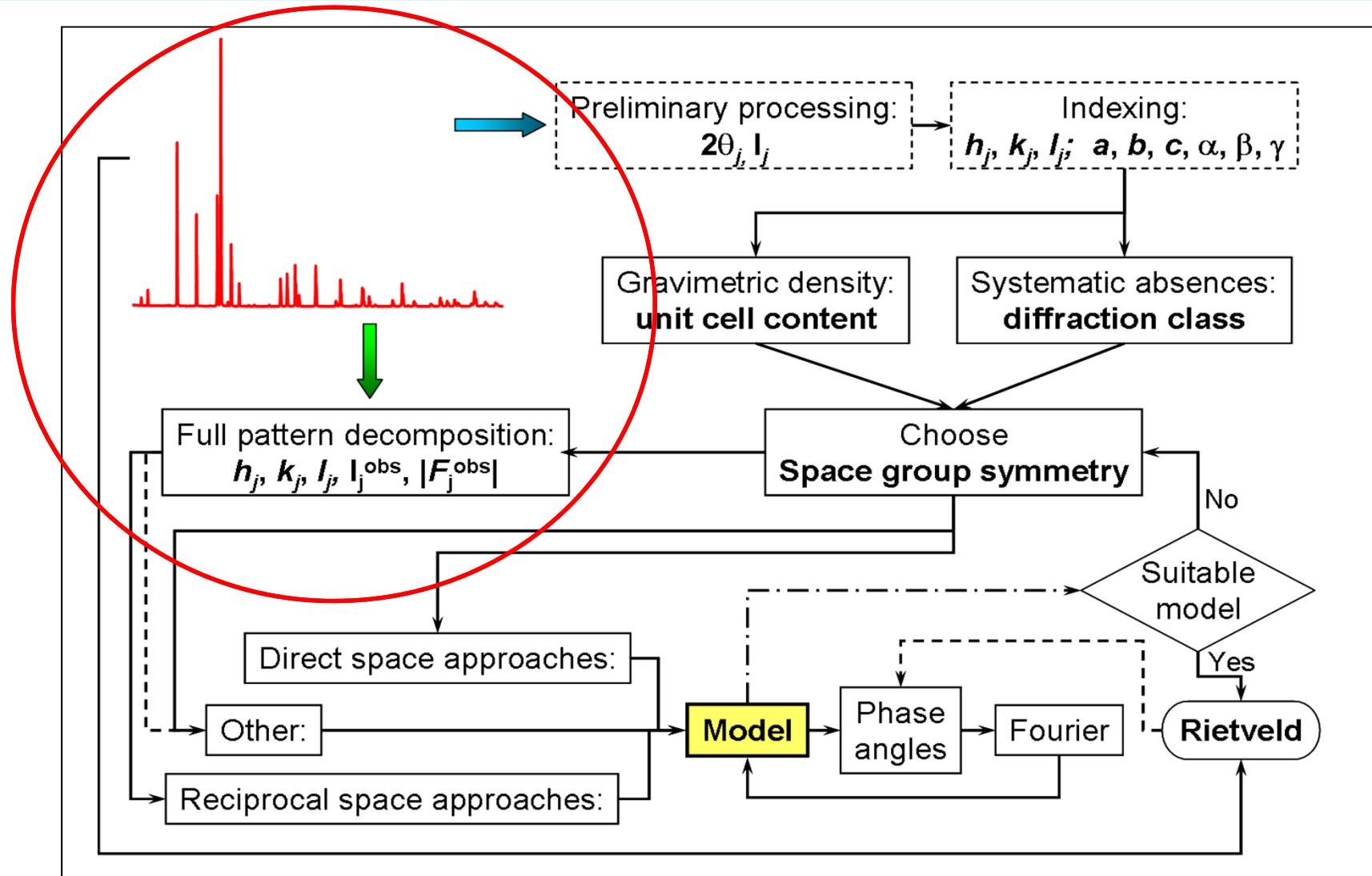
# Structure Solution/refinement



How to go from  
to this?



# Process for structure solution and refinement from powders using Bragg scattering



# Measured intensity and structure factor



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$$I_{hkl} \propto |F_{hkl}|^2$$

Measured intensity proportional to  $F_{hkl}^2$  and so we cannot tell whether  $F_{hkl}$  is positive or negative – the Phase problem

$$F_{hkl} \propto \sum f_i \exp[2\pi i(hx_i + ky_i + lz_i)] \exp(-U_i Q^2/2)$$

$f_i$  is the scattering power (form factor of the ith site i.e.  $(x_i, y_i, z_i)$  and includes fractional occupancy

Contribution of the ith site to the  $F_{hkl}$  in question

Atomic displacement of the ith atom site

# Centrosymmetry



*Since adding 1 to  $x_i, y_i$  or  $z_i$  does not change the structure factor it can be simplified to sum over the atoms of **one unit cell**.*

Also, since  $e^{i\phi} = i\sin\phi + \cos\phi$

$$F_{hkl} \propto \sum f_i i\sin[2\pi(hx_i + ky_i + lz_i)]\exp(-U_i Q^2/2) + \sum f_i \cos[2\pi(hx_i + ky_i + lz_i)]\exp(-U_i Q^2/2)$$

When an atom at  $x, y, z$  generates another atom by symmetry at  $-x, -y, -z$   
(centrosymmetric with a centre of symmetry at the origin)

We know that:

$$e^{i\phi} = i\sin\phi + \cos\phi$$

$$\cos(-\phi) = \cos\phi$$

$$\sin\phi = -\sin(-\phi)$$

This means  $e^{i\phi} + e^{-i\phi} = 2\cos\phi$

# Centrosymmetry continued



This allows the simplification of the structure factor to:

$$F_{hkl} \propto \sum f_i \cos[2\pi(hx_i + ky_i + lz_i)] \exp(-U_i Q^2/2)$$

*Where now the sum only includes one atom in each pair*

Systematic absences occur when other symmetry conditions are met. Reflections are only observed when:

- For body centering  $h+k+l=2n$
- For face centering  $h, k$  and  $l$  must all be odd or all be even
- Screw axes and glide planes give further conditions

These reduce the number of observed reflections in a diffraction pattern and is an integral part of choosing monochromator materials

See tutorial session after coffee break where you will prove this yourselves

# Structure solution/refinement



To unambiguously solve a structure the ratio of resolved and observed unique Bragg reflections to crystallographically independent atoms should be at least 10.

Crystal / powder requirements:

- Diffract out to beyond  $Q_{\max}$  of the instrument
- Be of adequate particle size
- Preferably not contain any local ordering

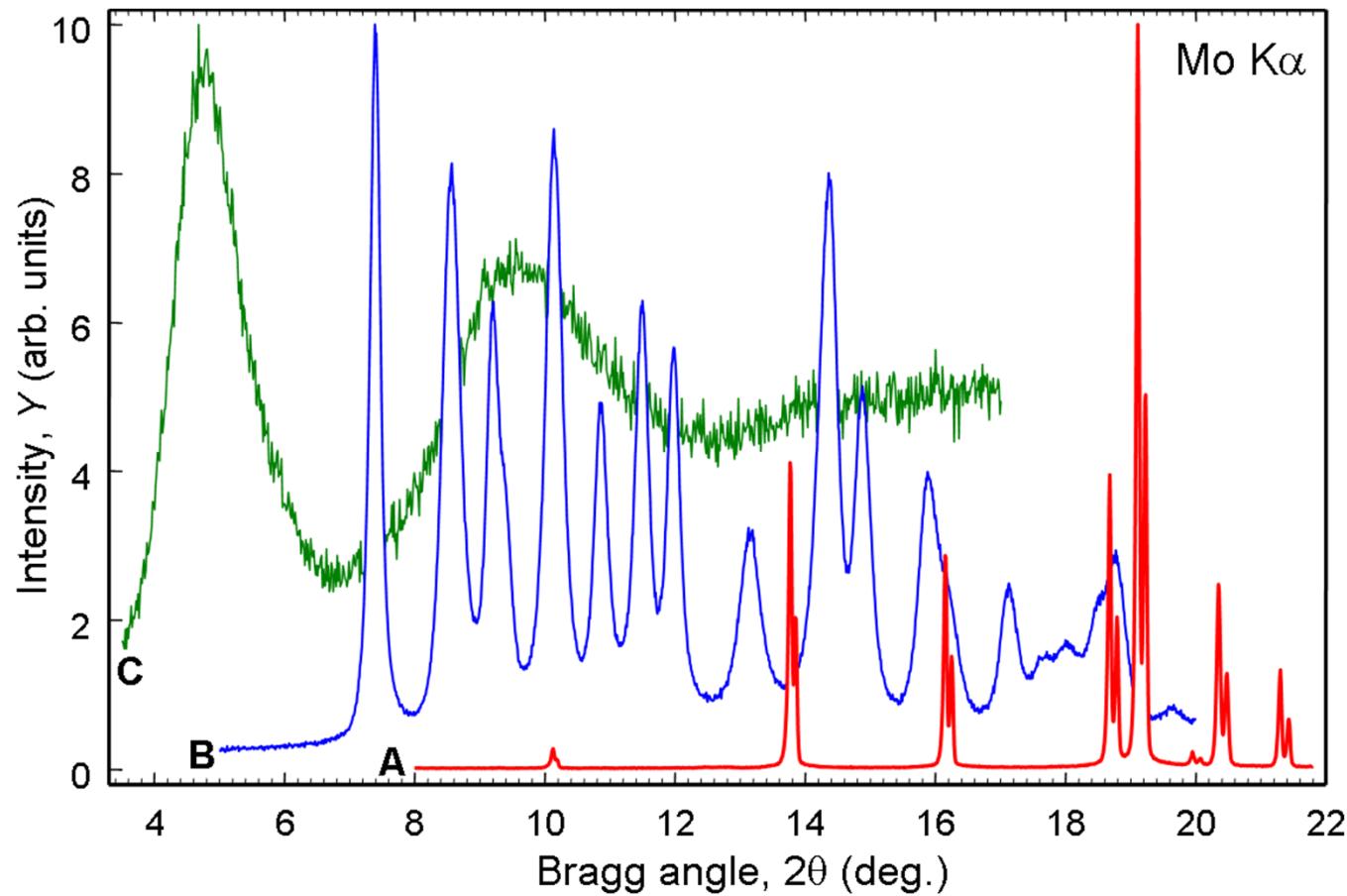
Instrument requirements:

- Access a  $Q_{\max}$  such that ratio of accessible Bragg reflections to crystallographically independent atoms is met
- Have a Q-resolution to resolve these Bragg reflections
- Be able to accurately measure the Bragg reflection intensity above the background

# Diffraction limit



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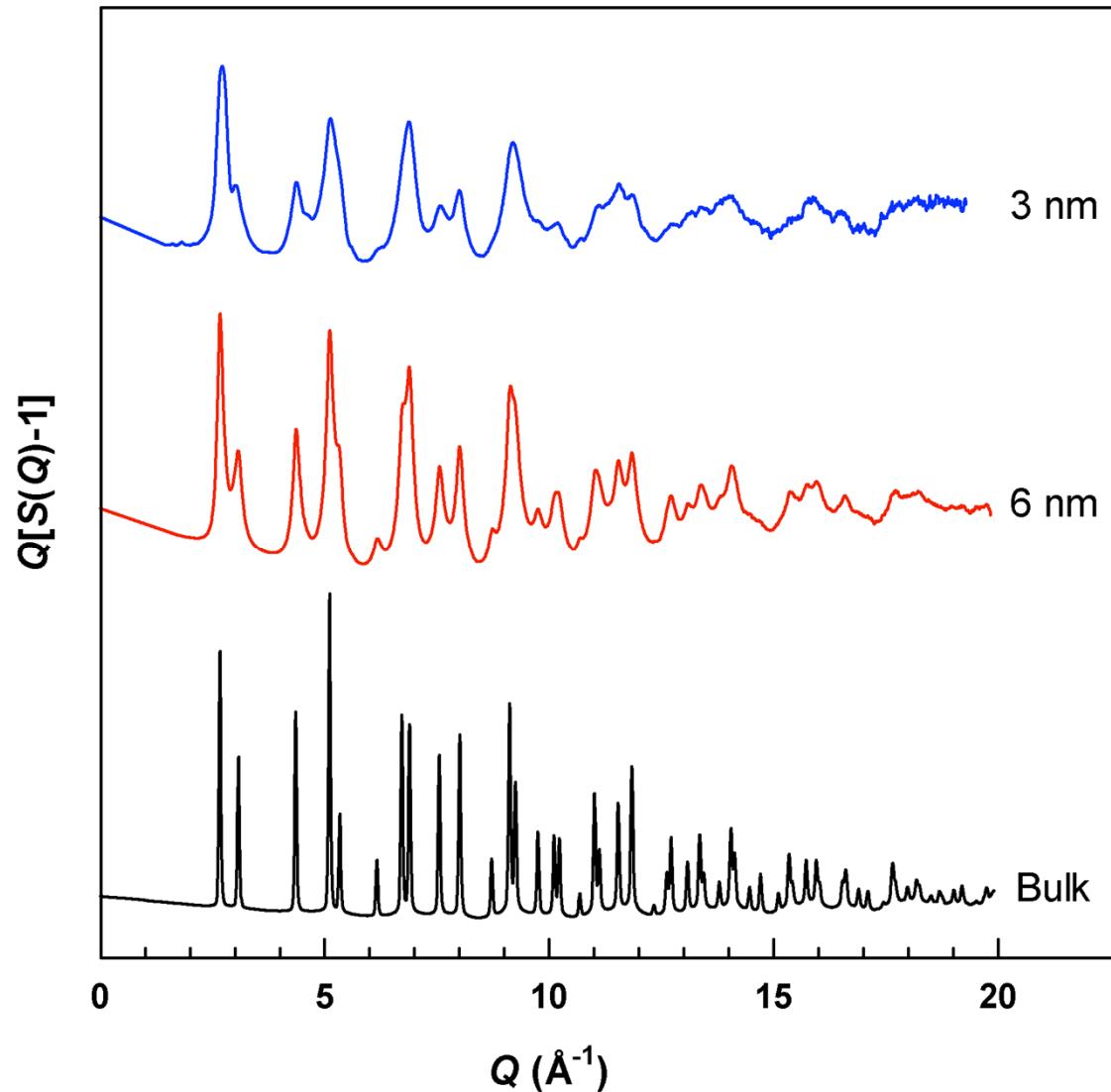


- A. Material with excellent crystallinity with low and nearly linear background
- B. Poorly crystalline material - causes for this can include small grain size, strained material, presence of an amorphous component, etc
- C. Non-crystalline material in the conventional sense - long-range order and periodicity are absent as no Bragg reflections. However, info on short range structure can be extracted

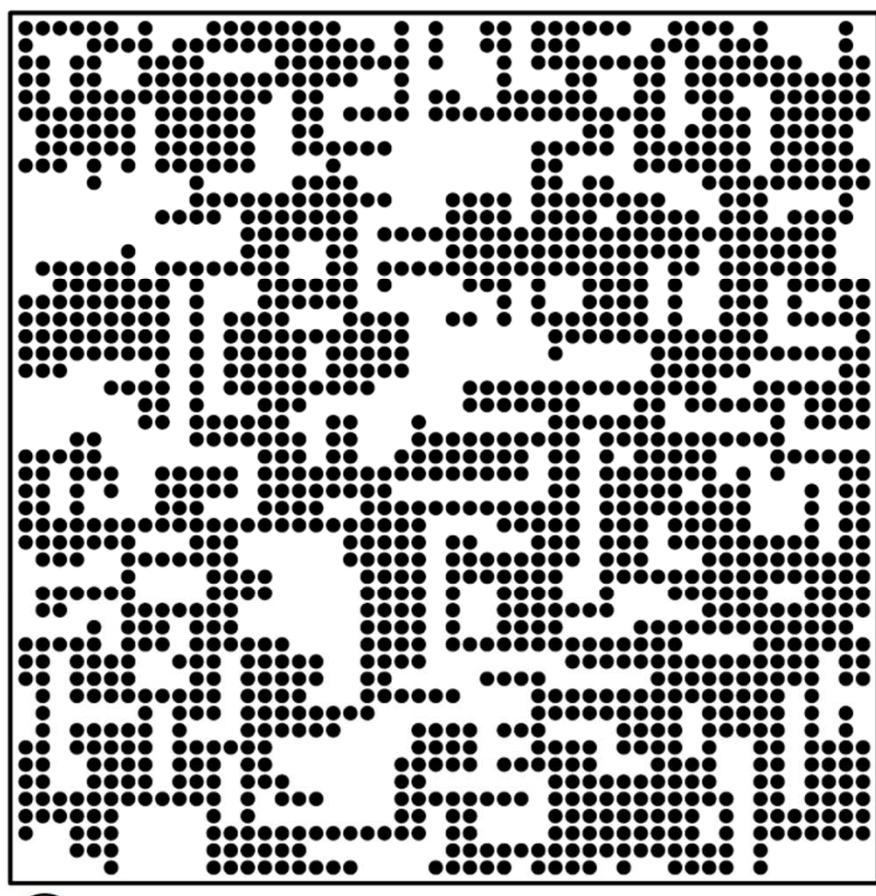
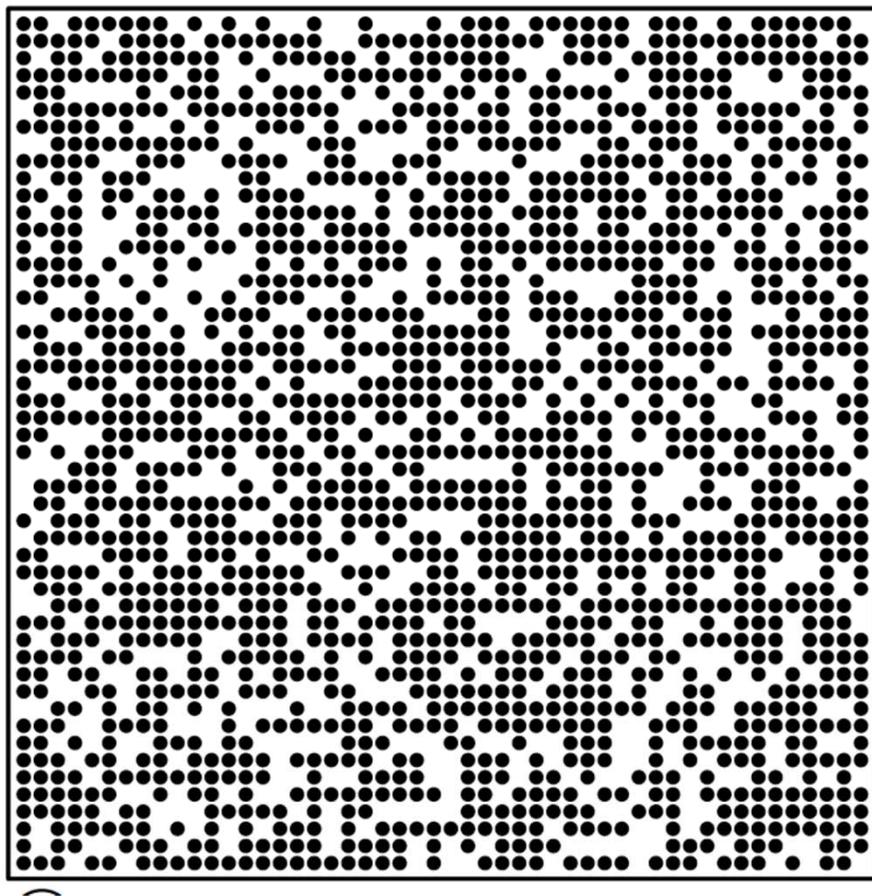
# Particle size effect



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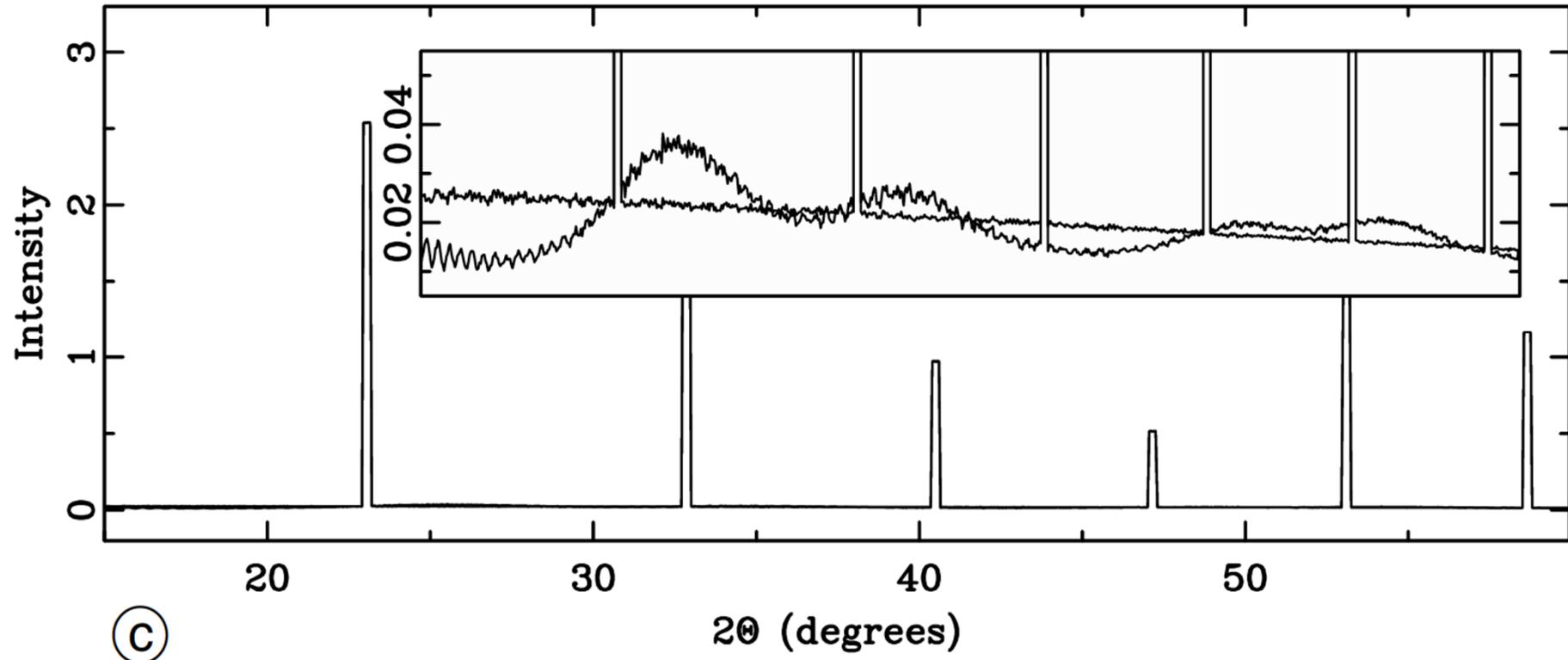


# Local Order



(reproduced from Proffen *et al.* (2003). *Z. Kristallogr.* **218**, 132-143)

# Local order

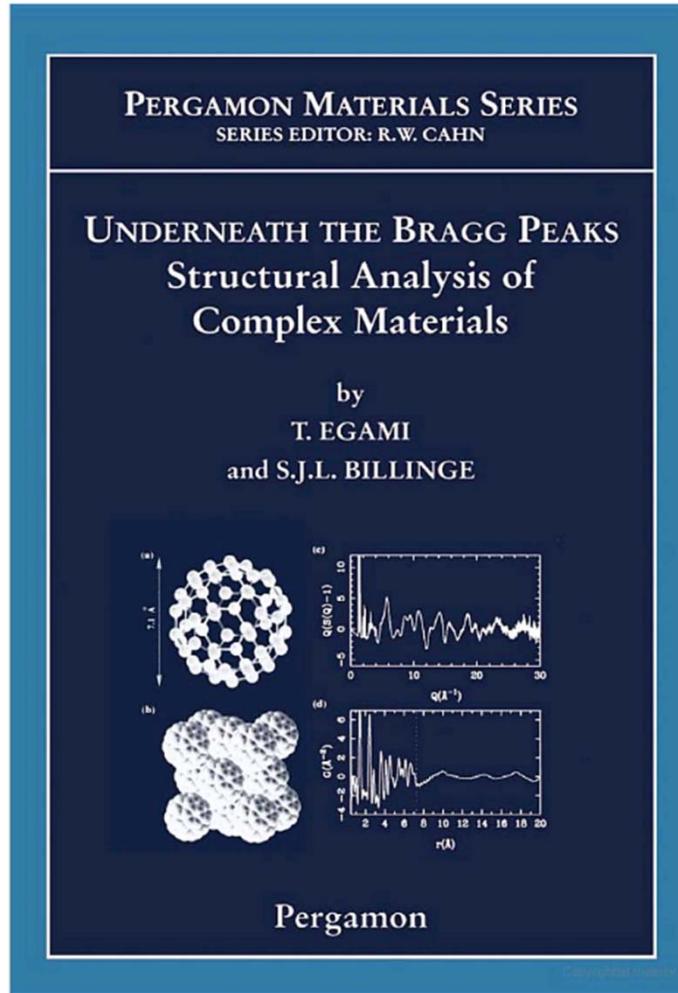


(c)

Diffuse scattering contributions appear between the Bragg reflections. This is ignored by the standard crystallographic approach, which only yields the long range average structure.

(reproduced from Proffen *et al.* (2003). *Z. Kristallogr.* **218**, 132-143)

# Pair distribution Function (PDF) analysis



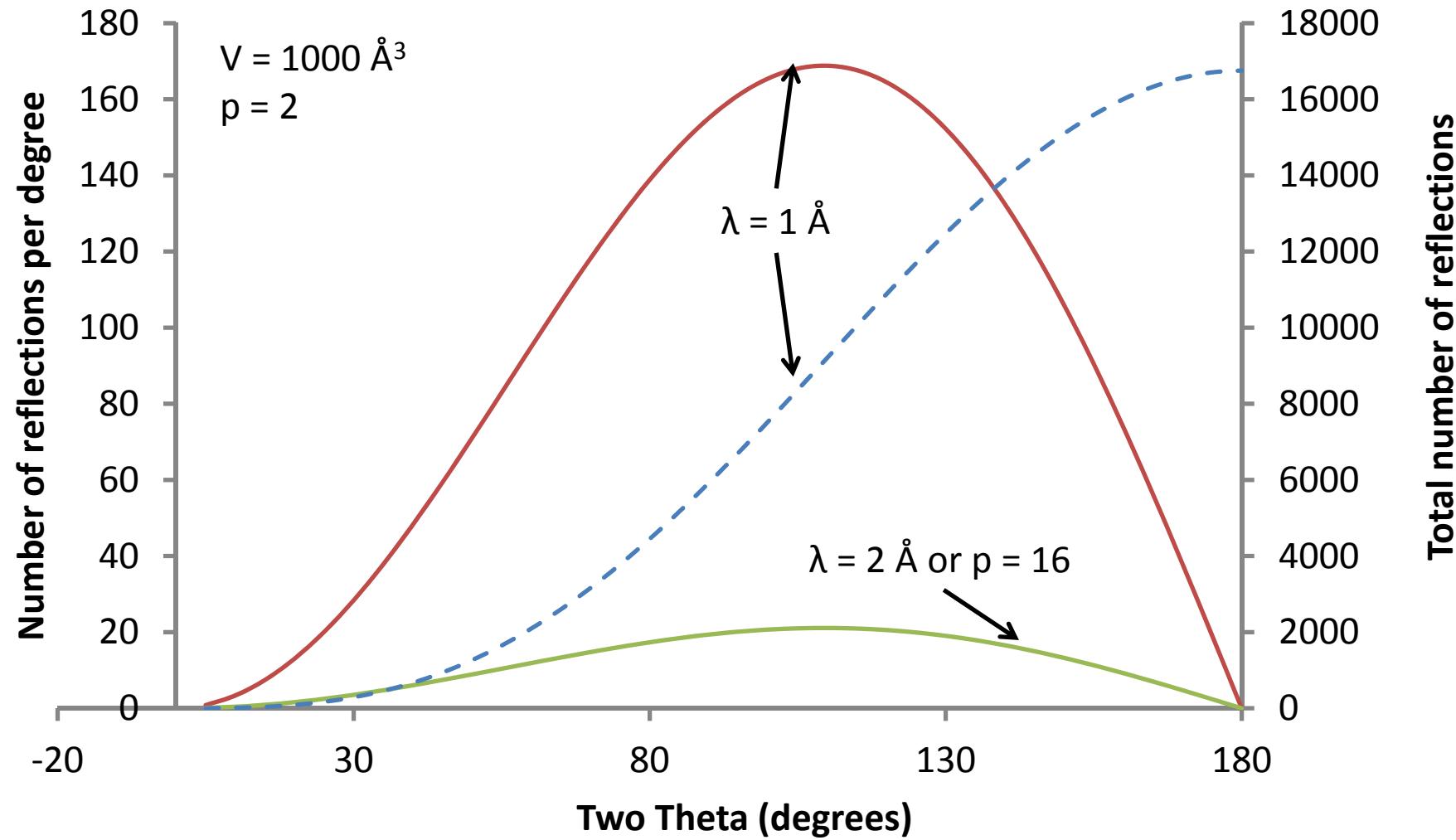
The PDF is obtained from the powder diffraction data via a sine Fourier transform of the normalized scattering intensity  $S(Q)$ :

$$\begin{aligned} G(r) &= 4\pi r[\rho(r) - \rho_0] \\ &= \frac{2}{\pi} \int_0^{\infty} Q[S(Q) - 1] \sin(Qr) dQ, \end{aligned} \quad (1)$$

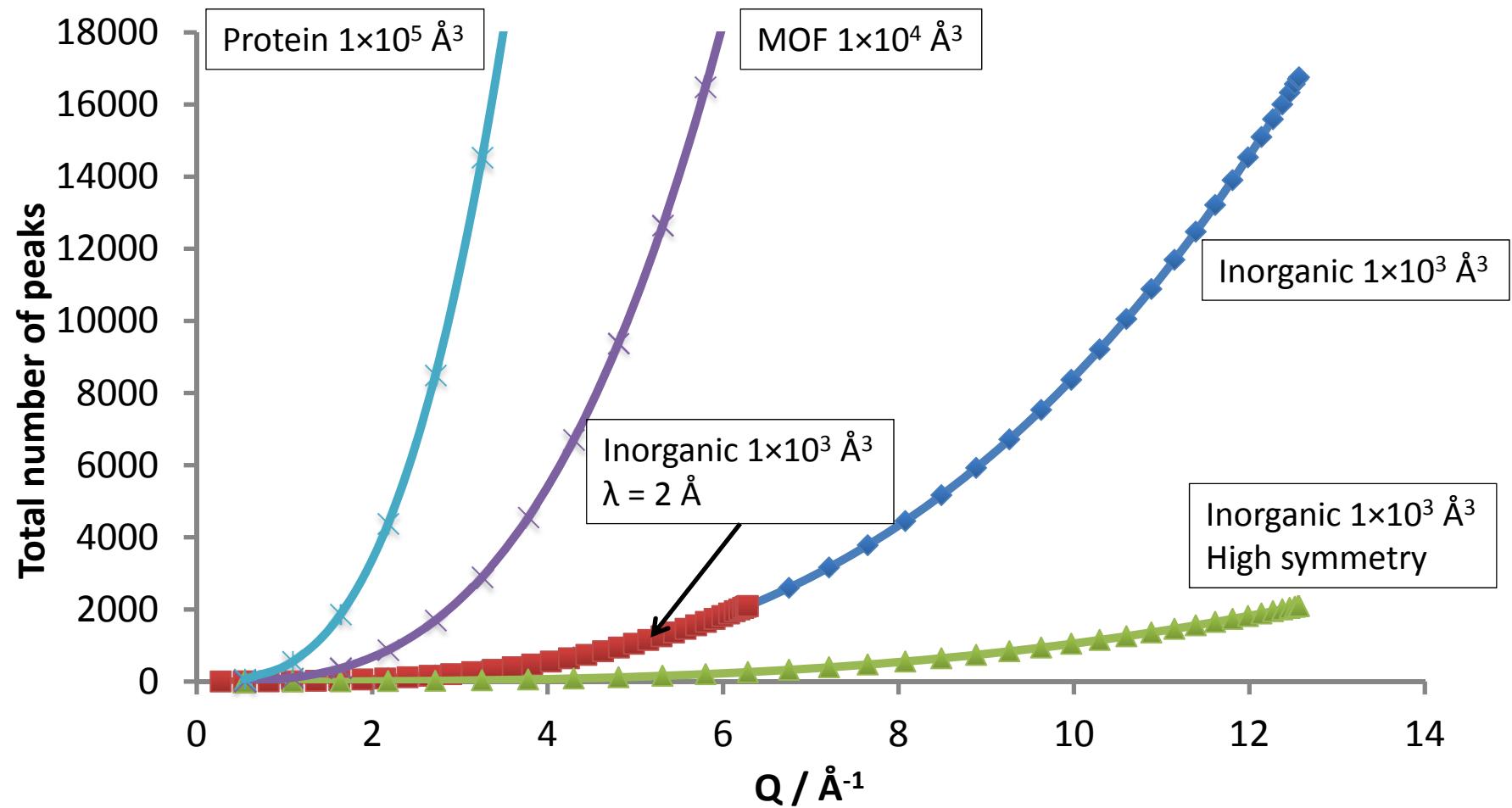
where  $\rho(r)$  is the microscopic pair density,  $\rho_0$  is the average number density and  $Q$  is the magnitude of the scattering vector. For elastic scattering  $Q = 4\pi \sin(\theta)/\lambda$  with  $2\theta$  being the scattering angle and  $\lambda$  the wavelength of the radiation used.

<http://www.totalscattering.org>

# The effect of wavelength and symmetry on number and density of allowed reflections



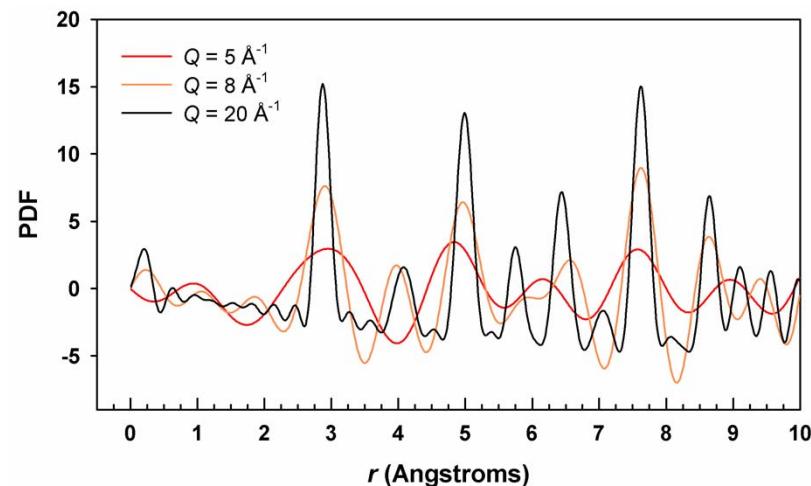
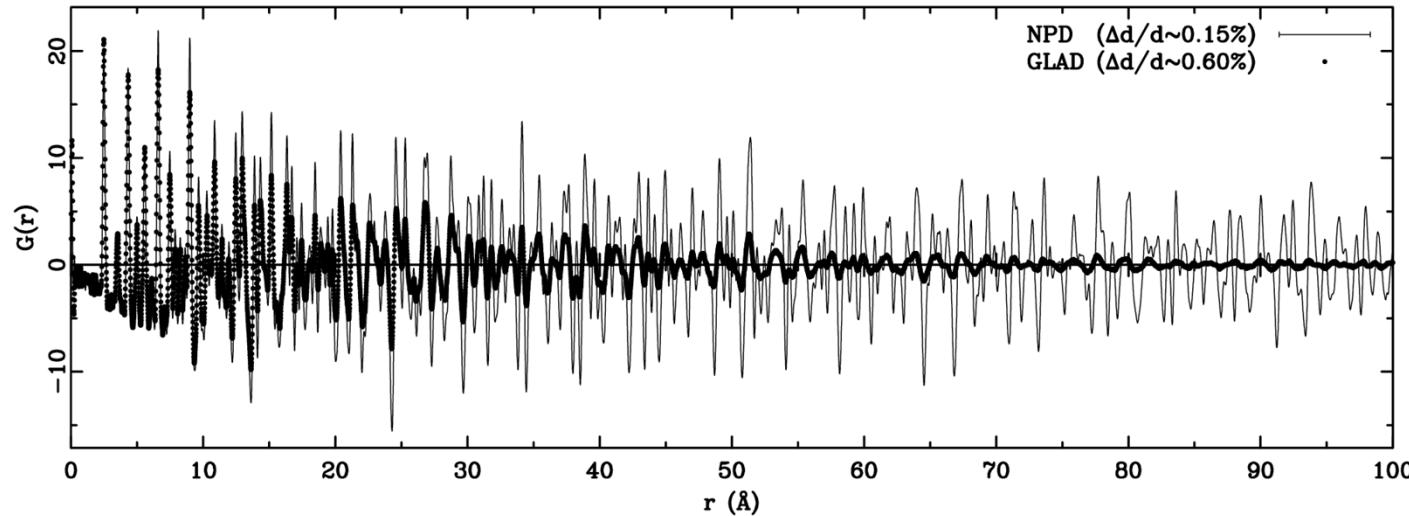
# Total Number of Reflections using 1 Å wavelength in reciprocal space



# PDF/Total scattering instrument requirements



(reproduced from Proffen  
*et al.* (2003). *Z. Kristallogr.*  
**218**, 132-143)



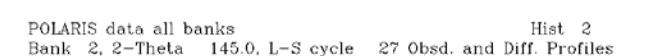
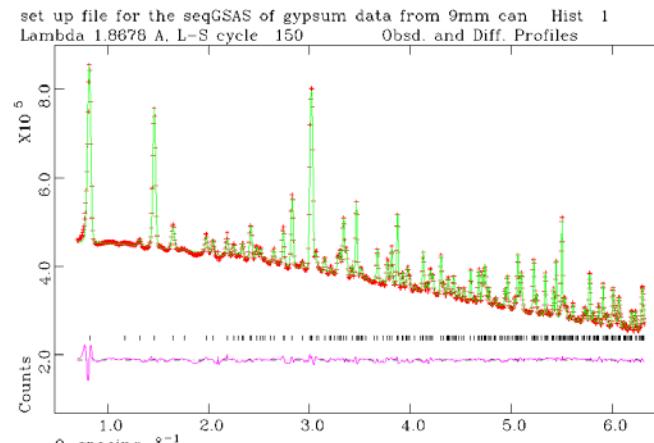
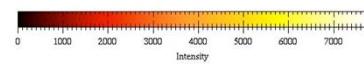
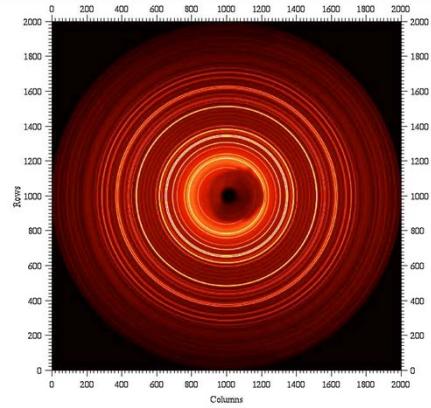
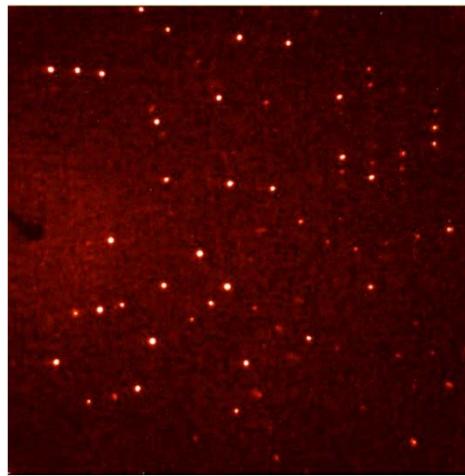
- Good  $\Delta d/d$  resolution at low  $d$  ( $\Delta Q/Q$  resolution at high  $Q$ )
- Access to as low  $d$  (high  $Q$ ) as possible

# Instrument choice



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- Single crystal or powder?
- Monochromatic or TOF?



# Single Crystal or Powder? Examples



Depends on the scientific problem:

- Unambiguous structure determination – single crystal
  - Beware extinction and absorption issues
- In situ studies – powders
  - Generally the only practical option
- Fast measurements – powders
  - Larger samples
- High background materials (such as incoherent scattering) – single crystal
  - BUT is possible with powder
- Multi-component systems investigations – powder
- Structural phase transitions – powder
  - Crystals tend to shatter
- Real systems – powders
- Very small samples – single crystal
  - Can become difficult to get a powder average

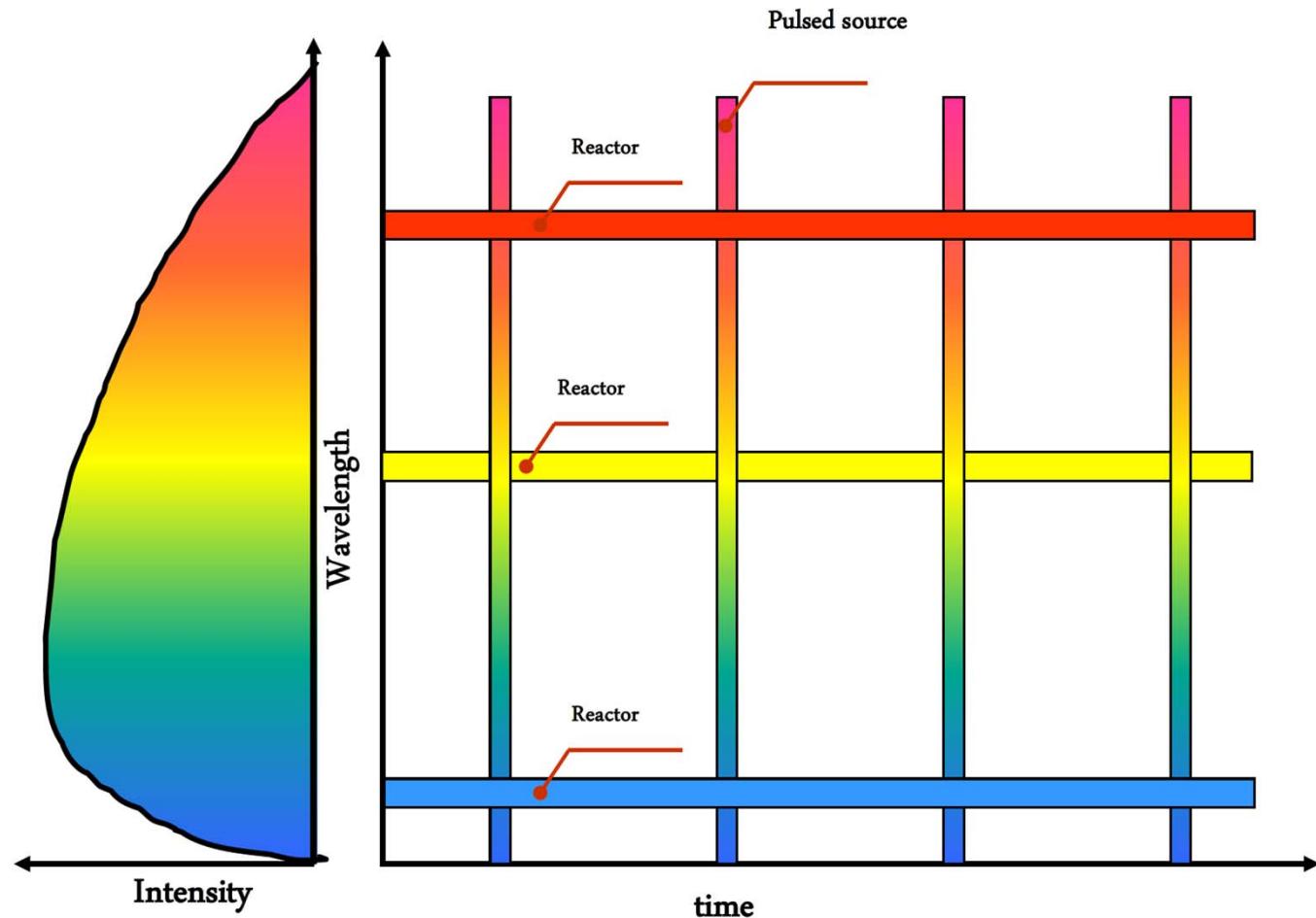
# Neutron Diffractometers: Monochromatic or time-of-flight?



$$\lambda = 2d\sin\theta$$

- Monochromatic
  - Fix wavelength and scan detector angle
  - Multiple  $2\theta$  required to cover  $Q(d)$  spacing range
  - $Q(d)$  spacing limit  $4\pi/\lambda$  ( $2\pi/d$ )
- TOF
  - Fix detector angle and scan wavelength
  - Single  $2\theta$  covers range of  $Q(d)$  space
  - $Q(d$  range) determined by  $\lambda_{\max}$ ,  $\lambda_{\min}$  and  $\theta$

# Monochromatic or time-of-flight? :Wavelength / energy selection



# Monochromatic or time-of-flight: Accessible Q(d) range



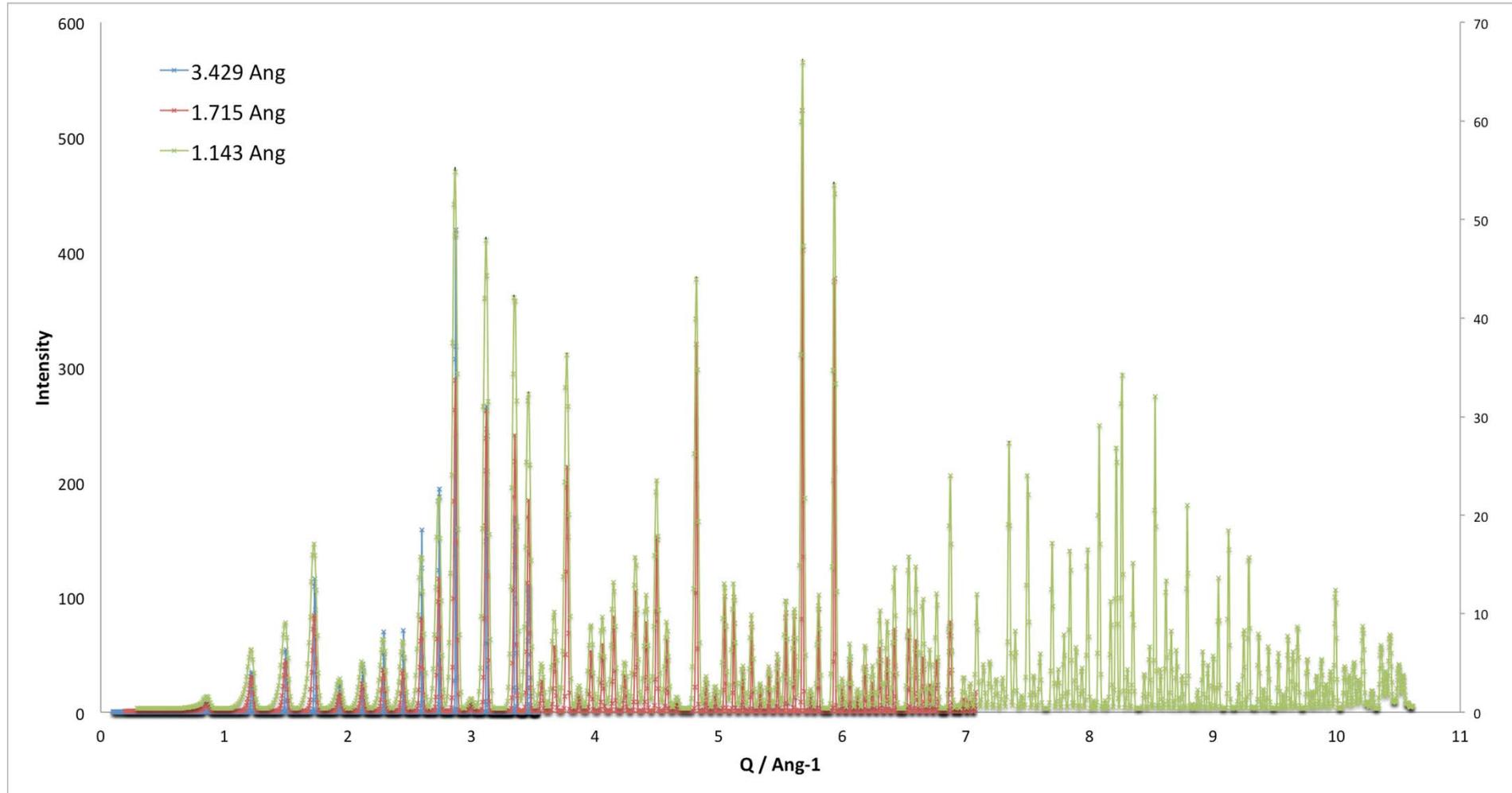
## Monochromatic

- For monochromatic instruments the  $Q_{\max}$  is  $4\pi/\lambda$  i.e. when  $\sin\theta = 1$ ,  $\theta = 90^\circ$ ,  $2\theta = 180^\circ$
- If a high  $Q_{\max}$  is required a shorter wavelength must be used.
- Shorter wavelengths are produced by higher order hkl planes
- Reflectivity is lower for shorter wavelengths
- Realistic  $Q_{\max}$  of around  $25 \text{ \AA}^{-1}$

## Time-of-flight

- $Q_{\max}$  depends on  $\lambda_{\min}$  and  $\theta$ .
- $\lambda_{\min}$  can be much lower than for the monochromatic case allowing  $Q_{\max} > 100 \text{ \AA}^{-1}$
- $\lambda_{\min}$  determined by the moderator, transport characteristics of the guide and which frame the instrument is working in

# Q coverage with different wavelengths



# Monochromatic or time-of-flight? :Resolution



Monochromatic

$$\frac{\Delta d}{d} = \frac{1}{2} \sqrt{U \cdot \cot^2(\theta) + V \cdot \cot(\theta) + W}$$

- U, V and W are functions of the collimation and U, V also takeoff angle to the monochromator
- Resolution minimum found near the takeoff angle of the monochromator  $2\theta_M$
- Higher takeoff angle gives higher resolution for identical wavelength
- Wavelength produced by monochromator is takeoff angle dependent for any particular hkl plane

Time-of-flight

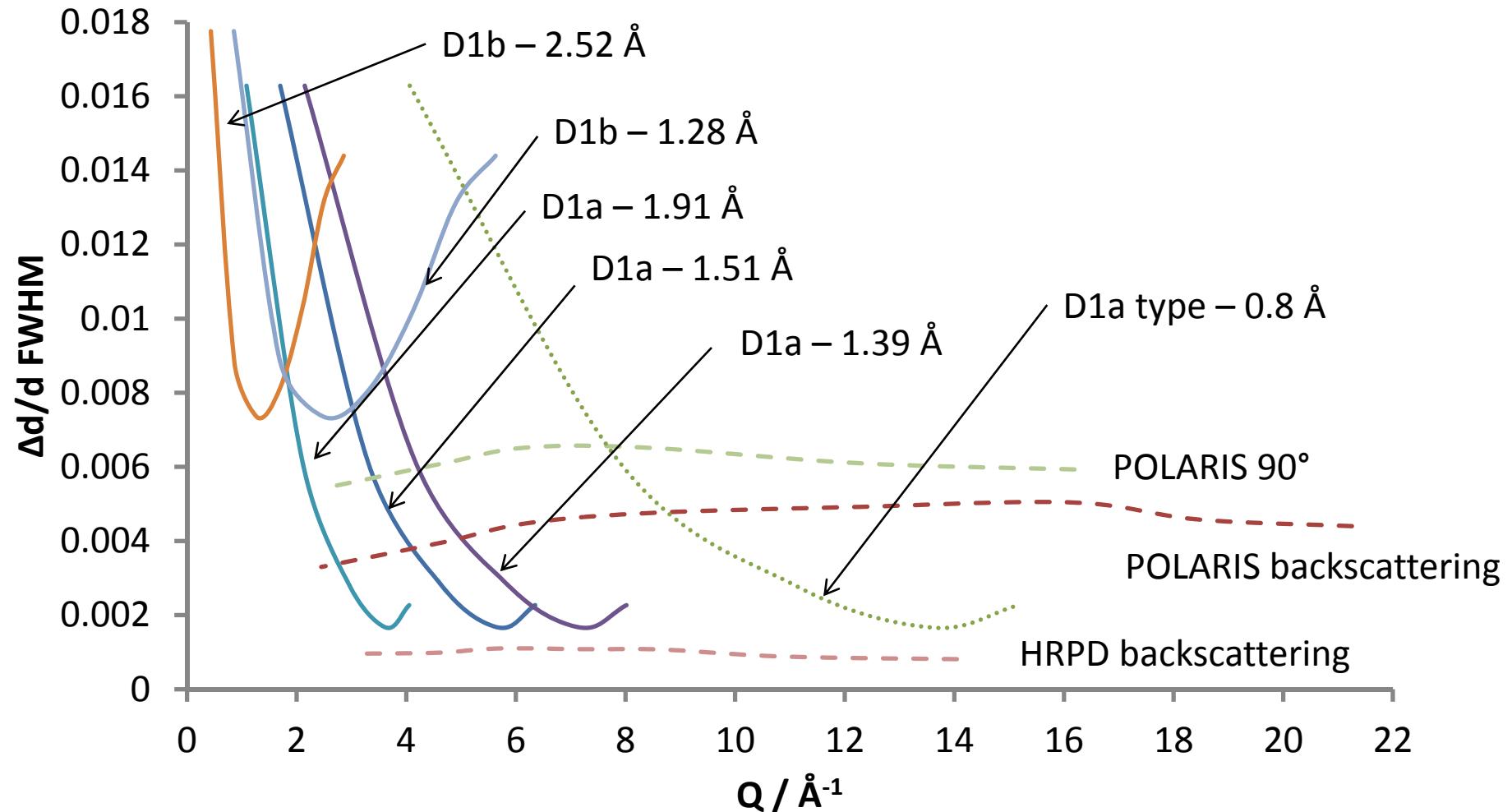
$$\frac{\Delta d}{d} = \left[ \Delta\theta^2 \cot^2 \theta + \left( \frac{\Delta t}{t} \right)^2 + \left( \frac{\Delta L}{L} \right)^2 \right]^{\frac{1}{2}}$$

- $\Delta\theta$  is the angular uncertainty
- The main component of  $\Delta t$  is the moderation time of the neutron
- $\Delta L$  is the flight path uncertainty of the neutron mainly due to the finite width of the moderator
- First term can be minimised by moving to higher scattering angle
- Second and third terms minimised by increasing instrument length

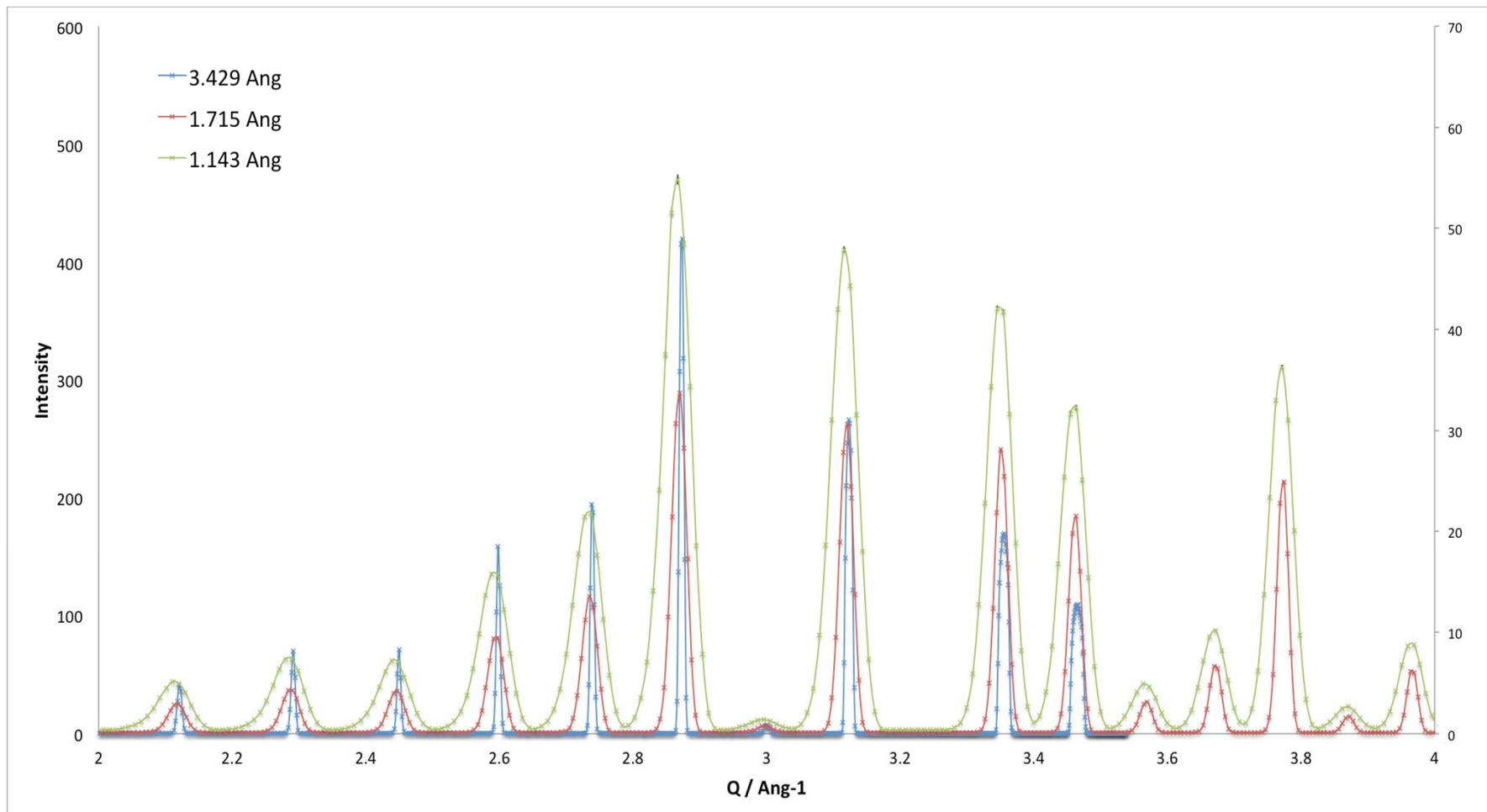
# Resolution functions



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# Q Resolution with different wavelengths

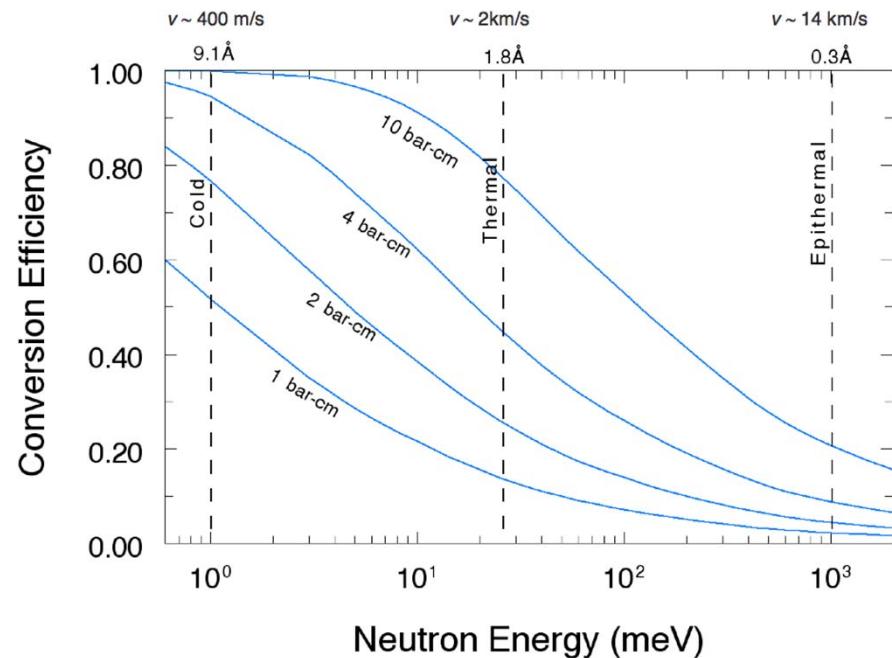


# Monochromatic or time-of-flight? Resolution



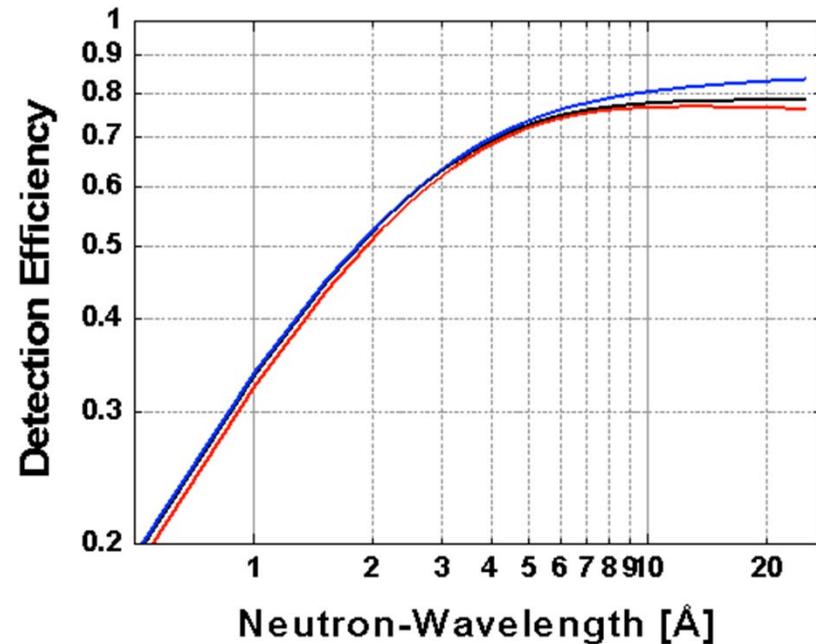
- Monochromatic
  - Simple, symmetric peakshape function
  - Resolution where it is needed
  - Best resolution where diffraction peak density is highest (see slides 62 and 52, which show minimum in resolution function around  $120^\circ 2\theta$ )
  - Different wavelength can be used to give resolution in Q-space where required
  - Different takeoff angle can be used to change resolution function
- Time-of-flight
  - Complex asymmetric peakshape related to moderator characteristics
  - Resolution almost constant for a given detector bank so increasing peak density with Q can be an issue
  - Resolution improved by moving to higher scattering angle detector bank

# Detection Efficiency



${}^3\text{He}$  detection efficiency as a function of detection depth. (from Radeka, Neutrons & photon detector workshop, 2012)

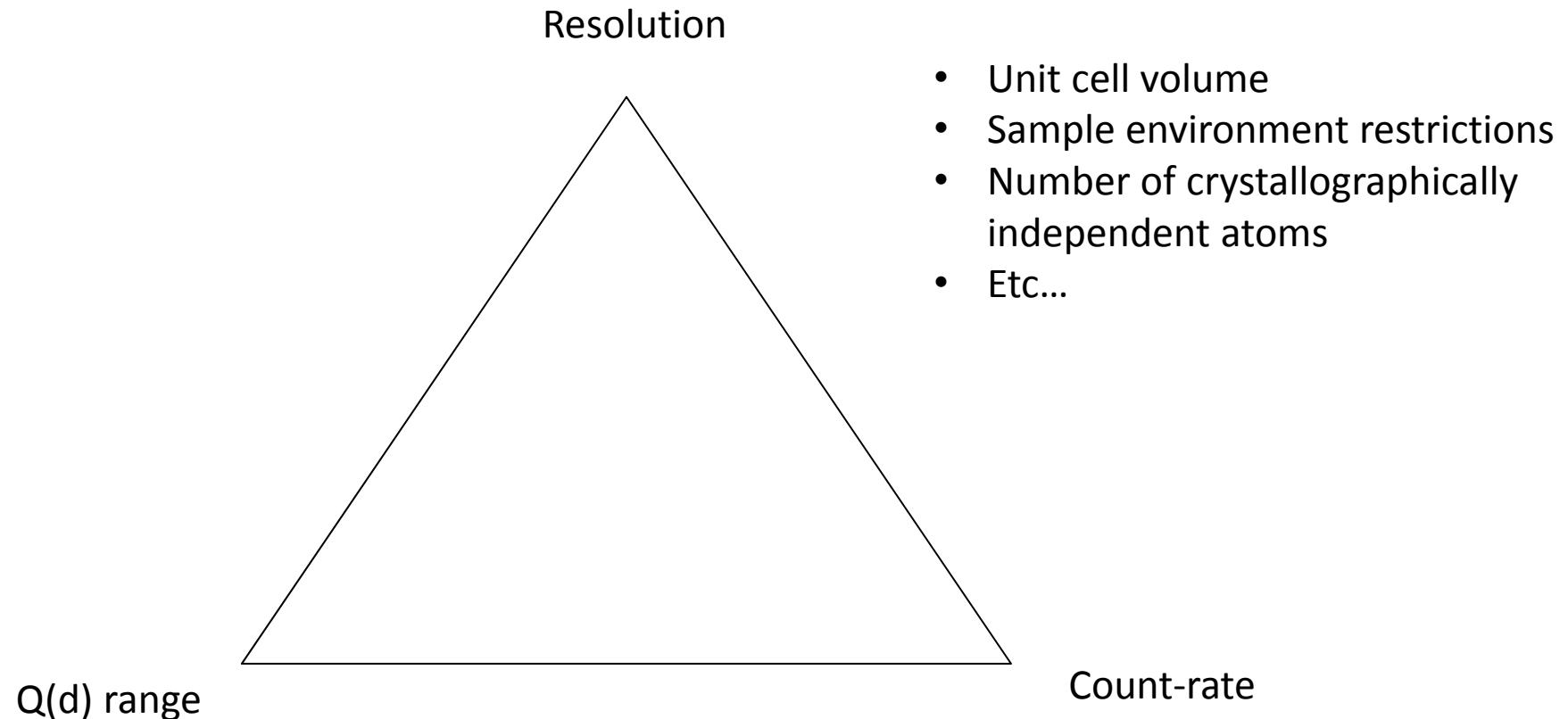
[https://portal.slac.stanford.edu/sites/conf\\_public/nxd2012/presentations/VR\\_Neutron%20gas%20dets\\_Aug1\\_2012.pdf](https://portal.slac.stanford.edu/sites/conf_public/nxd2012/presentations/VR_Neutron%20gas%20dets_Aug1_2012.pdf)



Predicted detector efficiency  
CASCADE-detector for 20  ${}^{10}\text{B}$  layers

<http://www.physi.uni-heidelberg.de/Forschung/ANP/Cascade/Projekt/results.php?lang=en>

# Why so many diffractometers?



# Examples of Neutron Diffractometer

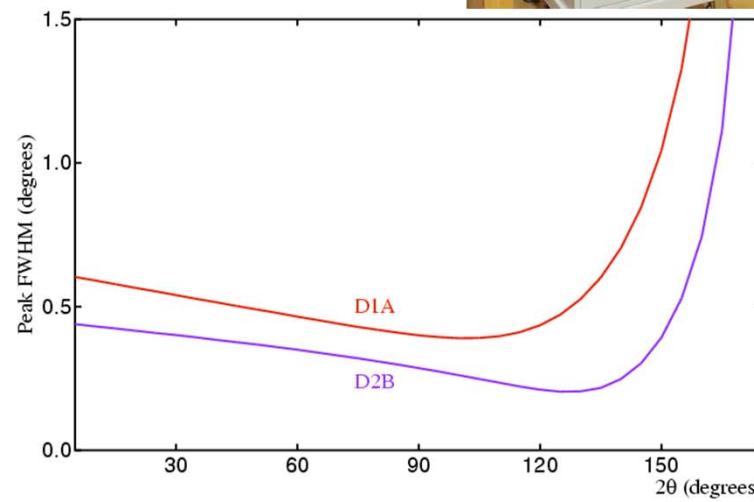
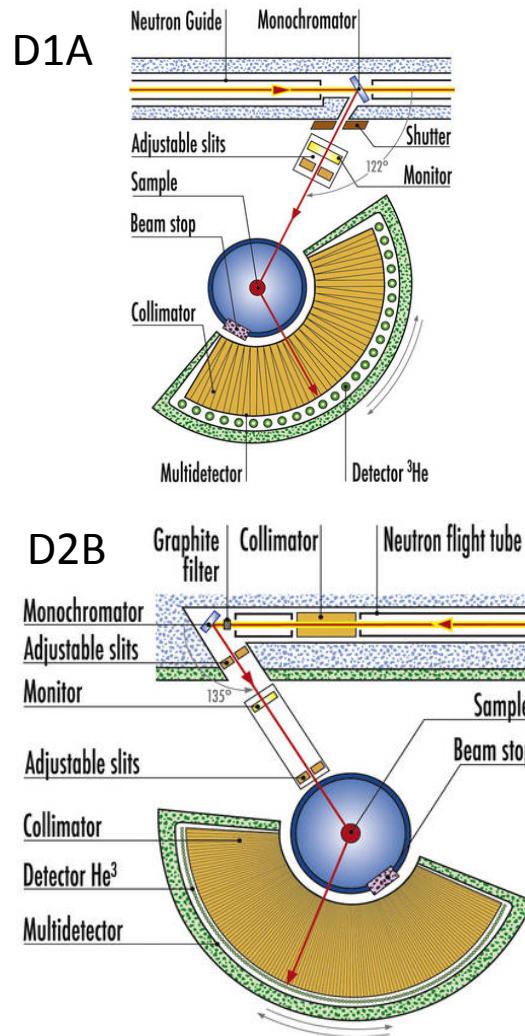


- Earliest diffractometers
- Continuous wavelength powder
  - High resolution powder
  - High flux powder
- Time-of-flight powder
  - High resolution powder
  - High flux powder
- Single crystal diffractometers

# Evolution of Instruments: First monochromatic neutron instruments



# Continuous wavelength, high resolution powder – D1A and D2B at ILL



# Continuous wavelength, high resolution powder – D1A and D2B at ILL



Instrument	D1A	D2B
Takeoff angle / °	122	135
Flux / n cm <sup>-2</sup> s <sup>-1</sup>	$10^6$	$10^6$ to $10^7$
Beam (h × w) / mm	$30 \times 20$	$50 \times 20$
Detectors	$25 \text{ } ^3\text{He} \times 10 \text{ cm h}$	$128 \text{ } ^3\text{He} \times 30 \text{ cm h}$
Wavelengths	Ge(hhl)	Ge(hhl)
Δd/d Resolution	$2-3 \times 10^{-3}$	Min $5 \times 10^{-4}$
Background	Very Low (60 m)	Low (15 m)
Average data collection time	3-24 hrs	0.25-4 hrs

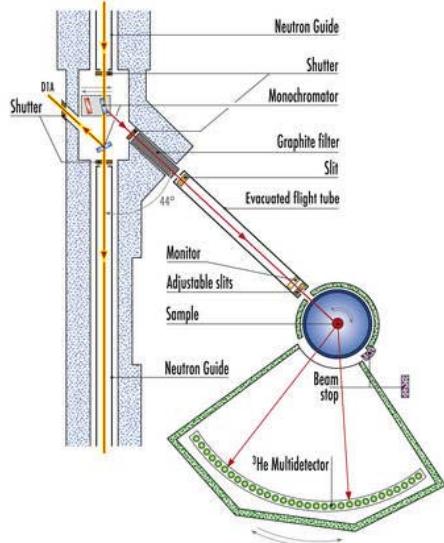
Similar instruments at all continuous sources:

Echidna (ANSTO), Spodi (FRM-II), BT-1 (NIST), 3T2 (LLB), HB-2A (HFIR) etc...

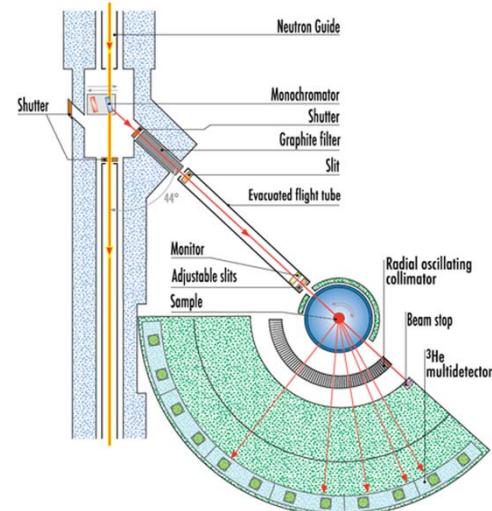
# Continuous wavelength, high flux powder – D1B and D20 at ILL



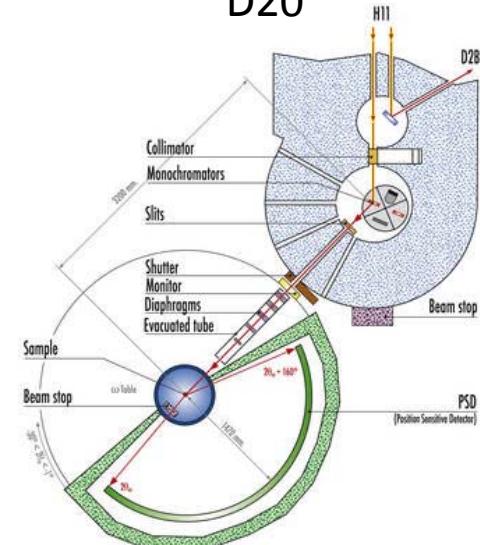
D1B



newD1B



D20



# Continuous wavelength, high flux powder – D1B and D20 at ILL



<b>Instrument</b>	D1B (old) / D1B (new)	D20
<b>Takeoff angle / °</b>	44	28, 42 ( $\pm 2$ )
<b>Flux / <math>n\text{ cm}^{-2}\text{ s}^{-1}</math></b>	$6.5 \times 10^6$ HOPG(002) $0.4 \times 10^6$ Ge(311)	$4.2 \times 10^7$ HOPG(002) $9.8 \times 10^7$ Cu(200) 42° $3.2 \times 10^7$ Cu(200) 28°
<b>Beam (h × w) / mm</b>	50 × 20	50 × 20
<b>Detectors</b>	80° multi-wire / 128° multi-wire 0.2° separation / 0.1° separation 400 channels / 1280 channels	153.6° micro-strip detector 0.1° separation 1536 channels
<b>Wavelengths / Å</b>	2.52, 1.28	2.42, 1.30, 0.87
<b>Δd/d Resolution</b>	$> 1 \times 10^{-2}$	$> 1 \times 10^{-2}$
<b>Background</b>	Medium (low with ROC)	Medium/High (low with ROC)
<b>Average data collection time</b>	5-10 mins / 1-5 mins	<1 min

Fewer comparable instruments: Wombat (ANSTO), G4.1 (LLB), HB-2C (HFIR)

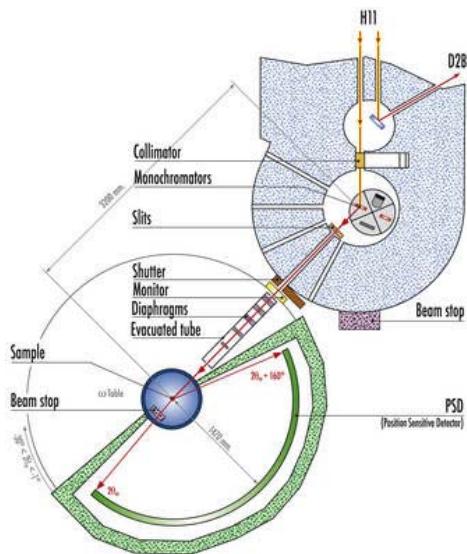
# Continuous wavelength, variable resolution powder – D20 at ILL



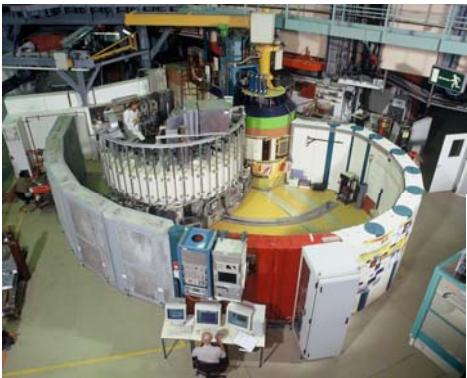
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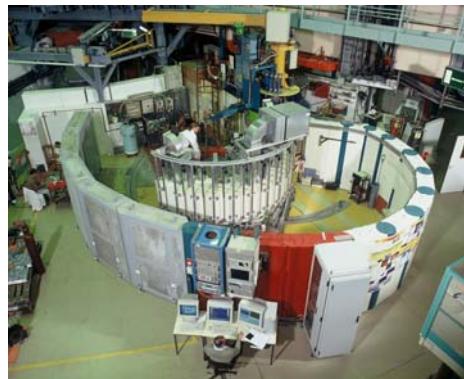
120°



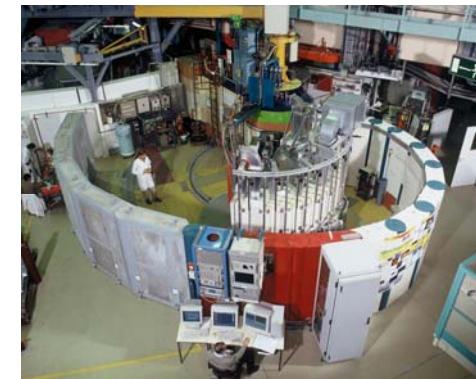
28°



90°



65°



42°

Photos courtesy T. Hansen ILL

# Continuous wavelength, General Purpose powder – D20 at ILL



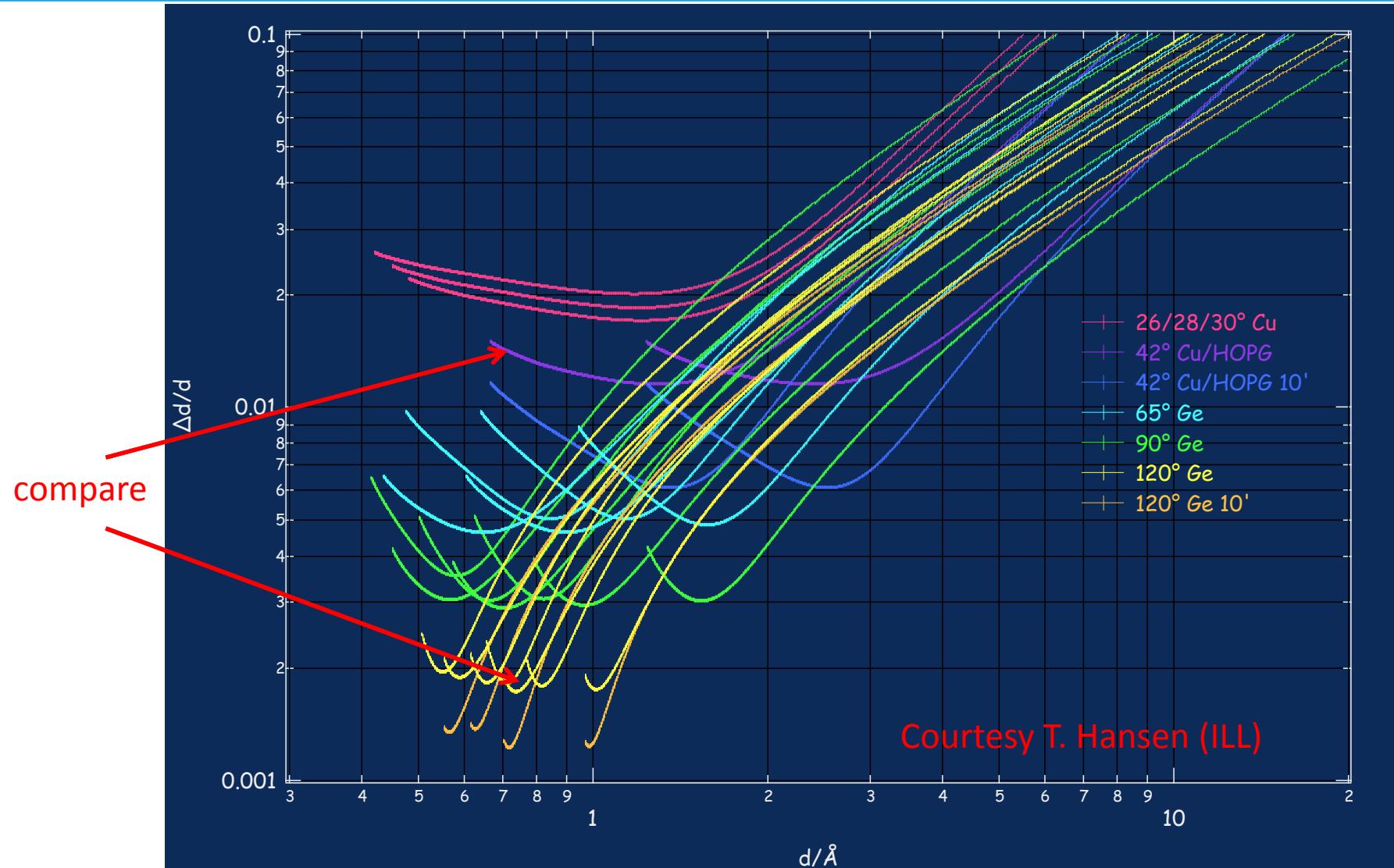
Instrument	D20 (high flux)	D20 (high takeoff angle)
Takeoff angle / °	28, 42 ( $\pm 2$ )	65, 90, 120 ( $\pm 2$ )
Flux / $n\text{ cm}^{-2}\text{ s}^{-1}$	$4.2 \times 10^7$ HOPG(002) $9.8 \times 10^7$ Cu(200) 42° $3.2 \times 10^7$ Cu(200) 28°	$8.0 \times 10^6$ Ge(115) $7.5 \times 10^6$ Ge(117) $4.0 \times 10^6$ Ge(119)
Beam (h × w) / mm	50 × 20	50 × 20
Detectors	153.6° micro-strip detector 0.1° separation 1536 channels	153.6° micro-strip detector 0.1° separation 1536 channels
Wavelengths / Å	2.42, 1.30, 0.87	variable 0.8-3 Ge(hhl/00l/hhh)
Δd/d Resolution	$> 1 \times 10^{-2}$	See next slide
Background	Medium/High (low with ROC)	Medium/High (low with ROC)
Average data collection time	<1 min	5-15 mins (30 times faster than similar counting statistics on D2B)

Even fewer contemporary instruments: HRPT (PSI), Wombat (ANSTO has potential)

# Resolution as a function of $\theta_B$



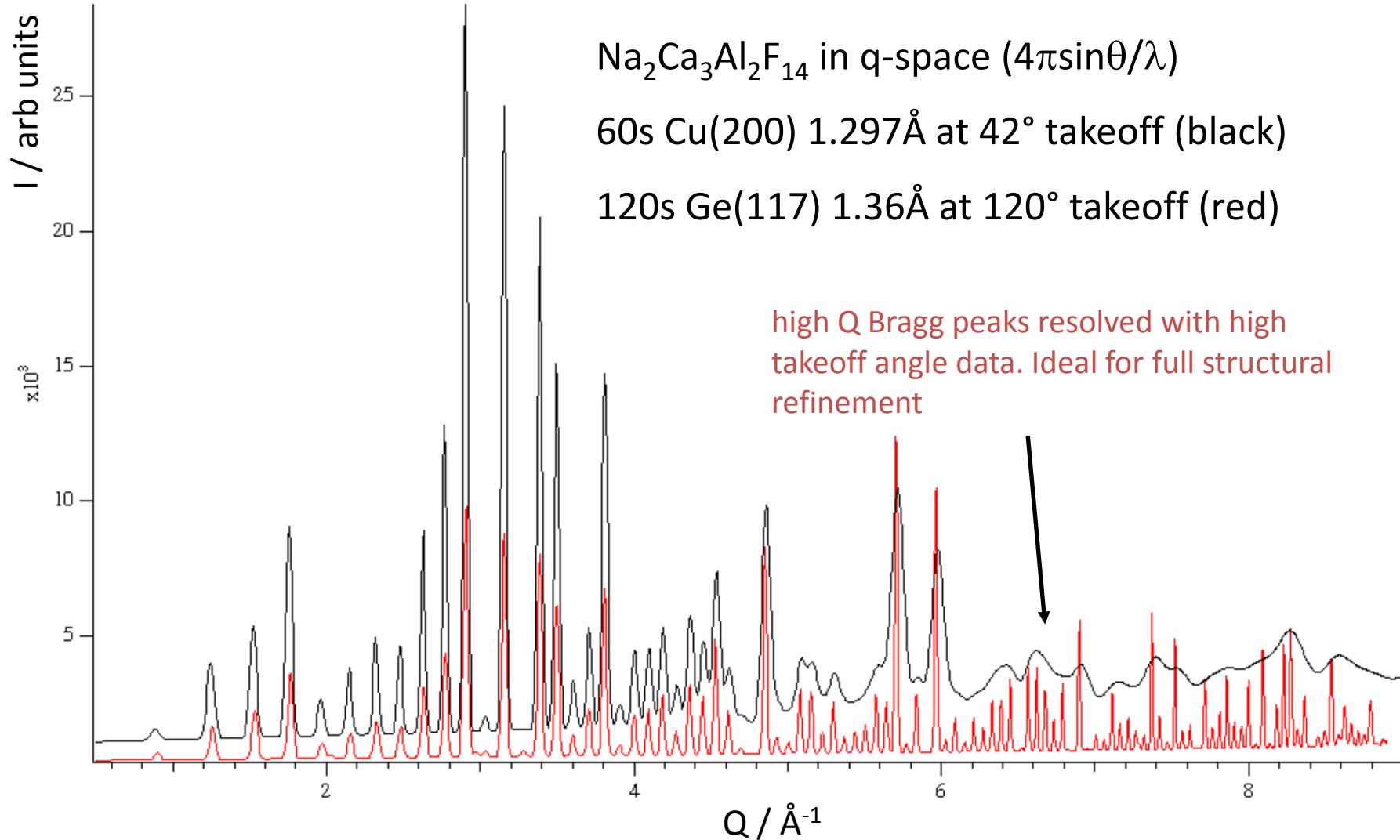
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# High flux v high takeoff-angle



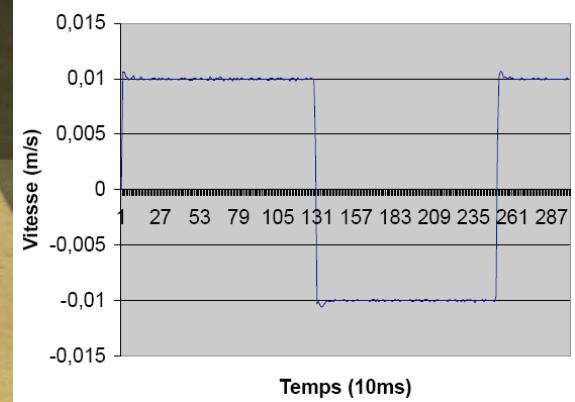
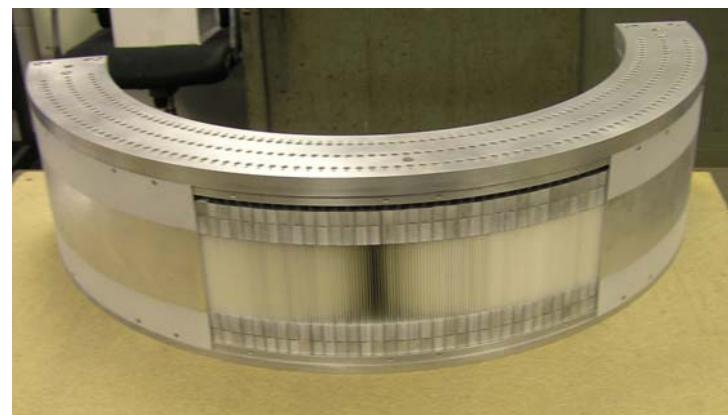
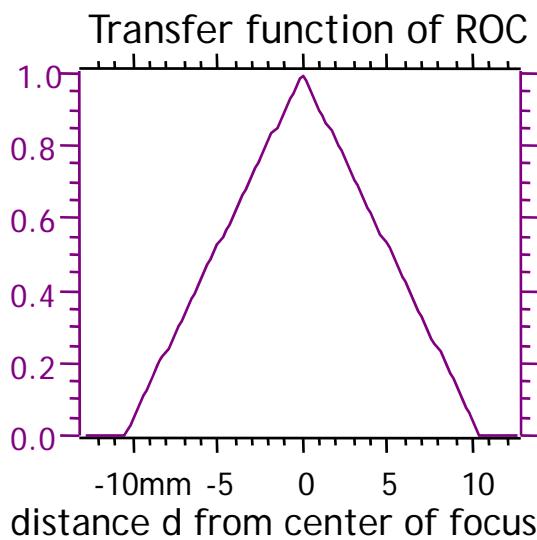
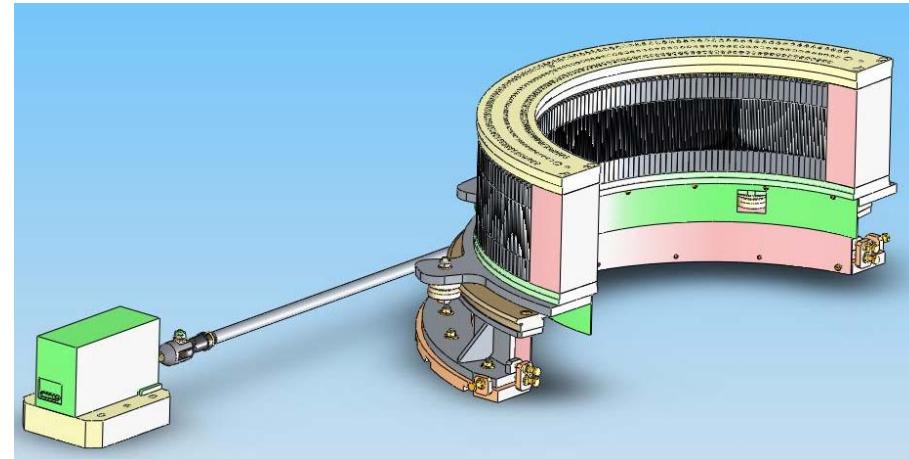
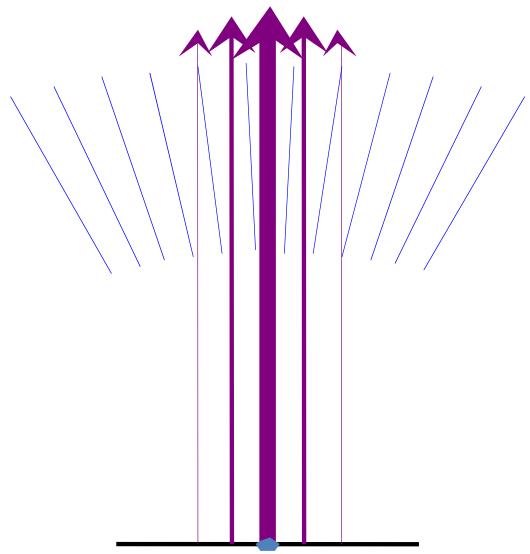
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# Parasitic Scattering with high flux instruments: Radial Oscillating Collimators (ROC)

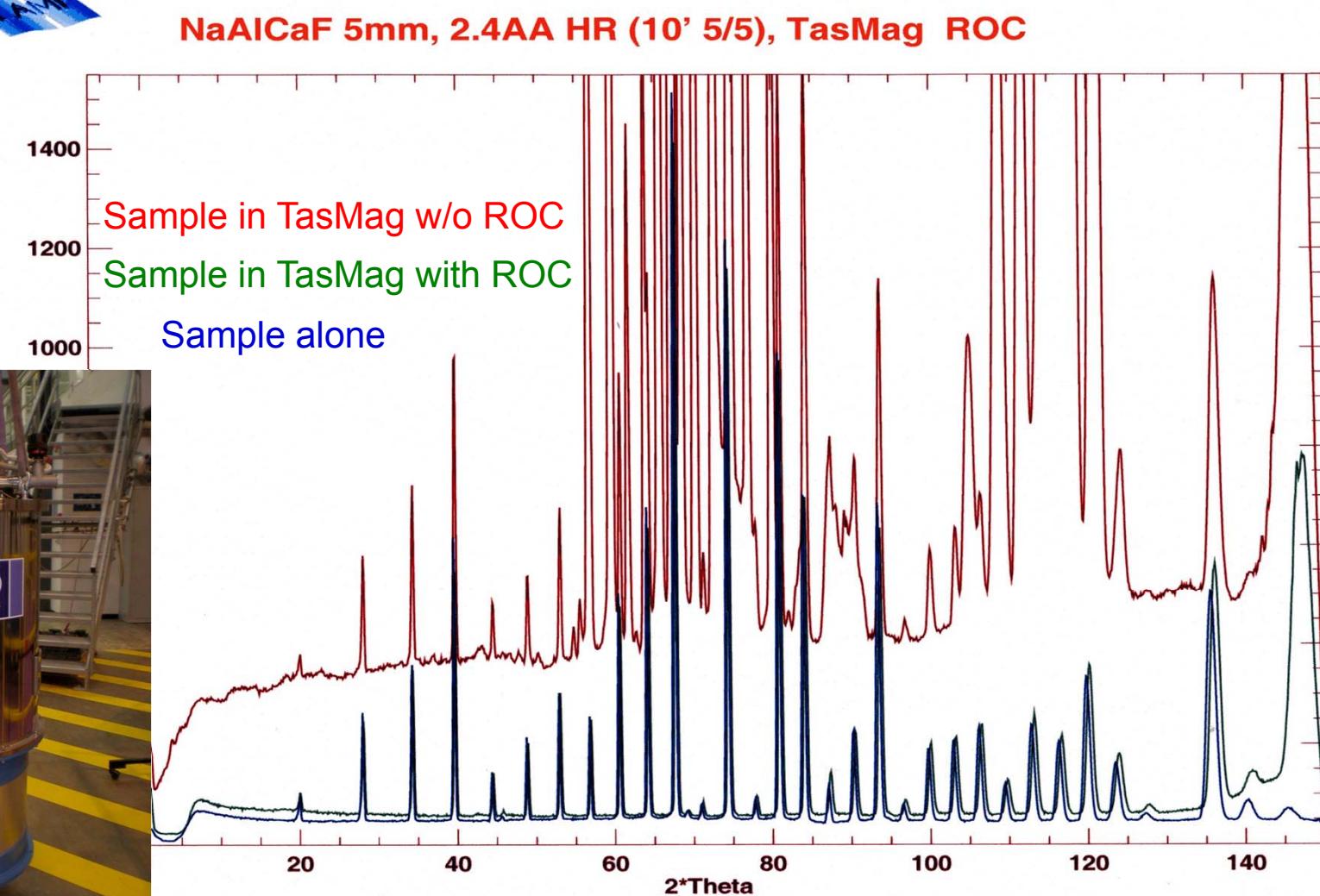
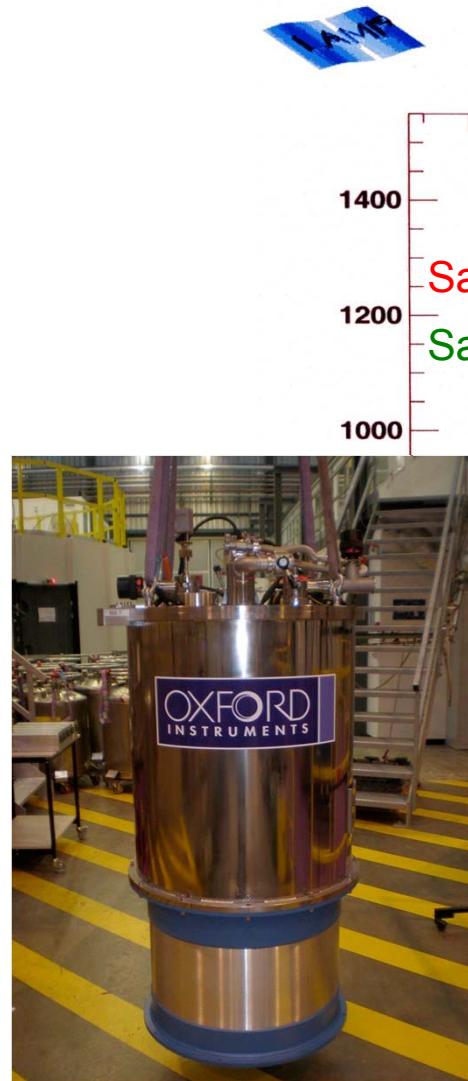


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SPALLATION  
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Photos Courtesy ILL

# Parasitic scattering can ruin experiments: ROC example

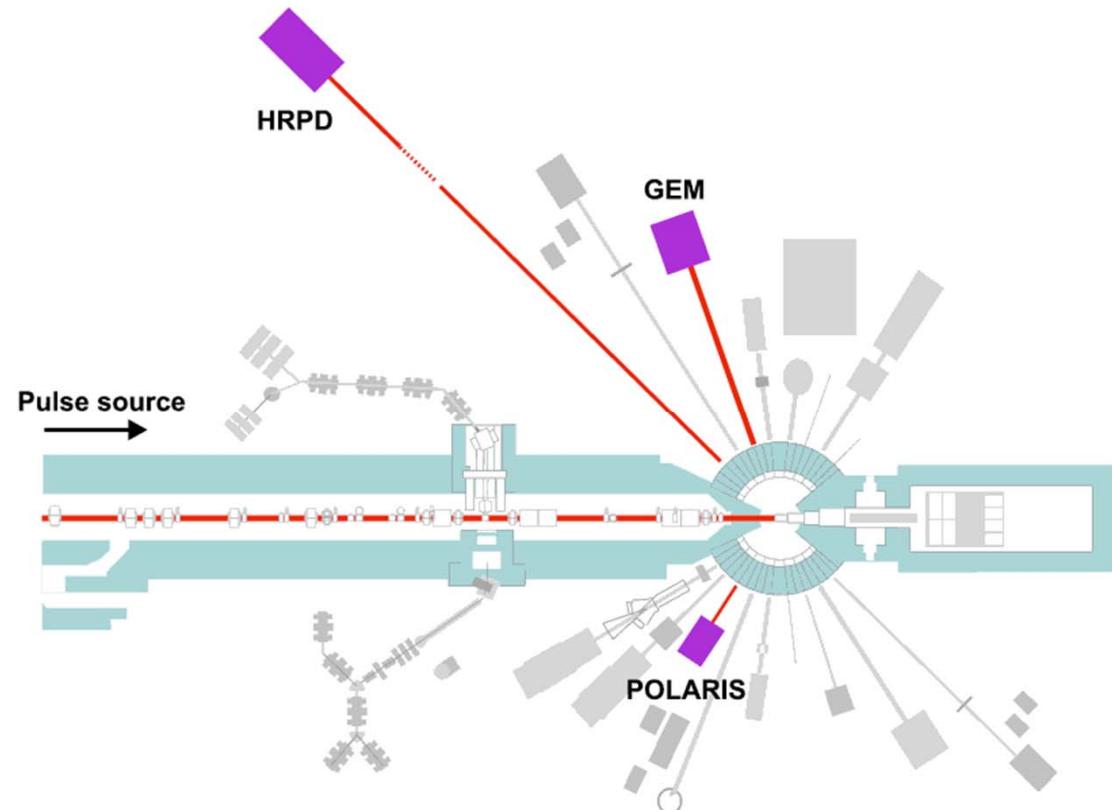


# Time-of-flight Powder Instruments



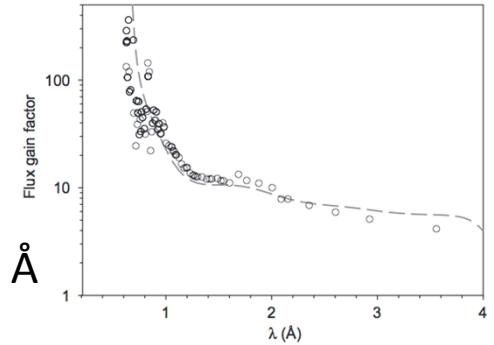
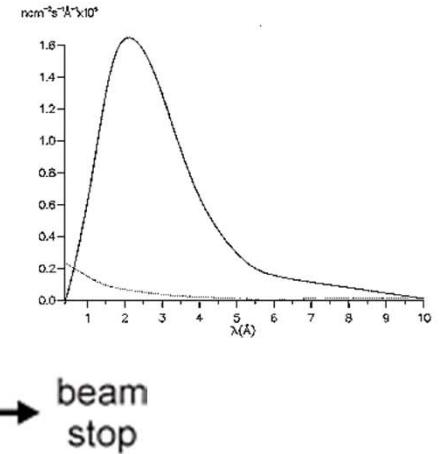
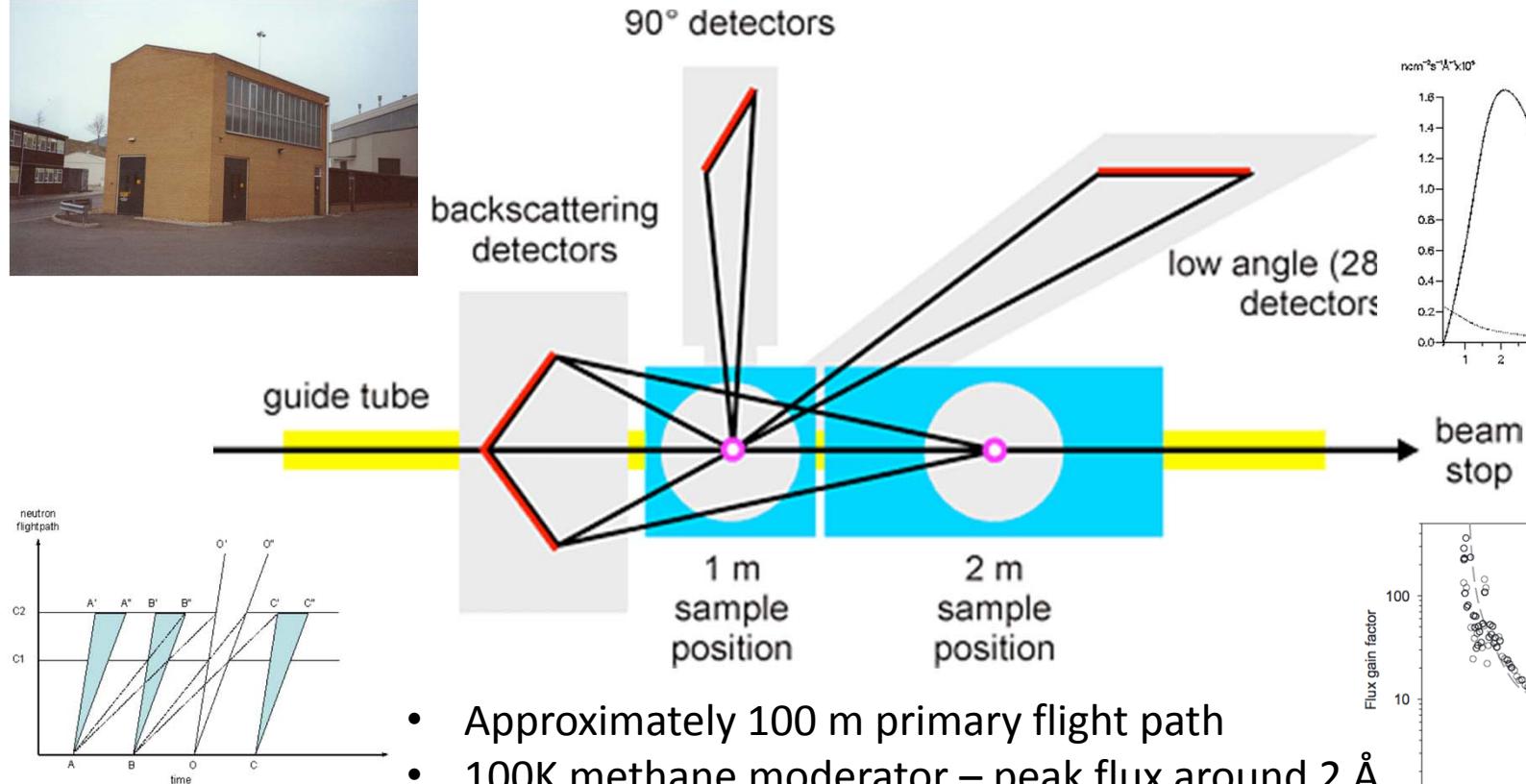
Highlight using 3 examples  
from ISIS TS-1

- HRPD – high resolution powder
- GEM – general purpose powder
- POLARIS – general purpose powder (old and new configuration)



All photos on the following slides from instruments at ISIS are courtesy of STFC

# Time-of-flight, high resolution powder: HRPD at ISIS



- Approximately 100 m primary flight path
- 100K methane moderator – peak flux around 2  $\text{\AA}$
- Operates at 5 or 10 Hz cf. TS-1 50 Hz
- Wavelength band 4  $\text{\AA}$  (5 Hz) or 2  $\text{\AA}$  (10 Hz)
- Supermirror guide upgraded in 2008 (36 km radius of curvature)

# HRPD at ISIS



**Table 1. HRPD Detector Bank Details**

	Backscattering	90°	Low Angle
Detector Specification	ZnS scintillator	ZnS scintillator	½" 10atm He <sup>3</sup> gas tubes
Geometry	60 rings: 7 < r <sub>1</sub> < 8.5cm 35.5 < r <sub>60</sub> < 37cm 8 Octants: 4147cm <sup>2</sup>	Slab: 20 x 20cm 66 x 3mm elements 6 Modules: 2400cm <sup>2</sup>	72 tubes: (20cm active length) 8 tubes/module 9 Modules: 1800cm <sup>2</sup>
Fixed Scattering Angle	160° < 2θ < 176° (1m)	87° < 2θ < 93°	28° < 2θ < 32°
Solid Angle ( $\Omega$ )	0.41 ster (1m)	0.08 ster	0.01 ster
Resolution ( $\Delta d/d$ )	$\sim 4.5 \times 10^{-4}$	$\sim 2 \times 10^{-3}$	$\sim 2 \times 10^{-2}$
d-spacing range (30-230ms)	$\sim 0.6 - 4.6 \text{ \AA}$ $0.25 - 4.6 \text{ \AA}$	$\sim 0.9 - 6.6 \text{ \AA}$ $0.4 - 6.6 \text{ \AA}$	$\sim 2.2 - 16.5 \text{ \AA}$ $1.0 - 16.5 \text{ \AA}$

- Large backscattering detector to minimise  $\cot^2\theta$  in resolution term
- High resolution at intermediate Q
- Long flight path to reduce  $\Delta t/t$  and  $\Delta L/L$  uncertainties
- Pulse skipping to increase bandwidth (@50 Hz 0.4 Å)
- Good combination of parameters for a high resolution TOF diffractometer

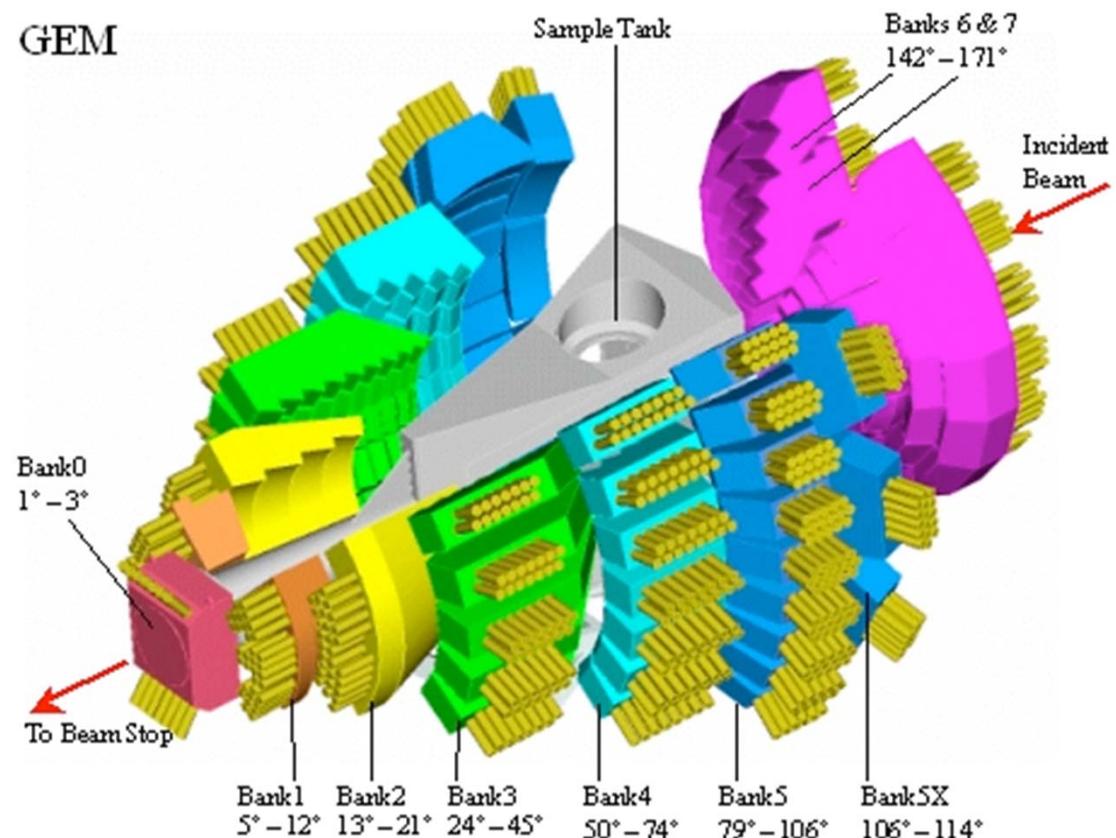
Contemporary instrument sHRPD (J-PARC), no current analogue at SNS

# Time-of-flight, General Purpose Powder: GEM (General Materials) at ISIS



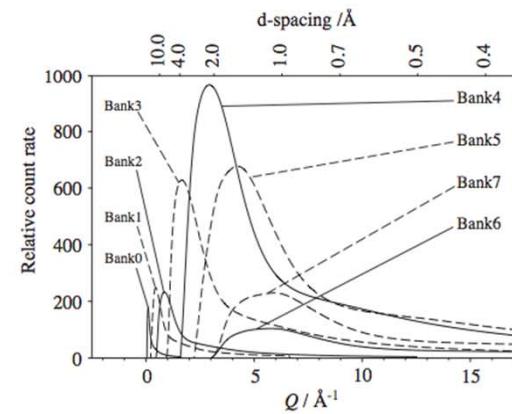
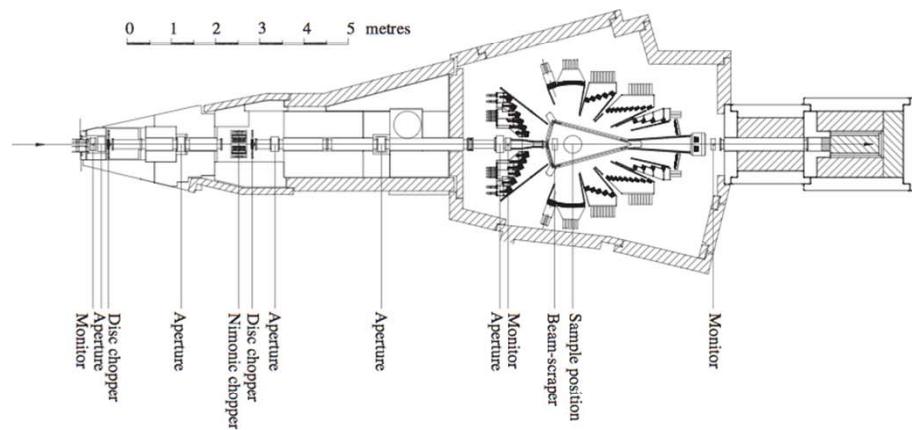
Initially constructed in the late 1990s this powder/liquids diffractometer hybrid changed the way TOF diffraction instruments were designed and built

- Approximately 17 m primary flight path
- 100K methane moderator
- 50 Hz Operation
- Wavelength band 0.05 – 3.4 Å
- Large area detector array of 7.27 m<sup>2</sup>
- ZnS detectors
- Radial oscillating collimator



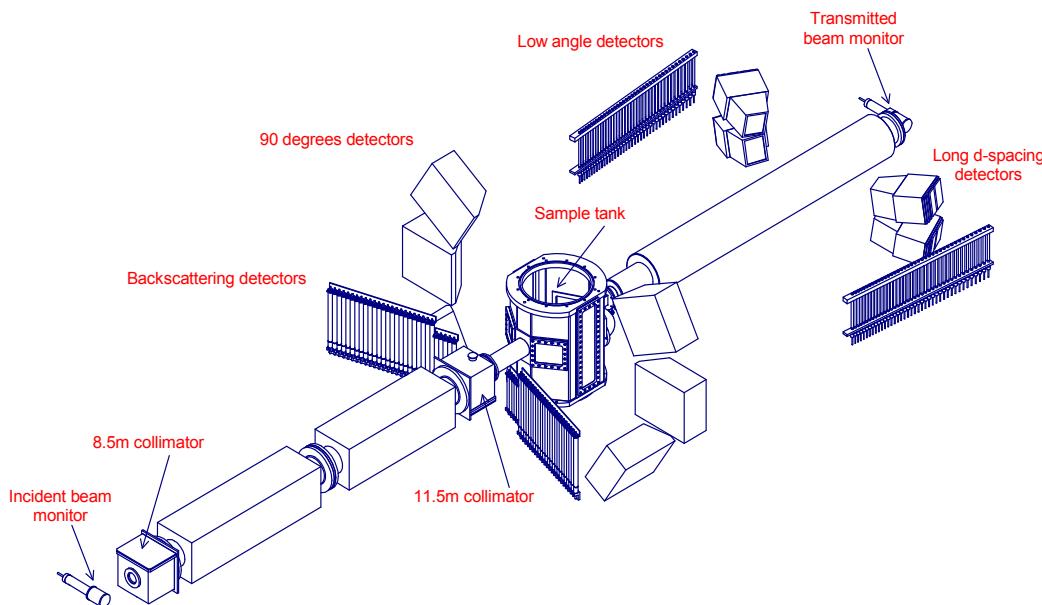
# GEM at ISIS

Detector Bank	Scattering angle $2\theta$ (deg)	Range in azimuthal angle $\phi$ (deg)	Secondary flight path $L_2$ (m)	Number of detector elements/modules	Solid angle $\Omega$ (sr)	Resolution $\Delta Q/Q(\%)$	Minimum accessible momentum transfer $Q_{\min}$ ( $\text{\AA}^{-1}$ )
Bank0	1.21–3.18	$\pm 90.0$	2.757–2.767	80/4	0.008	5–10	0.04
Bank1	5.32–12.67	$\pm 45.0$	2.365–2.376	330/6	0.056	4.7	0.17
Bank2	13.44–21.59	$\pm 43.4$	1.477–2.100	320/4	0.093	2.4	0.43
Bank3	24.67–45.61	$\pm 42.5$	1.077–1.893	900/10	0.478	1.7	0.79
Bank4	50.07–74.71	$\pm 44.4$	1.028–1.436	1400/14	0.988	0.79	1.56
Bank5	79.07–106.60	$\pm 44.5$	1.376–1.383	2160/18	1.135	0.51	2.35
Bank5X	106.02–114.19	$\pm 42.7$	1.377–1.387	720/18	0.378	0.5	2.95
Bank6	142.50–149.72	$\pm 69.3$	1.544–1.738	560/14	0.280	0.34	3.50
Bank7	149.98–171.40	$\pm 66.6$	1.035–1.389	800/10	0.443	0.35	3.57

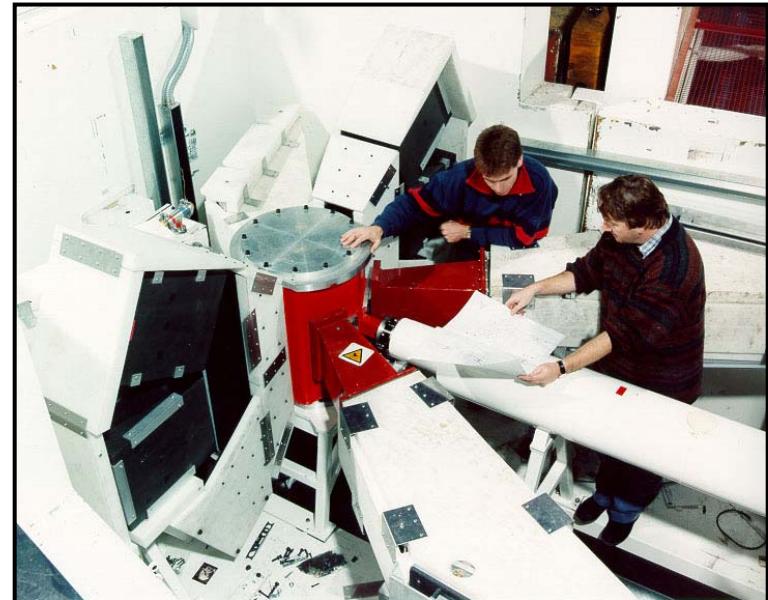


From Hannon, NIMA (2005), 551, 88-107

# Time-of-flight, General Purpose Powder: POLARIS (old configuration)



- 316K H<sub>2</sub>O poisoned at 1.5 cm
- Primary flight path 12 m
- Wavelength band 0.1 – 6 Å
- 50 Hz operation
- Maximum sample dimensions 4 × 2 cm



- Compare with GEM:
- Higher sample flux
  - Wider bandwidth
  - Lower resolution
  - Hotter spectrum
  - Lower detector coverage

# POLARIS (old configuration)



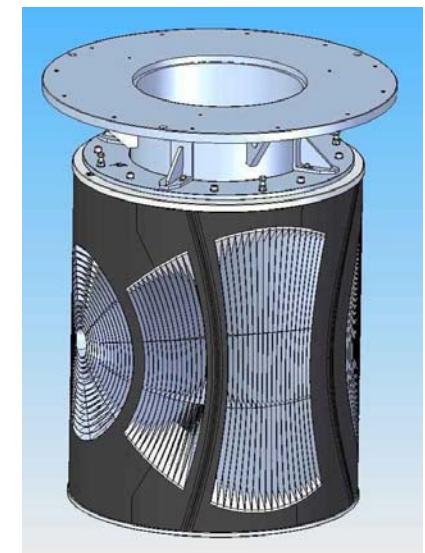
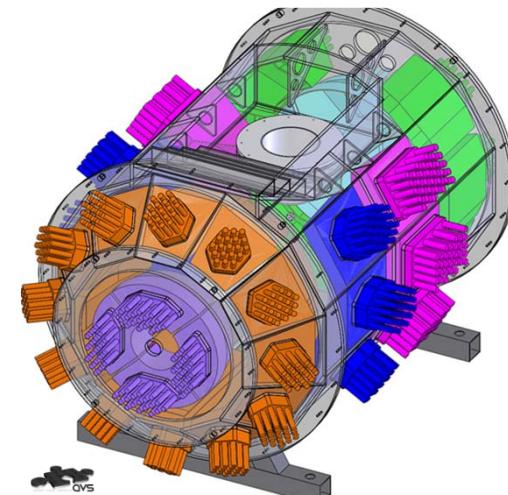
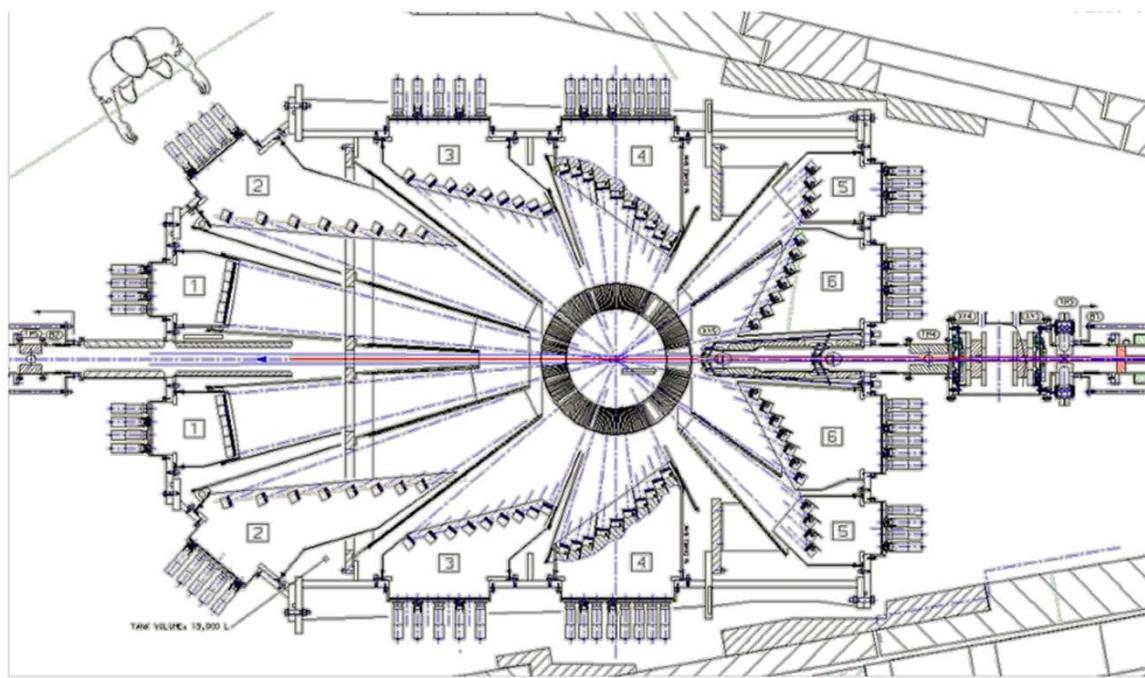
EUROPEAN  
SPALLATION  
SOURCE

bank position (label)	low angle (A)	low angle (B)	backscattering (C)	90 degrees (E)
detector type	$^3\text{He}$	ZnS	$^3\text{He}$	ZnS
no. of elements	$2 \times 40 = 80$	$4 \times 20 = 80$	$2 \times 29 = 58$	$6 \times 36 = 216$
L <sub>2</sub> (m)	1.72 - 2.65	~2.2	0.65 - 1.35	~0.80
2θ range	$28^\circ < 2\theta < 42^\circ$	$13^\circ < 2\theta < 15^\circ$	$130^\circ < 2\theta < 160^\circ$	$83^\circ < 2\theta < 97^\circ$
Ω (ster)	0.046	0.009	0.29	0.48
Δd/d	$\sim 1 \times 10^{-2}$	$\sim 3 \times 10^{-2}$	$\sim 5 \times 10^{-3}$	$\sim 7 \times 10^{-3}$
d-range (Å)	0.5 - 8.3	0.5 - 21.6	0.2 - 3.2	0.2 - 4.0
Q-range (Å <sup>-1</sup> )	0.75 - 12.6	0.3 - 12.6	2.0 - 31.4	1.5 - 31.4

- Good workhorse instrument for powder diffraction
- High Q accessible for disordered materials investigation using the PDF method
- Some in situ capability but limited by count-rate
- Compatible with a wide range of restricted geometry sample environment

Once GEM detector array completed in 2005, ISIS started to look at how POLARIS might be upgraded. Huge growth in PDF studies and in situ processing communities. Need an instrument with extended Q-range, higher count-rate and similar resolution to POLARIS taking lessons learned from GEM instrument design and construction.

# POLARIS Upgrade



- Increase primary flight path to 14 m
- Optimise each detector bank to give constant resolution
- Increase detector coverage
- Design a collimator to reduce background and parasitic scattering

<http://www.isis.stfc.ac.uk/instruments/polaris/polaris-upgrade-poster11575.pdf>

# POLARIS Upgrade



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SPALLATION  
SOURCE



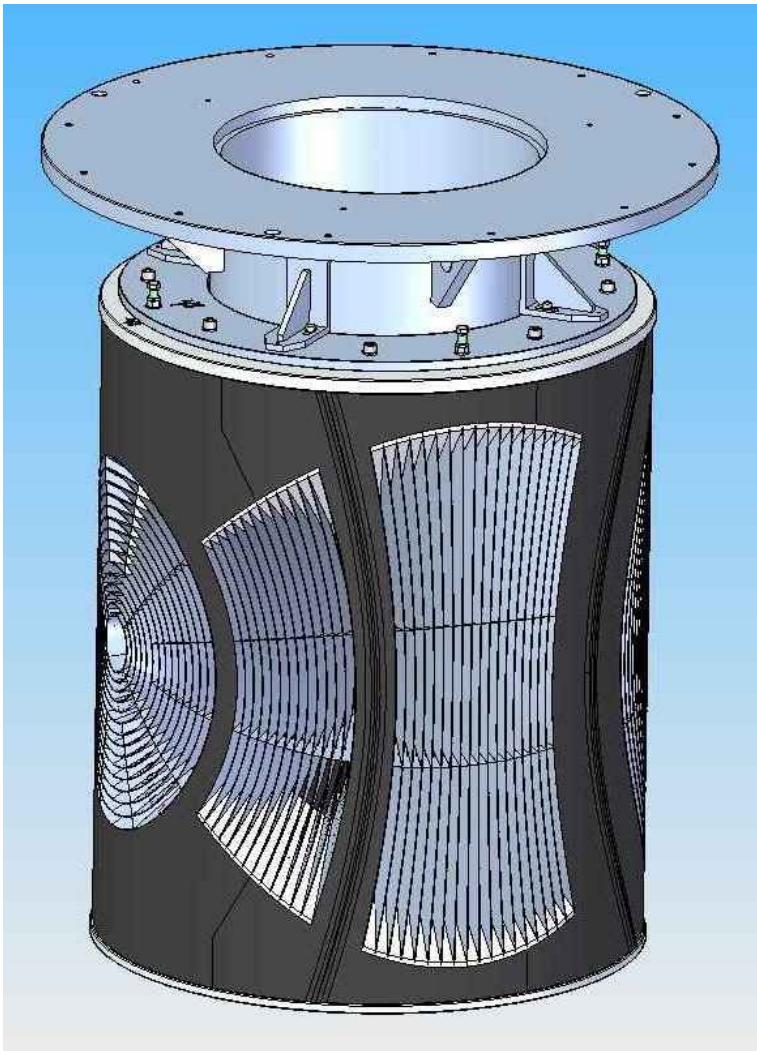
<http://www.isis.stfc.ac.uk/instruments/polaris/polaris4643.html>



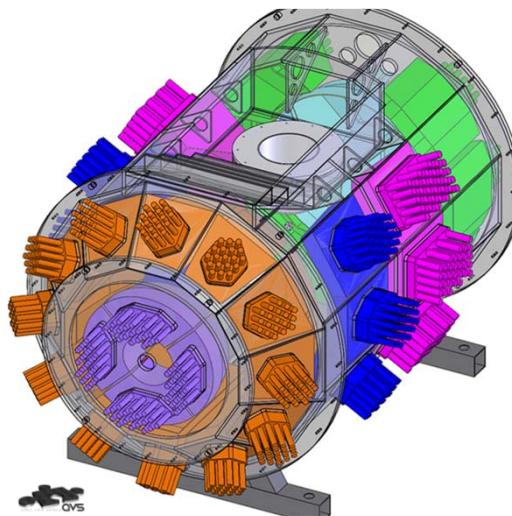
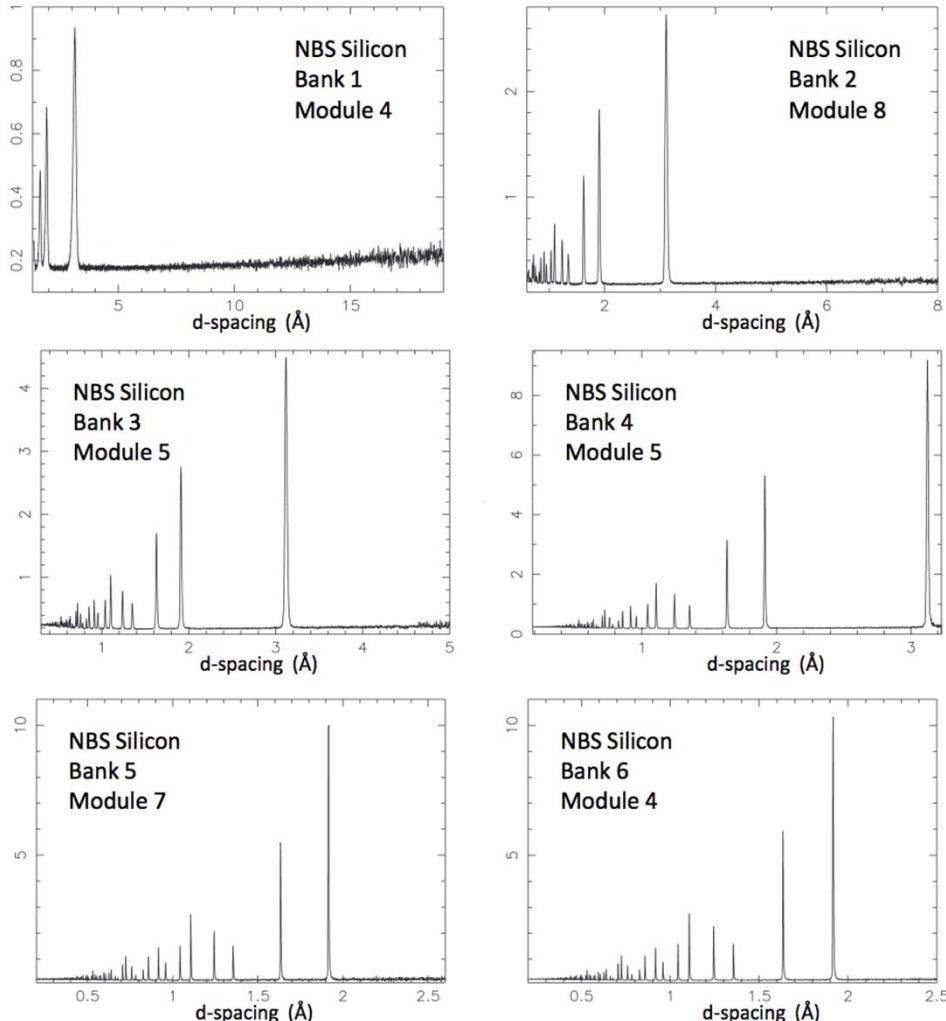
# POLARIS Upgrade



EUROPEAN  
SPALLATION  
SOURCE



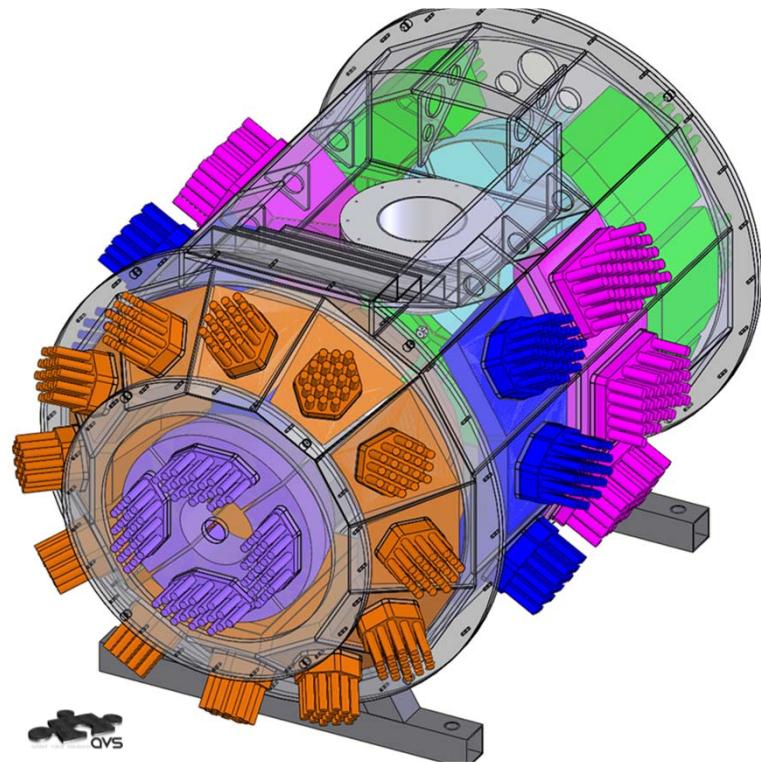
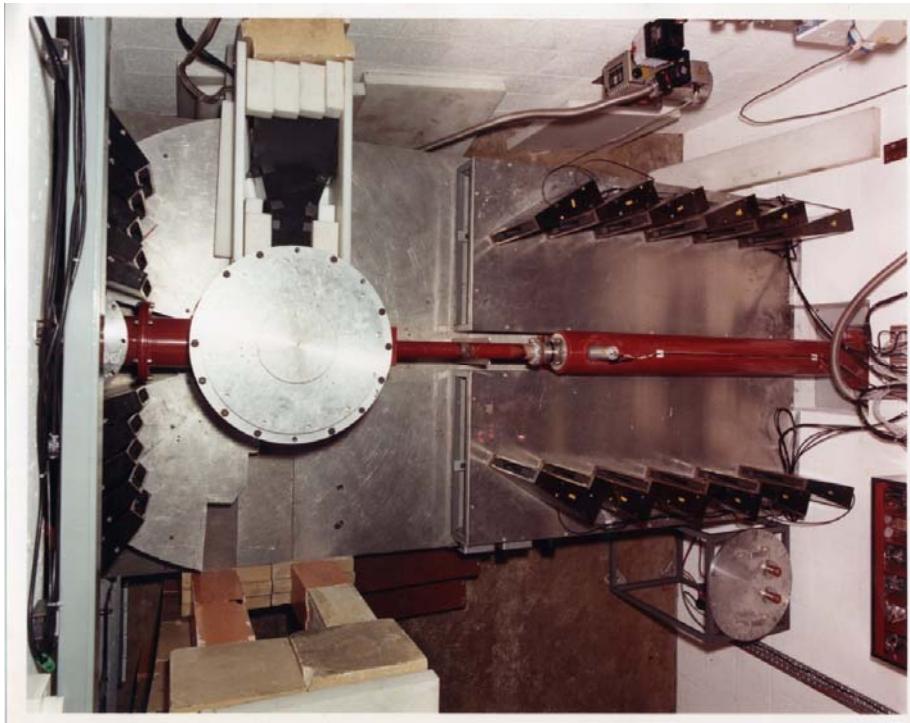
# New POLARIS



Bank 1 – cyan  
Bank 2 – green  
Bank 3 – pink  
Bank 4 – blue  
Bank 5 – orange  
Bank 6 - purple

- Increased count rate factor from 3 at high scattering angle to >20 for low angle banks
- Resolution improvement e.g. bank 5 and 6 of  $3 \times 10^{-3}$  cf.  $5 \times 10^{-3}$
- Improvement in data at high Q

# POLARIS 1995 cf. 2013



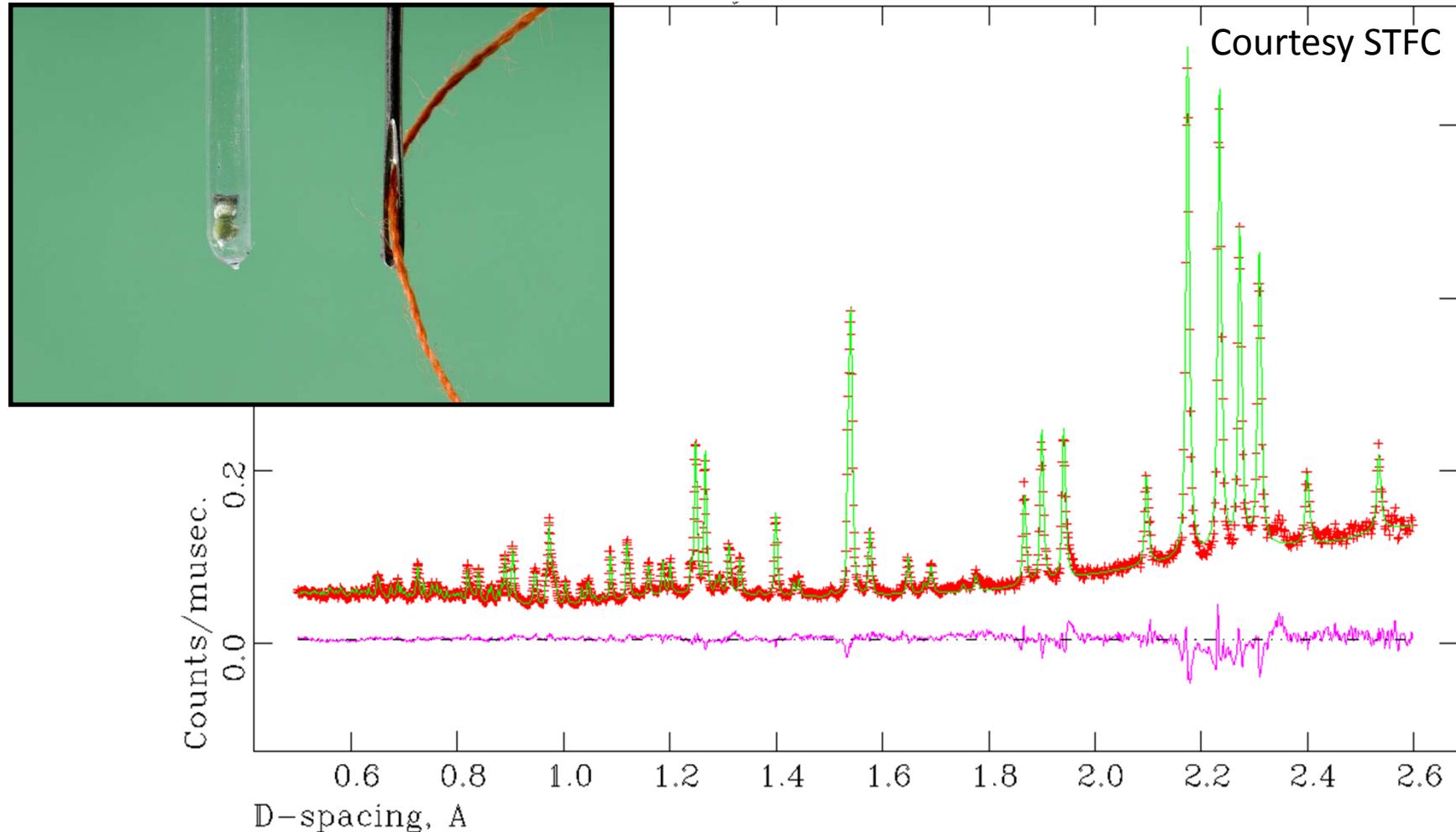
- 1995 500 mg 24+ hrs
- 2013 500 mg 15-20 minutes with increased Q-range

Contemporary instruments NOVA and iMateria (J-PARC), POWGEN-3 (SNS)

# Pushing the boundaries in sample size



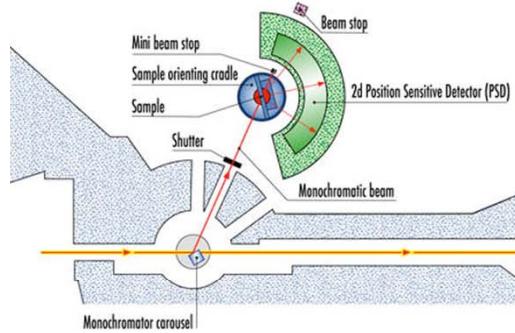
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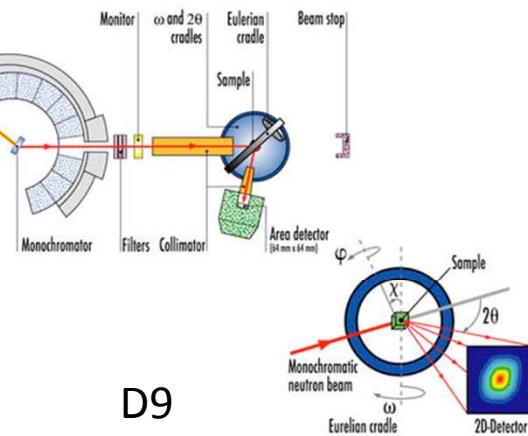
~1mm<sup>3</sup> sample of NaNiF<sub>3</sub> phase prepared at high  $p$  + high T

Lindsay-Scott *et al*, J. Appl. Cryst., **47**, 1939 (2014).

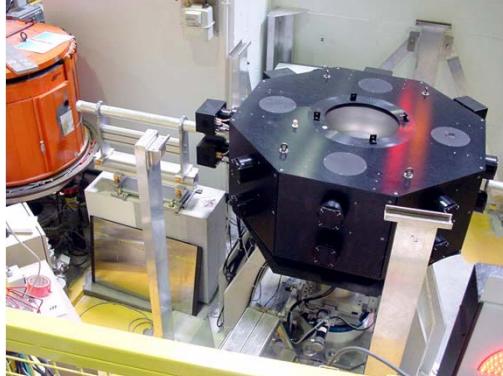
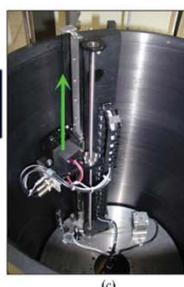
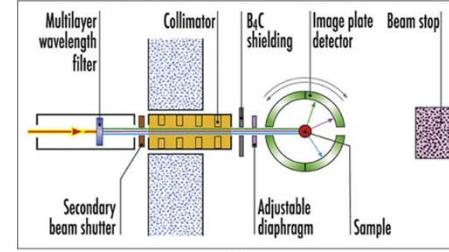
# Single Crystal Instruments Continuous Source - ILL



D19



D9



LADI-III

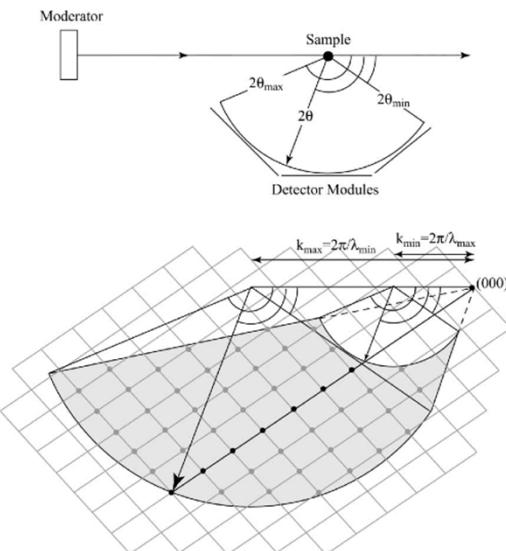
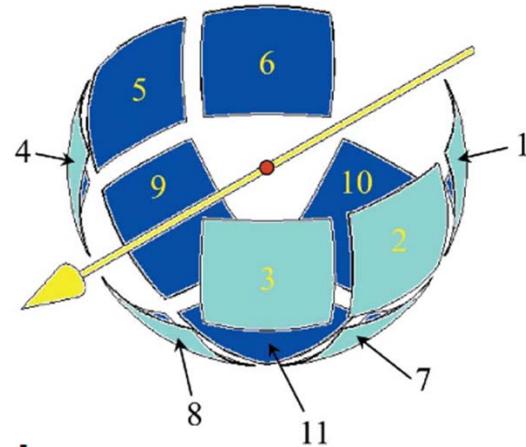
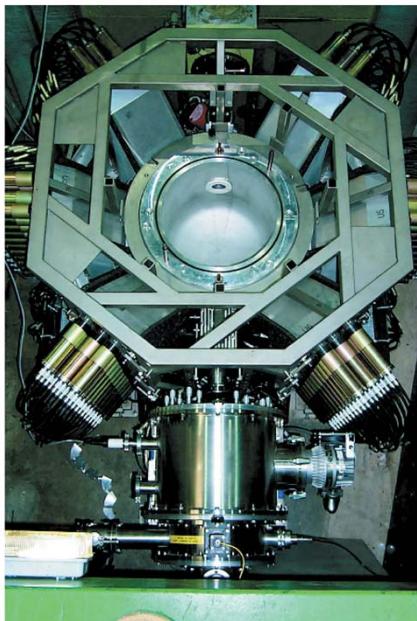
CYCLOPS

- Monochromatic and Laue type instruments are represented
- Q-range of interest and unit cell volume determine whether hot, thermal or cold neutron spectrum required for both instrument types

# Single Crystal Instruments: Spallation Source – SXD at ISIS



- H<sub>2</sub>O moderator poisoned at 2 cm
- 0.2 – 10 Å wavelength band
- Primary flight path 8.3 m
- Beam size < 15 mm
- 11 192 × 192 mm<sup>2</sup> detectors (3 × 3 mm<sup>2</sup> resolution)



Unlike an image plate set-up the detectors are continuously read-out as a function of TOF allowing spatial overlap to be resolved in the TOF channel and minimising background

Keen *et al.* J. Appl. Cryst. (2006), **39**, 714-722)  
<http://www.isis.stfc.ac.uk/instruments/sxd/sxd4813.html>

# Designing diffractometers



EUROPEAN  
SPALLATION  
SOURCE

## Define a science case

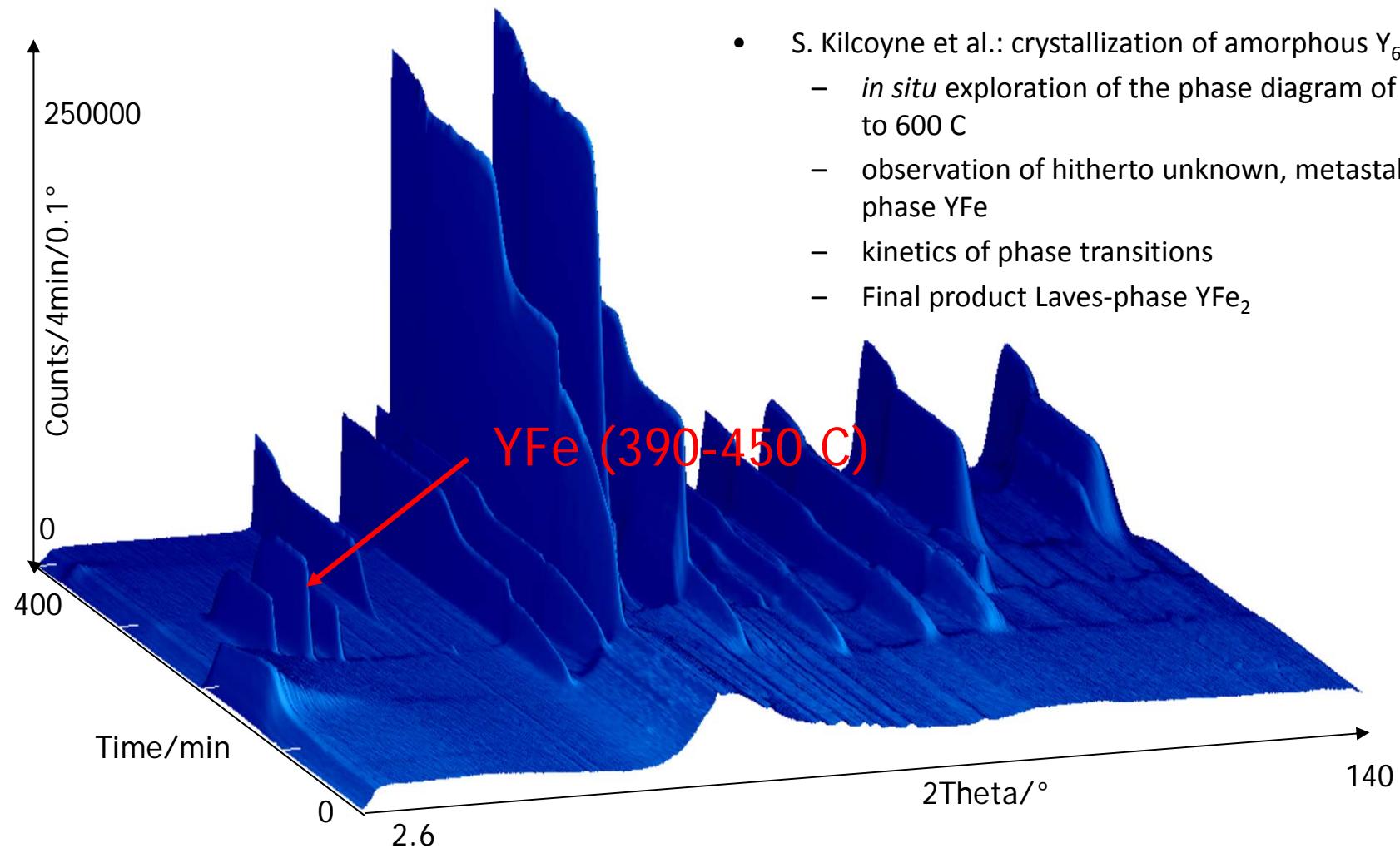
Instruments are designed and built to perform science

# Uses of Diffraction



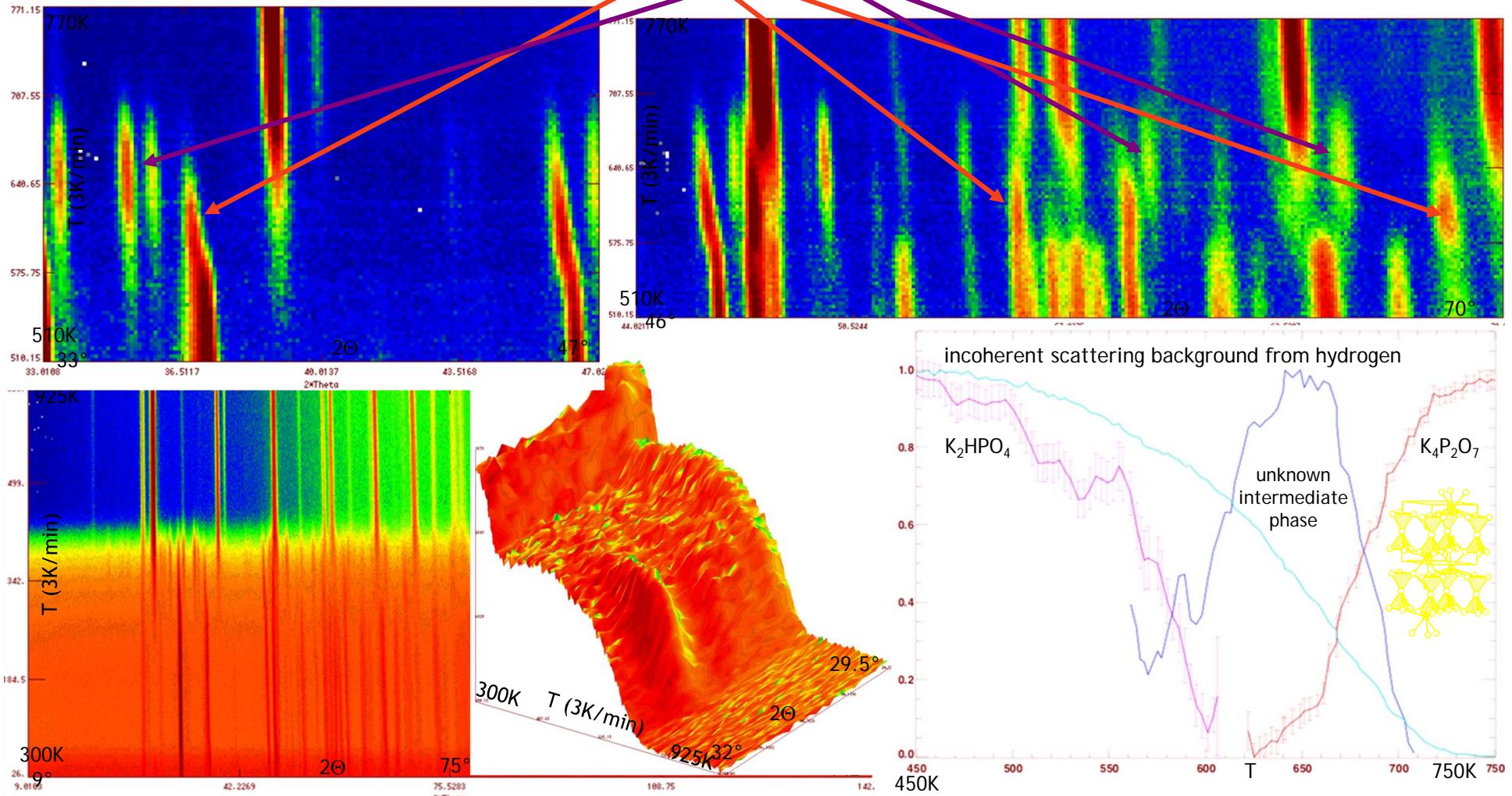
- Check purity of a sample
- Identify known phases
- Identify new phases
- Collect data for structural analysis
- Follow phase transitions
- Construct phase diagrams (T, P, B, etc)
- Study chemical processes in-situ
- Monitor particle size
- Analyse residual stress within materials
- Process control
- Many other uses

# Crystallisation

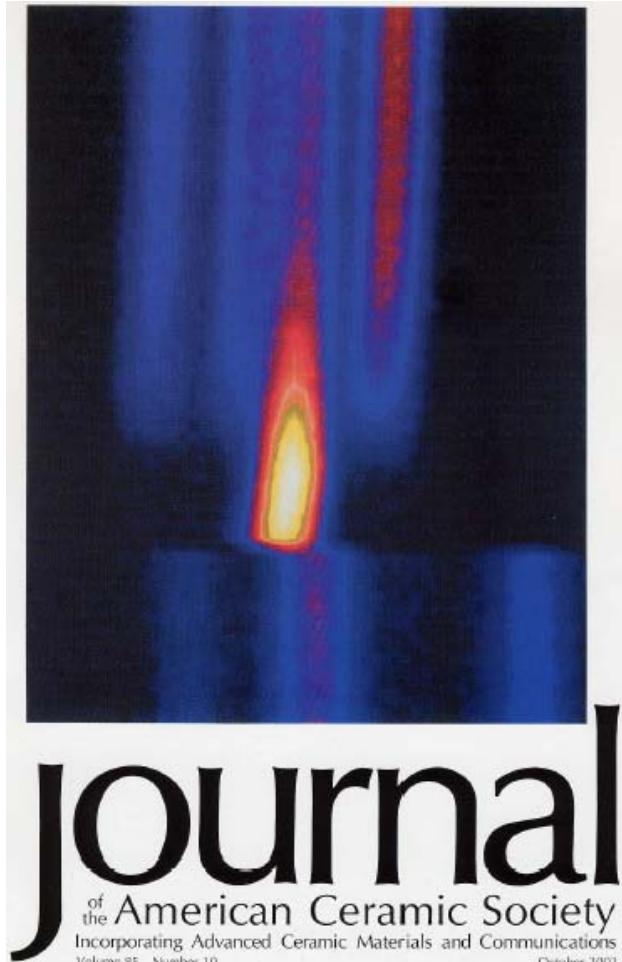


# In situ processing: dehydration

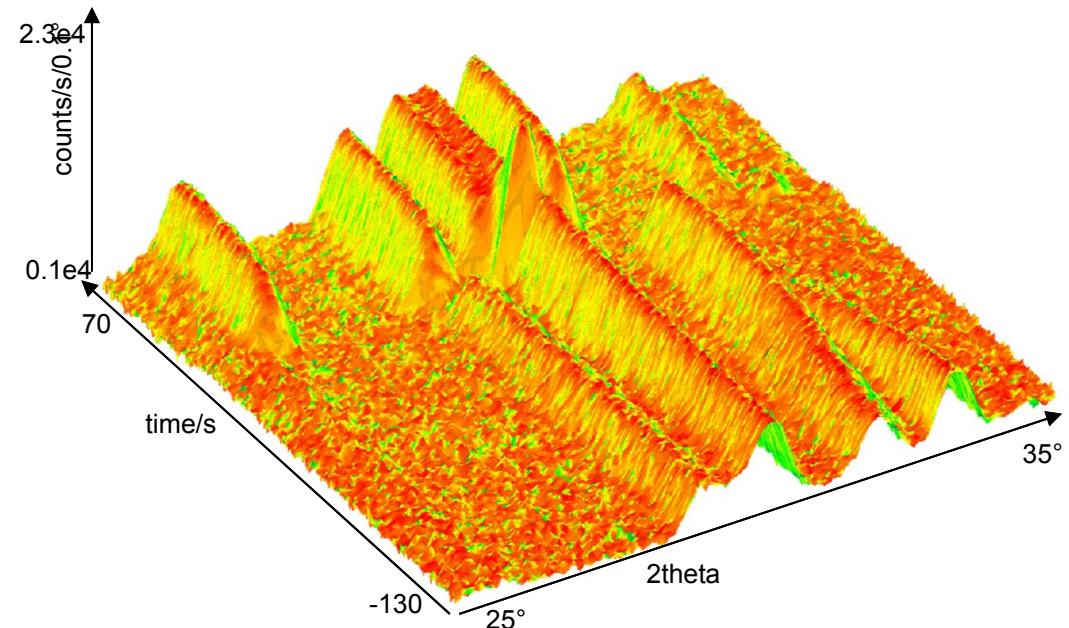
- $\text{K}_2\text{HPO}_4 \cdot 3\text{H}_2\text{O}$   $\text{K}_2\text{HPO}_4$  ?? ?  $\gamma\text{-K}_2\text{P}_2\text{O}_7$



# In situ processing: fast reactions



$\text{Ti}_3\text{SiC}_2$  made by hot isostatic pressing is expensive  
In-situ investigation of thermal explosion synthesis (TES)  
Initiate by heating from 850-1050 °C at 100 °C/min  
Acquisition time 500 ms (300 ms deadtime)

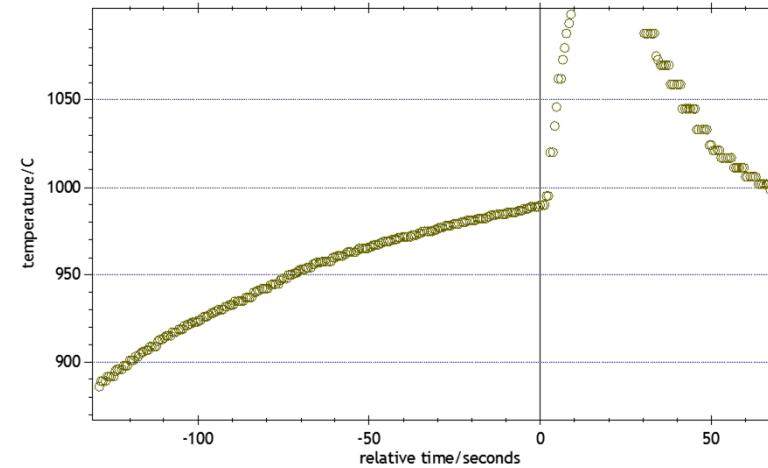
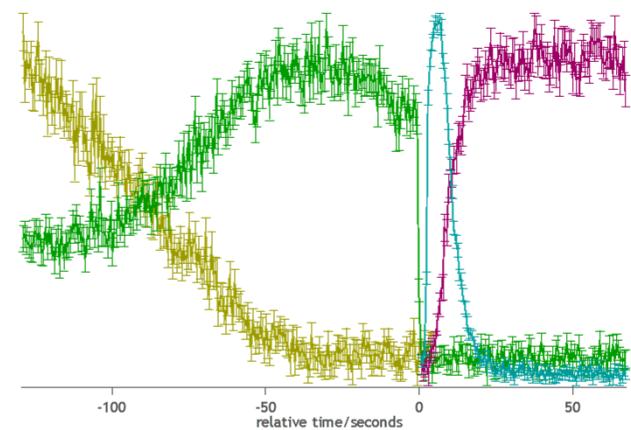
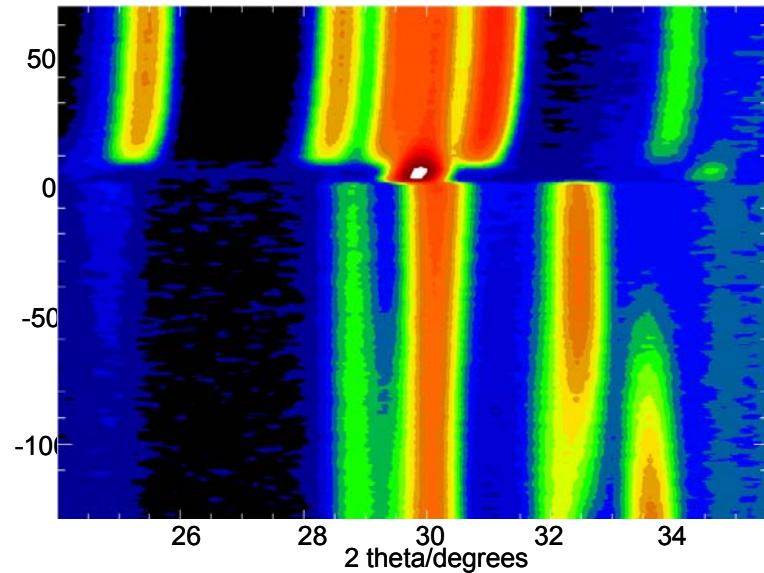


D.P.Riley et al. *J. Am. Ceramic. Soc.* 2002, 2417-2424.

# In Situ Processing

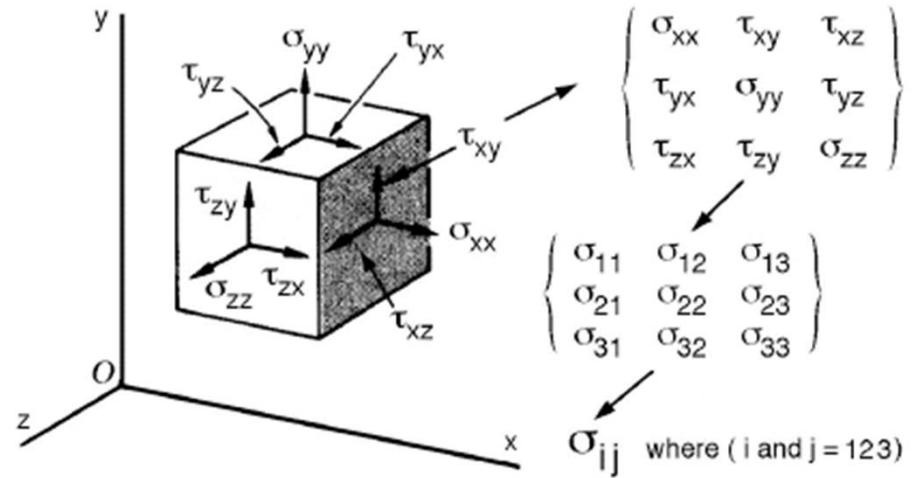
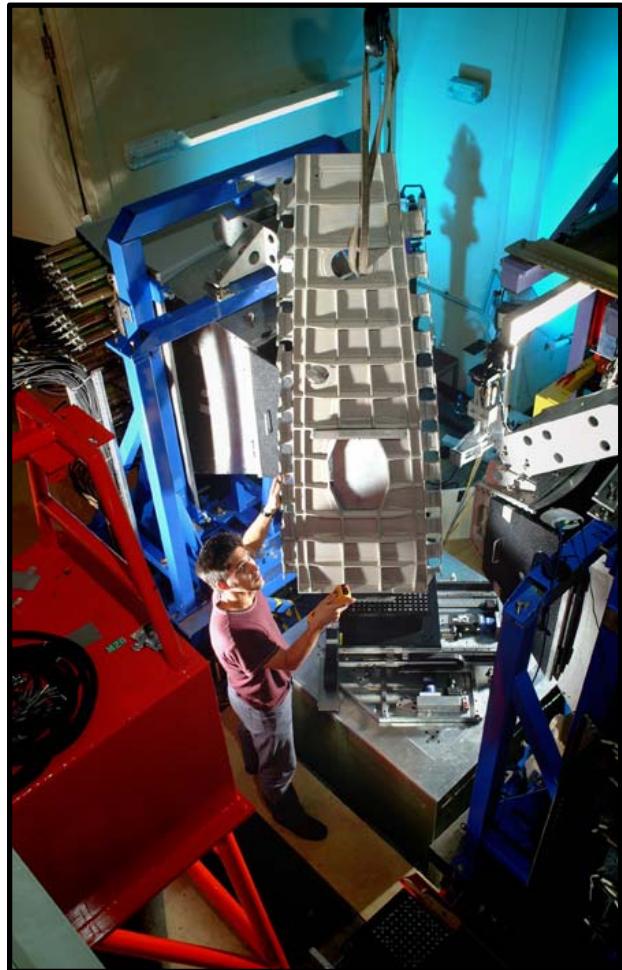


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SPALLATION  
SOURCE



$\alpha \rightarrow \beta$  Ti at 870°C  
TiC<sub>x</sub> growth  
Ignition + melting T ↑ < 2000°C  
Si substituted TiC formed  
Ti<sub>3</sub>SiC<sub>2</sub> precipitates after 5s  
Complete after further 5s

# Diffraction: residual stress



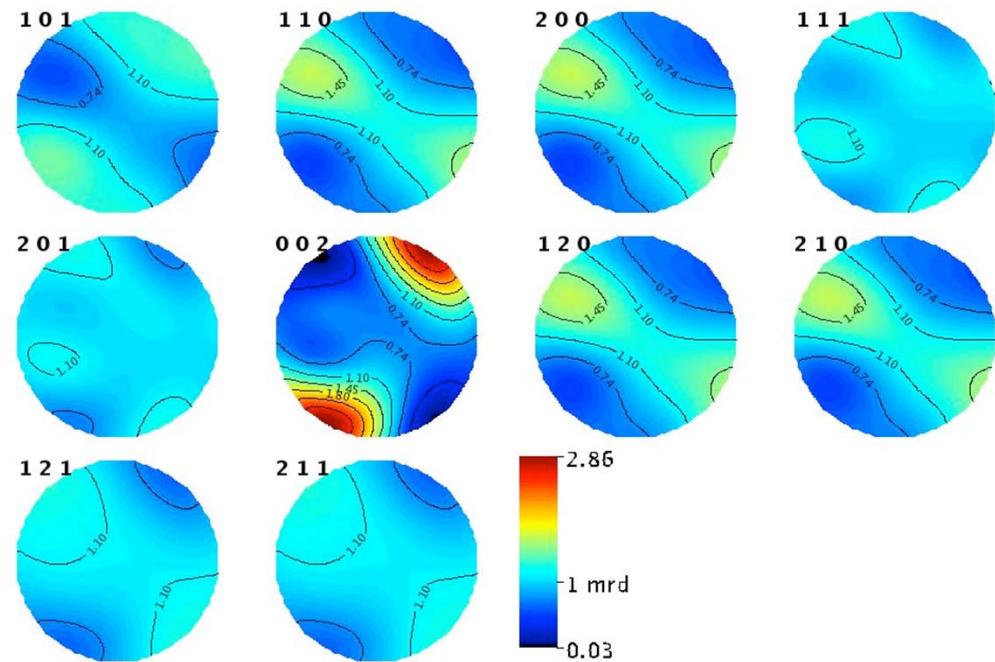
## Applications w.r.t. Residual stresses

Fatigue/Structural Integrity  
Welds  
Alloy development  
Microstructure/Texture  
Phase transformation  
In-situ experiments

Photo courtesy STFC

# Texture analysis

- Peak intensity depending on sample orientation  $I(2\theta, \chi, \varphi)$ 
  - transformed to pole figures (PF)  $I(\alpha, \beta)/<|>$
  - crystallite *orientation distribution function (ODF)*
- *Rietveld texture analysis (RITA)*
  - ODF as parameter set in least squares refinement of a whole data set (300-2000 patterns)
  - reconstruction of complete *pole figures* from ODF
  - program *MAUD* (Lutterotti)



# Final comments



- Diffraction covers a very wide science case
- There are many diffractometers, each optimised to a particular region of parameter space that is determined by the science case
- New sources and instruments will offer new opportunities
- Instrument upgrades can give order of magnitude increases in performance

## Wish list

- Detectors with high efficiency for short wavelength neutrons
- Improved beam transport for short wavelength neutrons