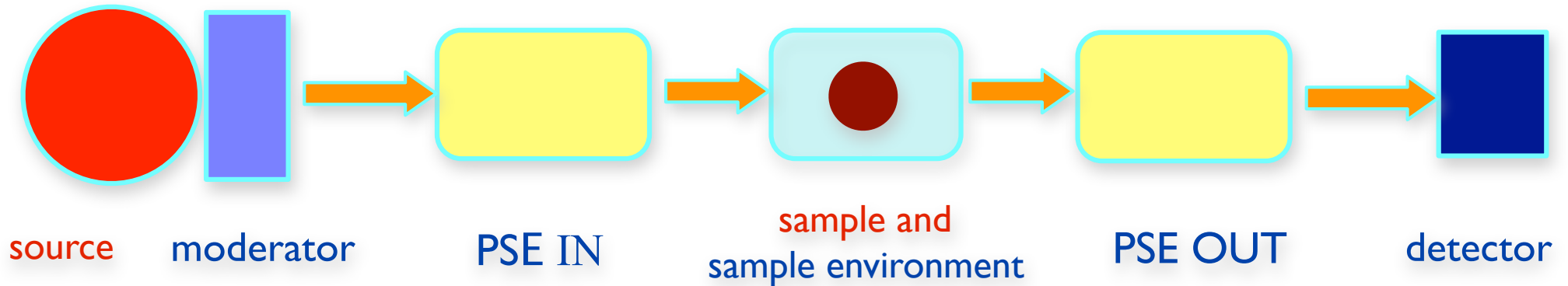


Neutron Spin Echo spectroscopy and Magnetism

Katia Pappas
Delft University of Technology

- Magnetic scattering
- Paramagnetic NSE
- Ferromagnetic NSE: magnetic fields
- Intensity modulated NSE: for samples depolarising the neutron beam: ferromagnets, superconductors
- Polarimetric NSE: chirality

from the source to the detector



Neutron flux

$$\varphi = \Phi \eta \frac{dE d\Omega}{4\pi}$$

source flux
distribution

intensity
losses

field of neutron
instrumentation

definition of the beam : Q, E and polarisation

Neutron Spin Echo

why ?

very high resolution

how ?

using the transverse components of
beam polarization

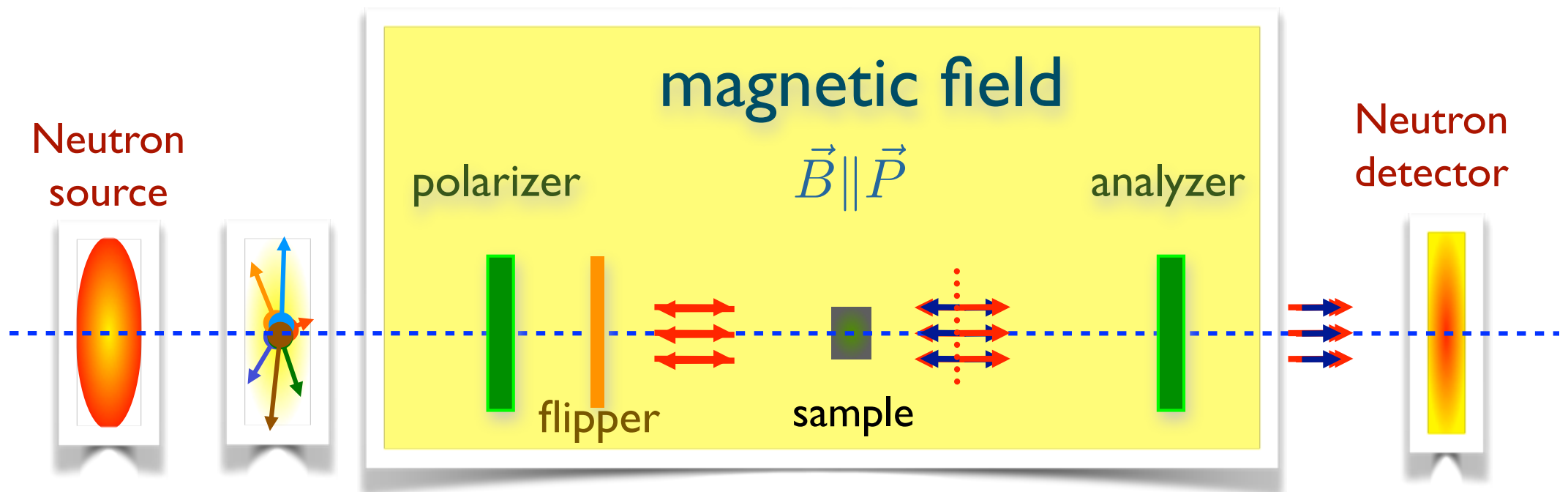
Larmor precession

Polarized Neutrons

● polarizer

● analyzer

magnetic field (guide - precession)

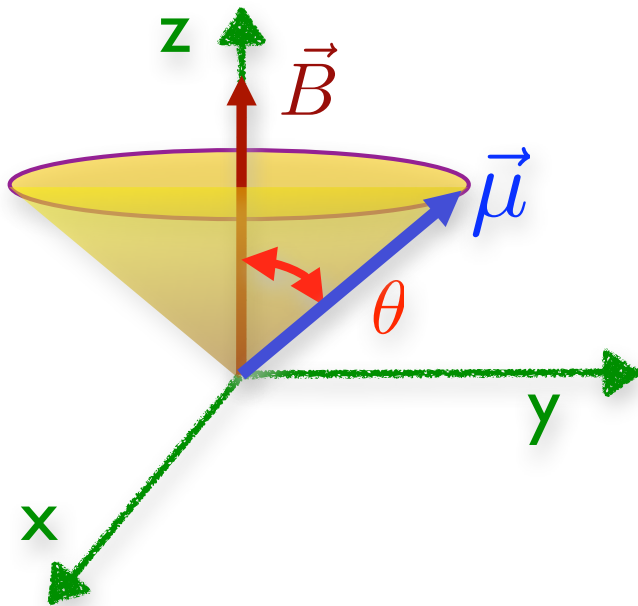


Larmor Precession

Motion of the polarization of a neutron beam
in a magnetic field



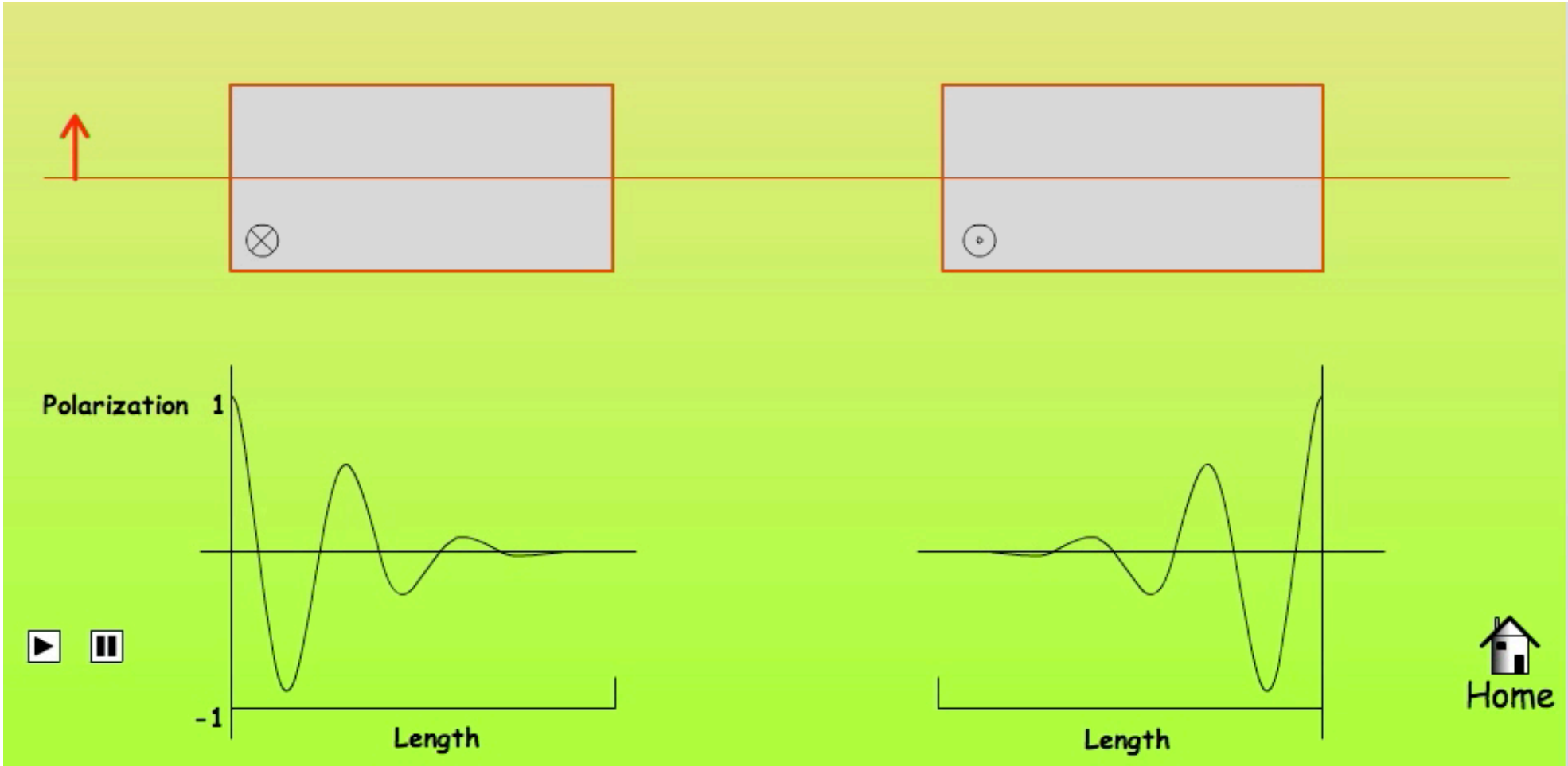
$$\frac{d\vec{\mu}}{dt} = \gamma \cdot (\vec{\mu} \times \vec{B}) = \vec{\mu} \times \vec{\omega}_L$$



Gyromagnetic ratio
of neutrons

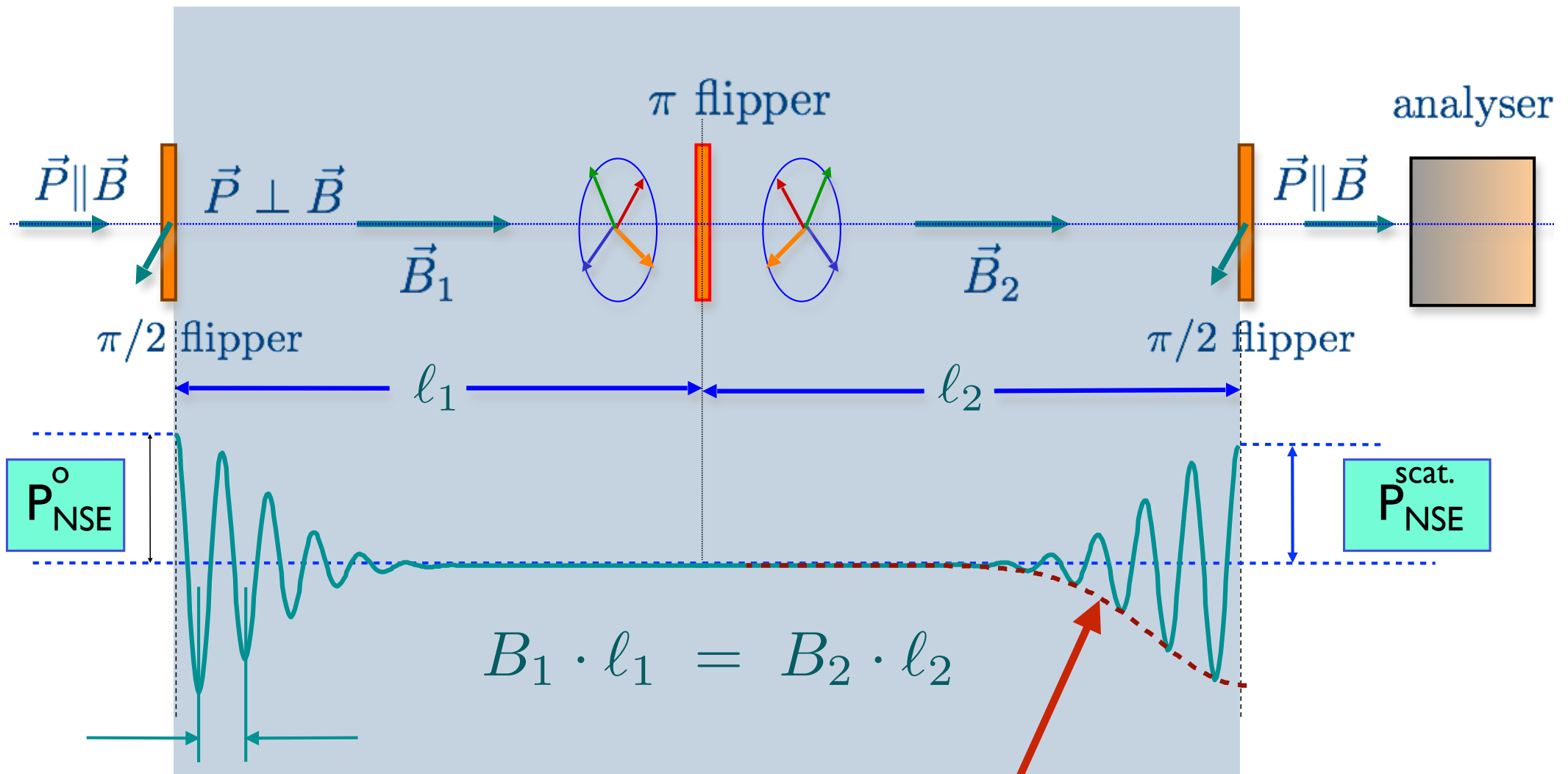
$$\gamma = 183.2 \text{ rad MHz T}^{-1}$$

$$\phi = \gamma B t_{tof} = \gamma B \ell / v$$



after R. Gähler

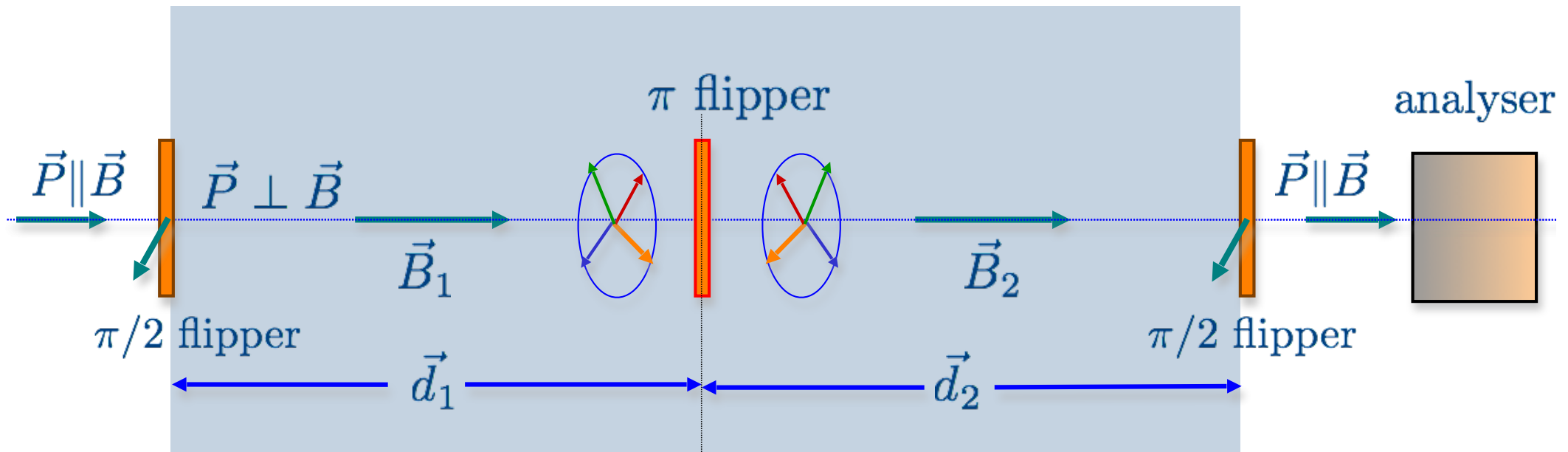
neutron spin echo spectroscopy



$$1.357 \cdot 10^{-5} T \cdot m / \lambda [\text{nm}]$$

$$P_{\text{NSE}, \parallel \vec{B}} = \langle \cos(\phi) \rangle = \int f(v) \cos(\phi) dv$$

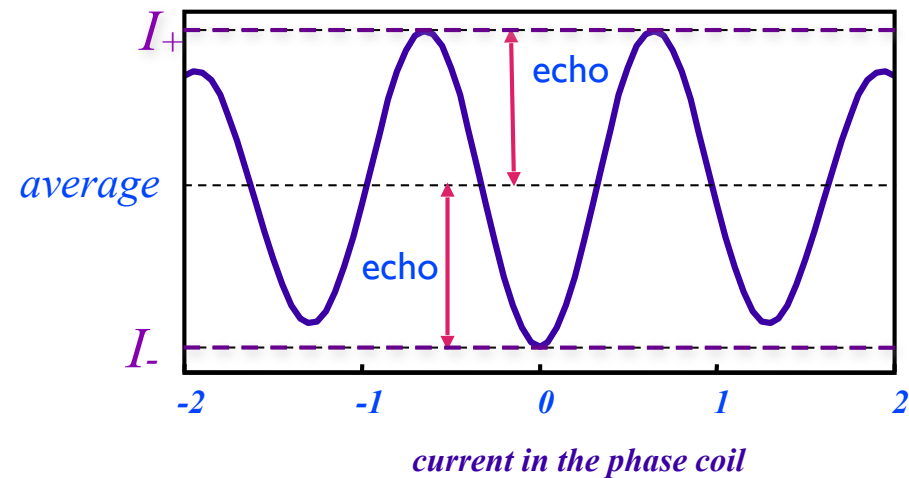
neutron spin echo spectroscopy



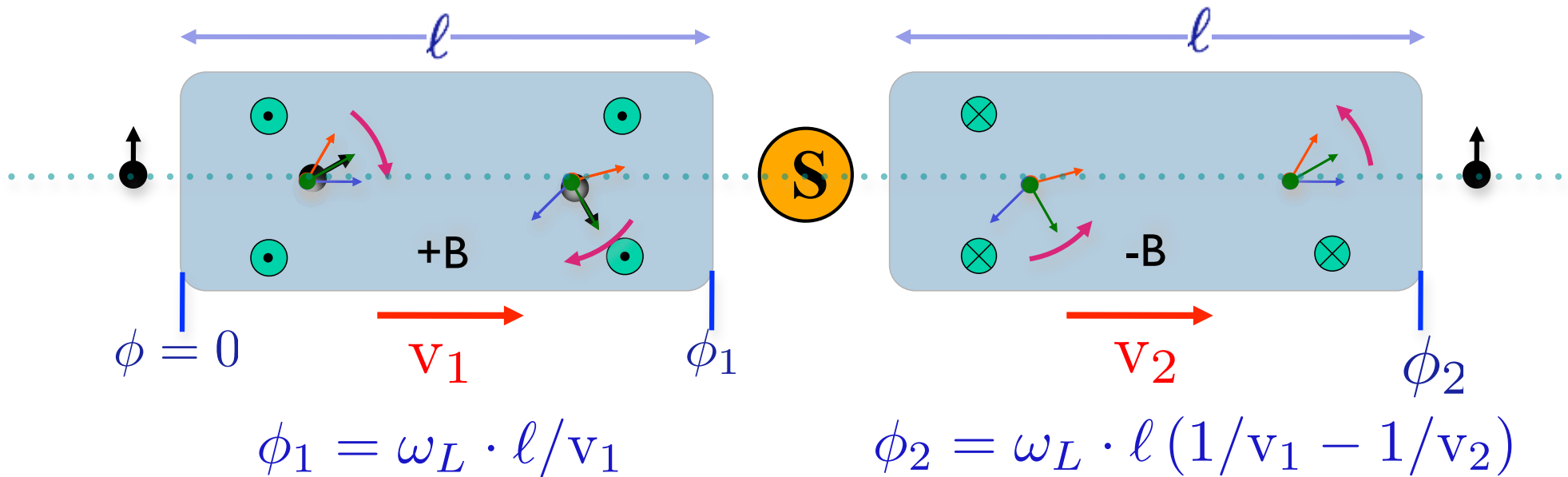
ideally

$$\text{echo modulation} = (I_+ - I_-) / 2$$

$$\text{for } |\vec{P}| = 1$$



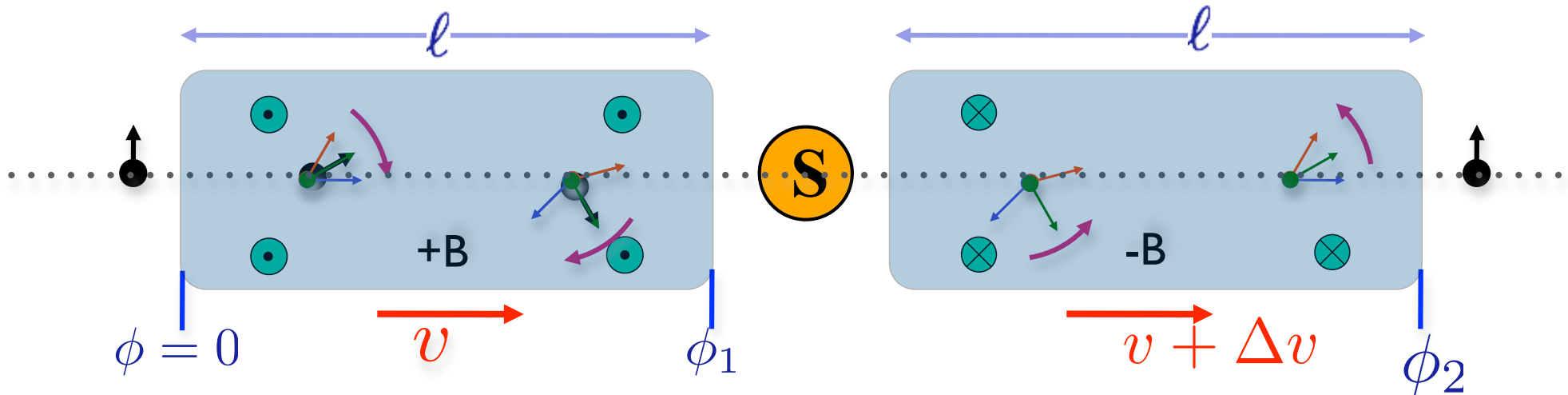
basic equations



for $v_1 = v$ and $v_2 = v + \Delta v \Rightarrow$

$$\phi_2 = \omega_L l [1/v - 1/(v + \Delta v)] \approx \omega_L l \Delta v / v^2 = \omega_L t \Delta v / v$$

basic equations



scattering theory : $\Delta v \rightarrow \omega$

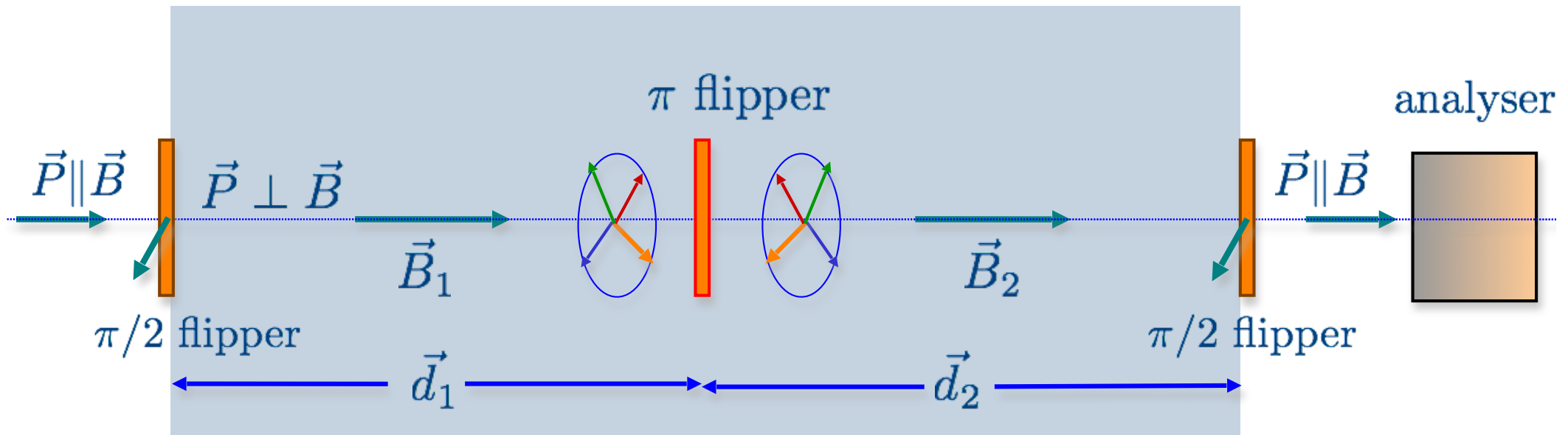
$$\hbar\omega = m/2 \cdot (v_1^2 - v_2^2) = m/2 \cdot (v_1 - v_2) (v_1^2 + v_2^2) \approx m \cdot v \cdot \Delta v$$

$$\phi_2 = \omega_L \ell [1/v - 1/(v + \Delta v)] \approx \omega_L \ell \Delta v / v^2 = \omega_L t \Delta v / v$$

$$\Rightarrow \phi_2 = \phi = t_{NSE} \cdot \omega$$

and $t_{NSE} = \omega_L \cdot \ell \cdot \hbar / (mv^3)$

neutron spin echo spectroscopy



$$P_{NSE} = P_s \langle \cos(\phi - \langle \phi \rangle) \rangle = P_s \frac{\int S(Q, \omega) \cos[t(\omega - \omega_0)] d\omega}{\int S(Q, \omega) d\omega}$$

for quasi-elastic scattering $\omega_0 = 0$

$$P_{NSE}^{scat} / P_s = \Re [S(Q, t)] / S(Q) = I(Q, t)$$

most generally $\phi - \langle \phi \rangle = f(\vec{q}, \omega) \propto S(\vec{Q}, t)$
 locally

- **Magnetic scattering**
- **Paramagnetic NSE**
- **Ferromagnetic NSE: magnetic fields**
- **Intensity modulated NSE: for samples depolarising the neutron beam: ferromagnets, superconductors**
- **Polarimetric NSE: chirality**

The vector interaction of a polarised neutron beam with magnetic moments

$$S_m(\vec{Q}, \omega) = (\gamma\rho_o)^2 \frac{k_f}{k_i} \left[\sum_{q_i, q_f} p_{q_i} \left[\langle q_i | m_{\perp}^* | q_f \rangle \cdot \langle q_f | m_{\perp} | q_i \rangle \right] \delta(E_f - E_i + \hbar\omega) \right]$$

for an unpolarised beam

$$S_m(\vec{Q}, \omega) = S_m^o(\vec{Q}, \omega)$$

Blume-Maleev equations: magnetic part

The vector interaction of a polarised neutron beam with magnetic moments

$$S_m(\vec{Q}, \omega) = (\gamma\rho_o)^2 \frac{k_f}{k_i} \left[\sum_{q_i, q_f} i \vec{P}_i \cdot (\langle q_i | m_{\perp}^* | q_f \rangle \times \langle q_f | m_{\perp} | q_i \rangle) \right] \delta(E_f - E_i + h\omega)$$

the polarisation dependent term:

$$S_m(\vec{Q}, \omega) = S_m^o(\vec{Q}, \omega) - \eta \zeta \vec{P}_i \cdot \hat{Q}$$

$$\eta = \begin{array}{l} 1 \text{ totally chiral} \\ 0 \text{ non-chiral} \end{array}$$

$$\zeta = \begin{array}{l} +1 \text{ right handed} \\ -1 \text{ left handed} \end{array}$$

The vector interaction of a polarised neutron beam with magnetic moments

$$S_m(\vec{Q}, \omega) = (\gamma\rho_o)^2 \frac{k_f}{k_i} \left[\sum_{q_i, q_f} p_{q_i} \left[\langle q_i | m_{\perp}^* | q_f \rangle \cdot \langle q_f | m_{\perp} | q_i \rangle + i \vec{P}_i \cdot \left(\langle q_i | m_{\perp}^* | q_f \rangle \times \langle q_f | m_{\perp} | q_i \rangle \right) \right] \right] \delta(E_f - E_i + h\omega)$$

$$S_m(\vec{Q}, \omega) = S_m^o(\vec{Q}, \omega) (1 - \eta) (\zeta \vec{P}_i \cdot \hat{Q})$$

$$\eta = \begin{array}{l} 1 \text{ totally chiral} \\ 0 \text{ non-chiral} \end{array}$$

$$\zeta = \begin{array}{l} +1 \text{ right handed} \\ -1 \text{ left handed} \end{array}$$

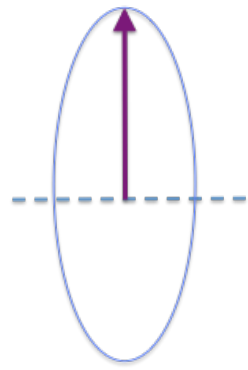
The vector interaction of a polarised neutron beam with magnetic moments

$$S_m(\vec{Q}, \omega) = (\gamma\rho_o)^2 \frac{k_f}{k_i} \left[\sum_{q_i, q_f} p_{q_i} \left[\langle q_i | m_{\perp}^* | q_f \rangle \cdot \langle q_f | m_{\perp} | q_i \rangle + i \vec{P}_i \cdot \left(\langle q_i | m_{\perp}^* | q_f \rangle \times \langle q_f | m_{\perp} | q_i \rangle \right) \right] \right] \delta(E_f - E_i + h\omega)$$

$$S_m(\vec{Q}, \omega) = S_m^o(\vec{Q}, \omega) (1 - \eta \zeta \vec{P}_i \cdot \hat{Q})$$

$$\vec{P}_f = -\hat{Q} \left[\hat{Q} \cdot \vec{P}_i + \zeta \eta \right]$$

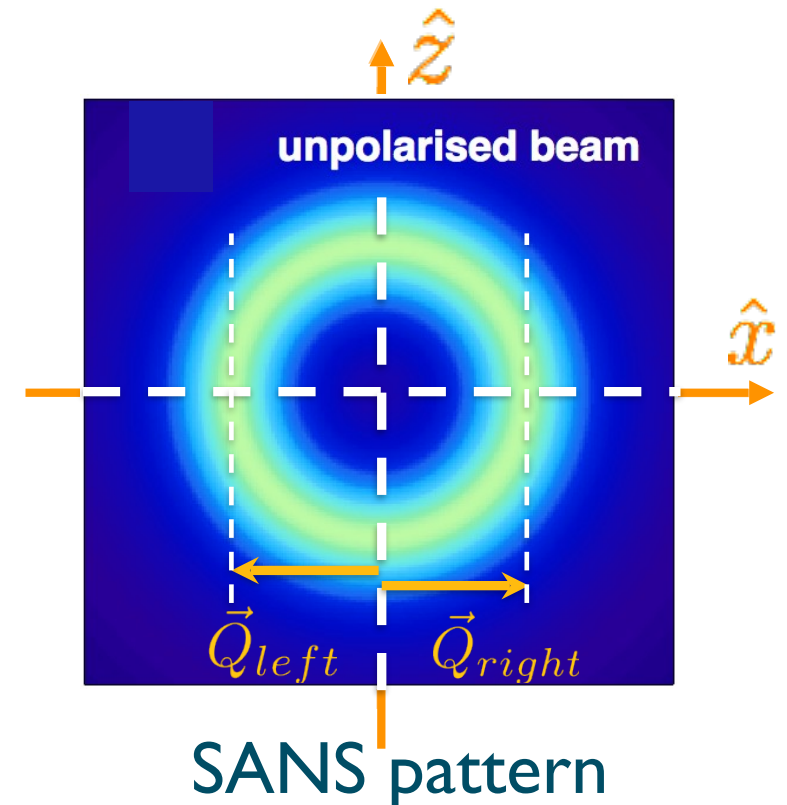
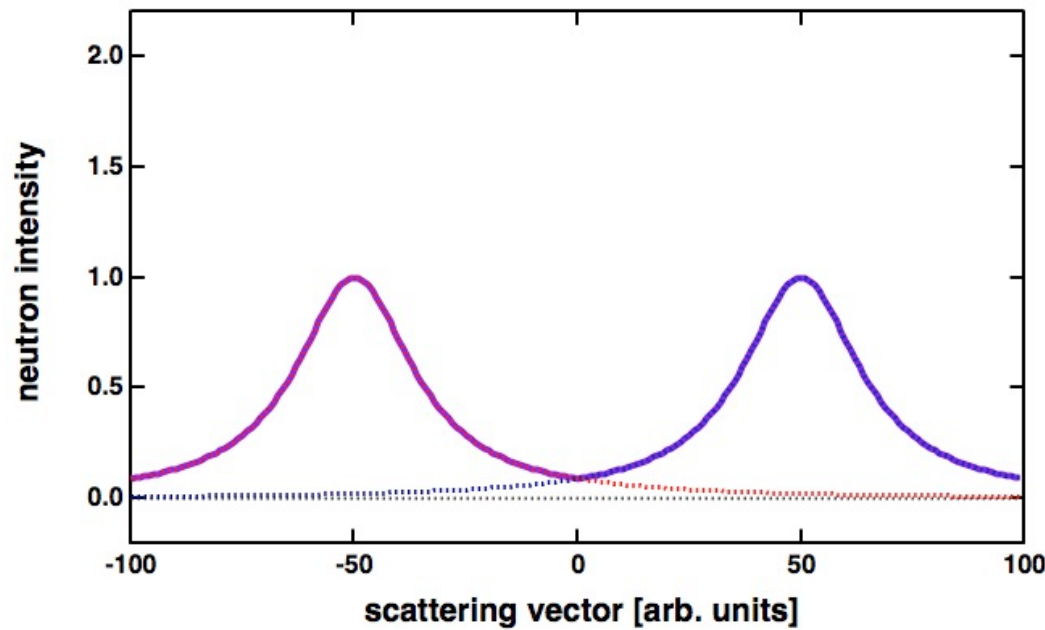
The interaction of a neutron beam with magnetic moments



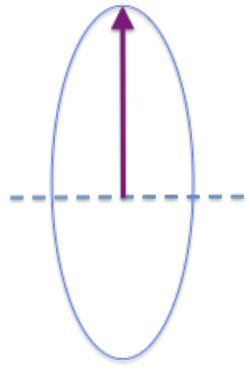
$$S_m(\vec{Q}, \omega) = S_m^o(\vec{Q}, \omega)(1 - \eta \zeta \vec{P}_i \cdot \hat{Q})$$

$\phi = 90^\circ \quad \eta = 1$

unpoloarised neutron beam



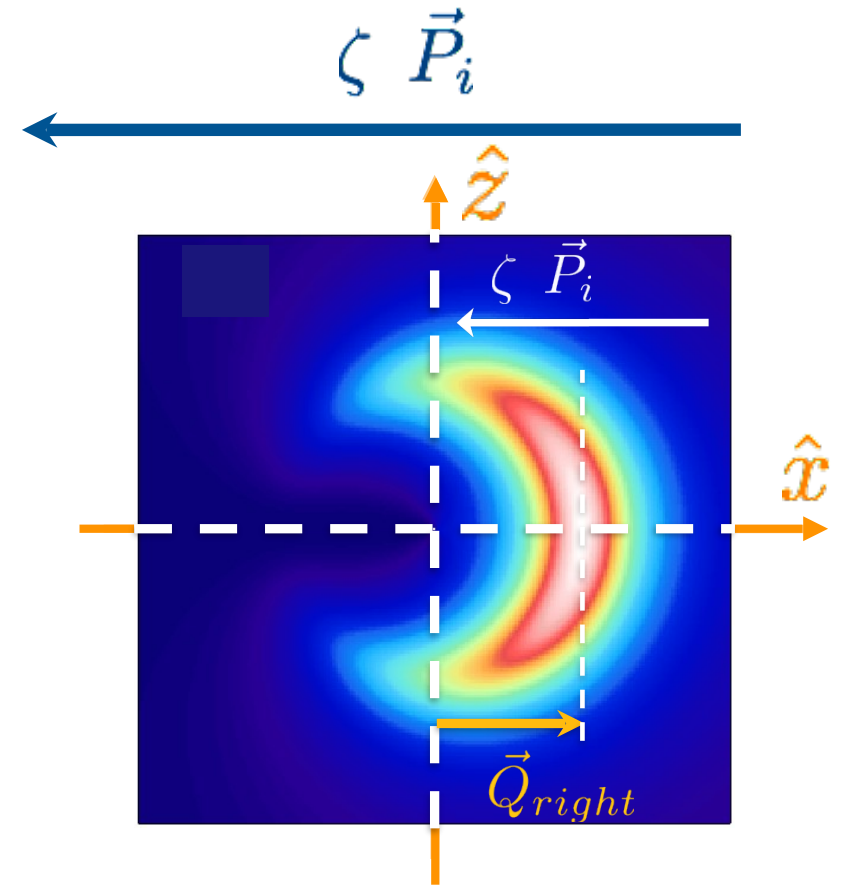
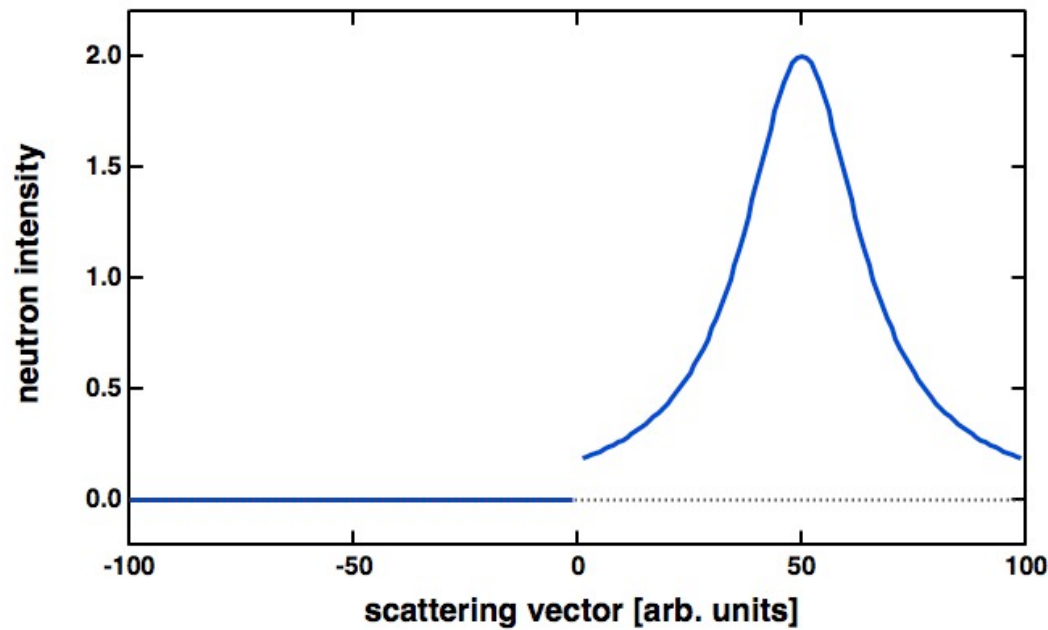
The interaction of a neutron beam with magnetic moments



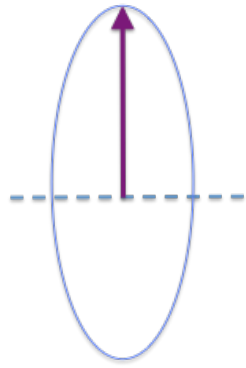
$$\phi = 90^\circ \quad \eta = 1$$

polarised neutrons

$$S_m(\vec{Q}, \omega) = S_m^o(\vec{Q}, \omega)(1 - \eta \zeta \vec{P}_i \cdot \hat{Q})$$



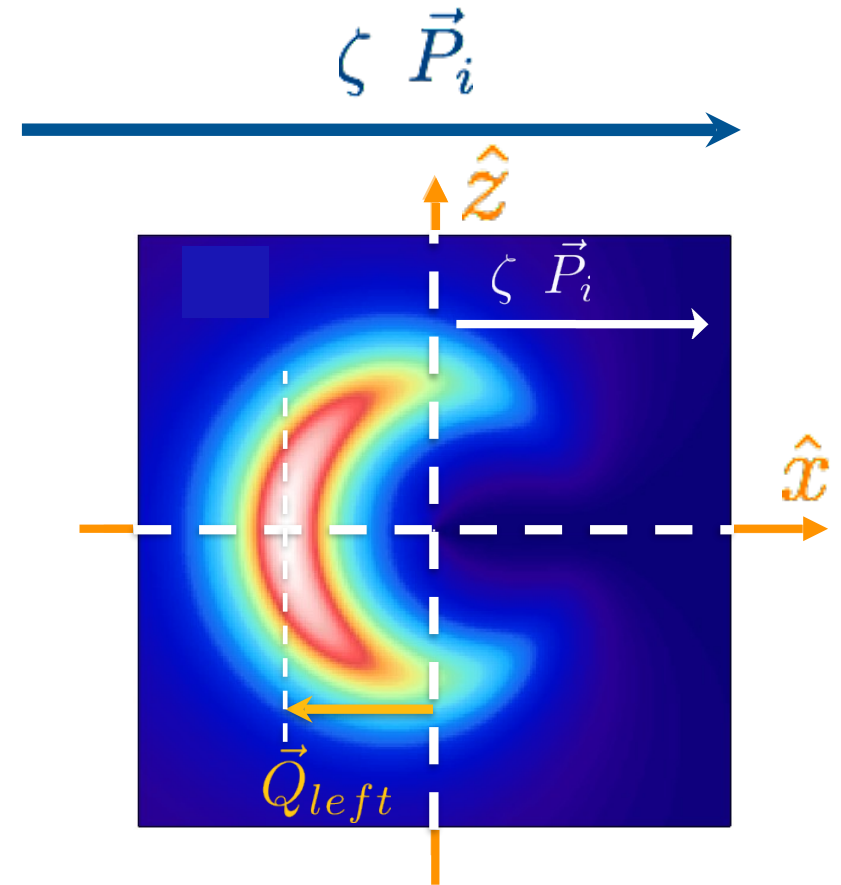
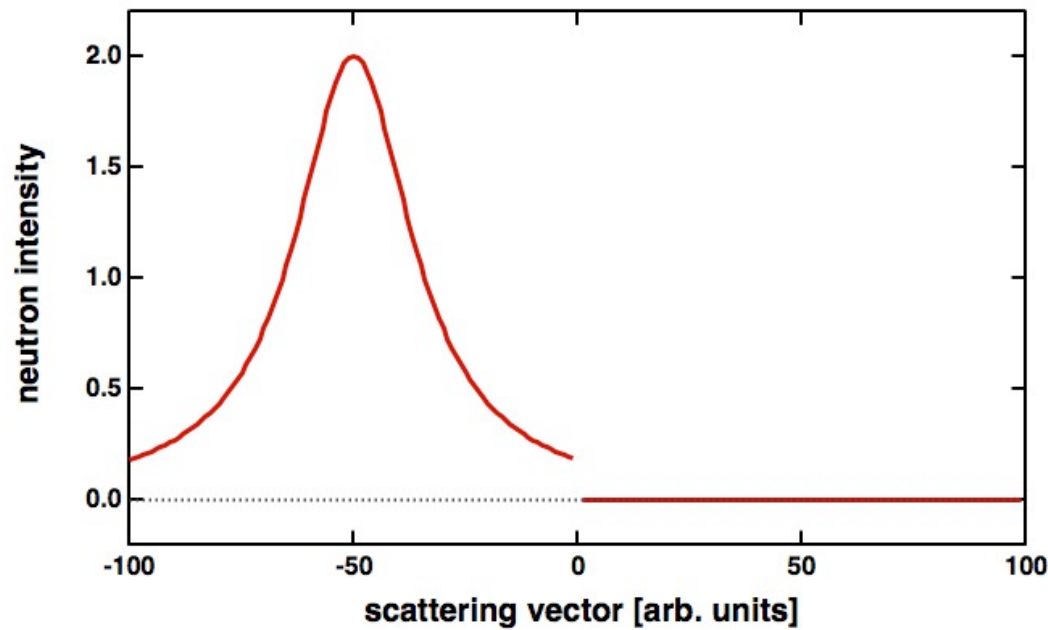
The interaction of a neutron beam with magnetic moments



$$\phi = 90^\circ \quad \eta = 1$$

polarised neutrons

$$S_m(\vec{Q}, \omega) = S_m^o(\vec{Q}, \omega)(1 - \eta \zeta \vec{P}_i \cdot \hat{Q})$$



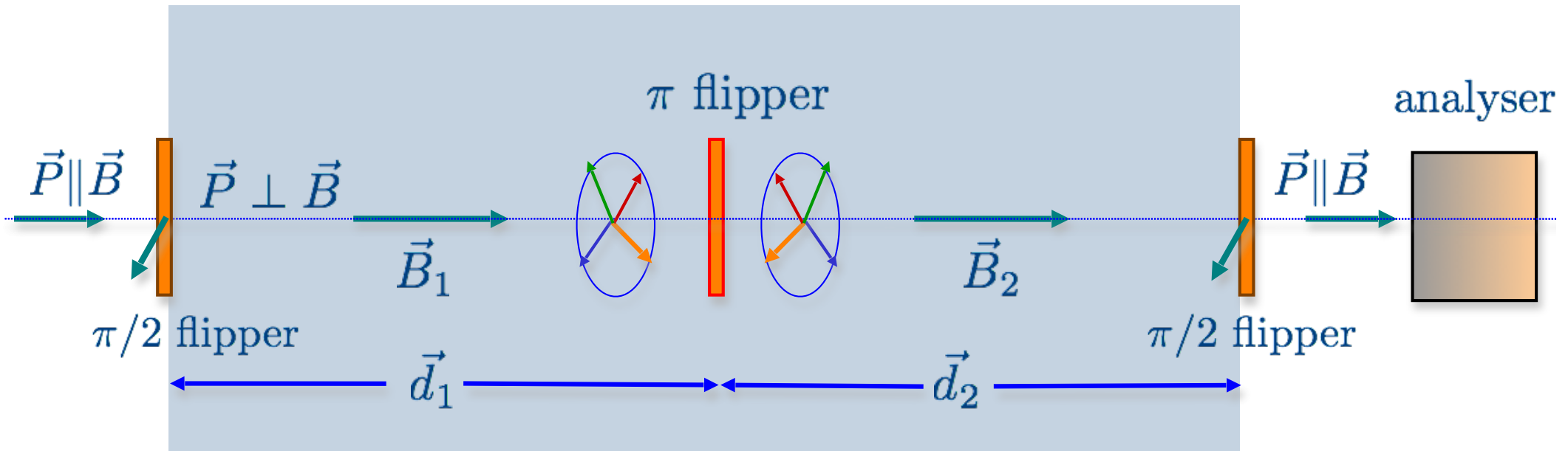
the vector interaction of a polarised neutron beam with magnetic moments provides direct information on the topology of the magnetic moments

if the topology of the magnetic moments is known

the vector interaction of a polarised neutron beam with magnetic moments provides direct information on the topology of the neutron magnetic moments

- Magnetic scattering
- Paramagnetic NSE
- Ferromagnetic NSE: magnetic fields
- Intensity modulated NSE: for samples depolarising the neutron beam: ferromagnets, superconductors
- Polarimetric NSE: chirality

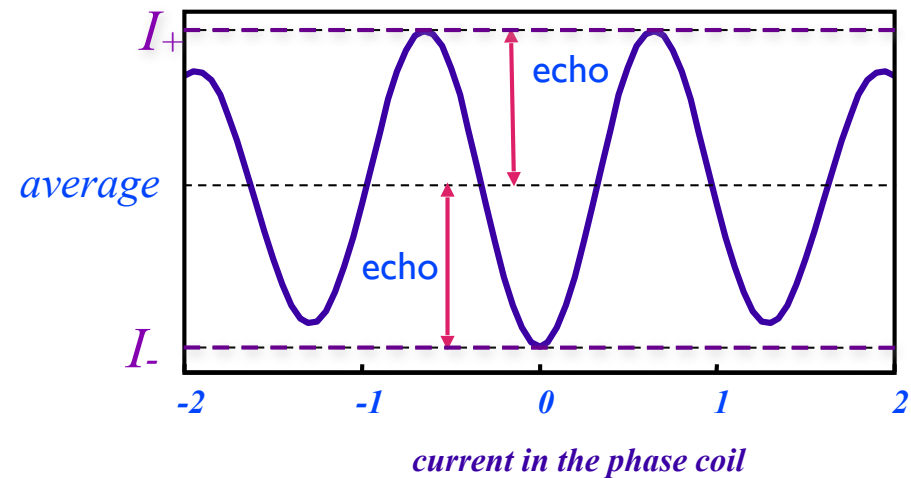
neutron spin echo spectroscopy



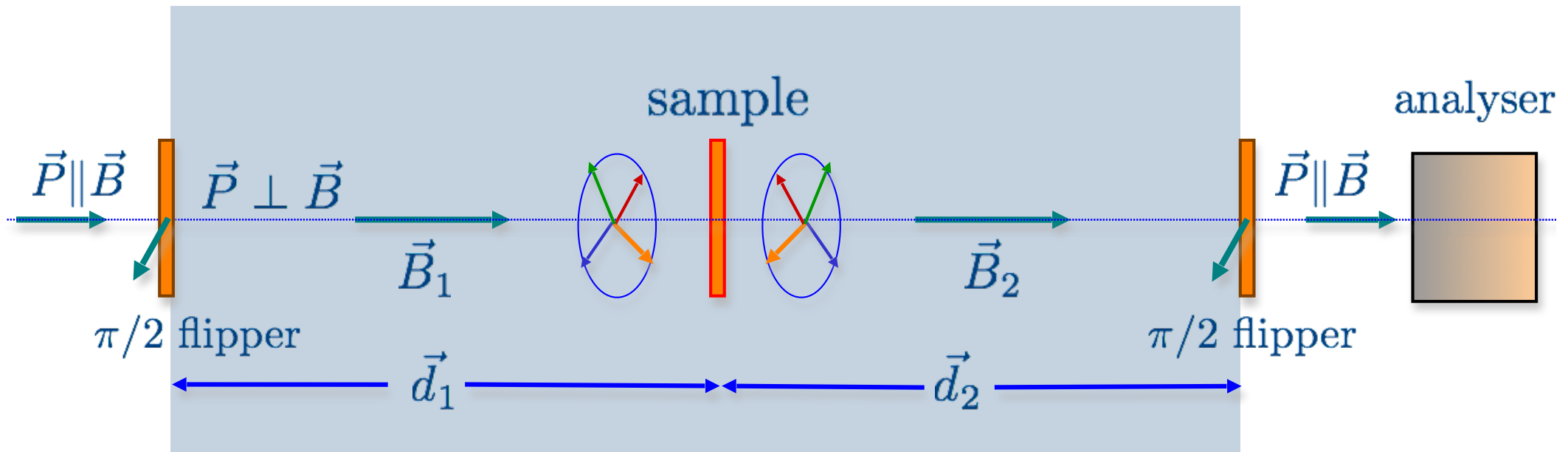
ideally

$$\text{echo modulation} = (I_+ - I_-) / 2$$

$$\text{for } |\vec{P}| = 1$$



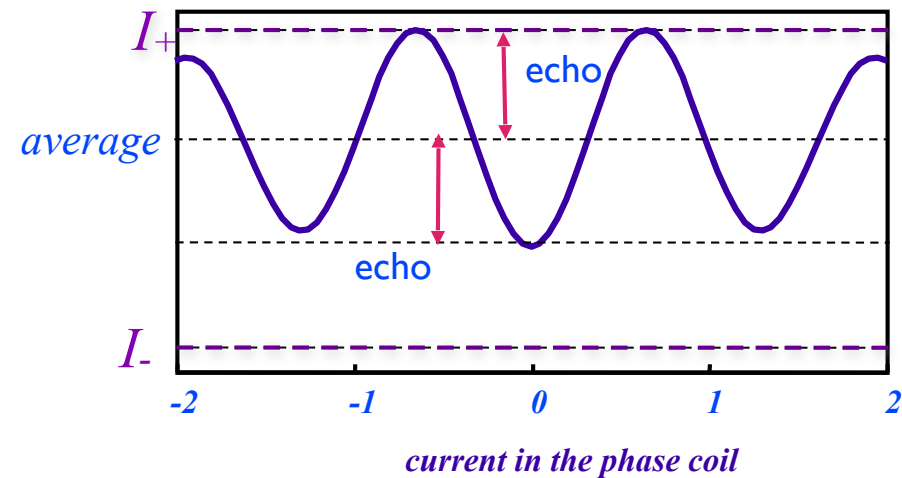
paramagnetic neutron spin echo spectroscopy



ideally

$$\text{echo modulation} = (I_+ - I_-) / 3$$

$$\text{for } |\vec{P}| = 1$$



magnetic scattering : $\vec{P}_f = -\hat{Q} [\hat{Q} \cdot \vec{P}_i + \zeta \eta]$

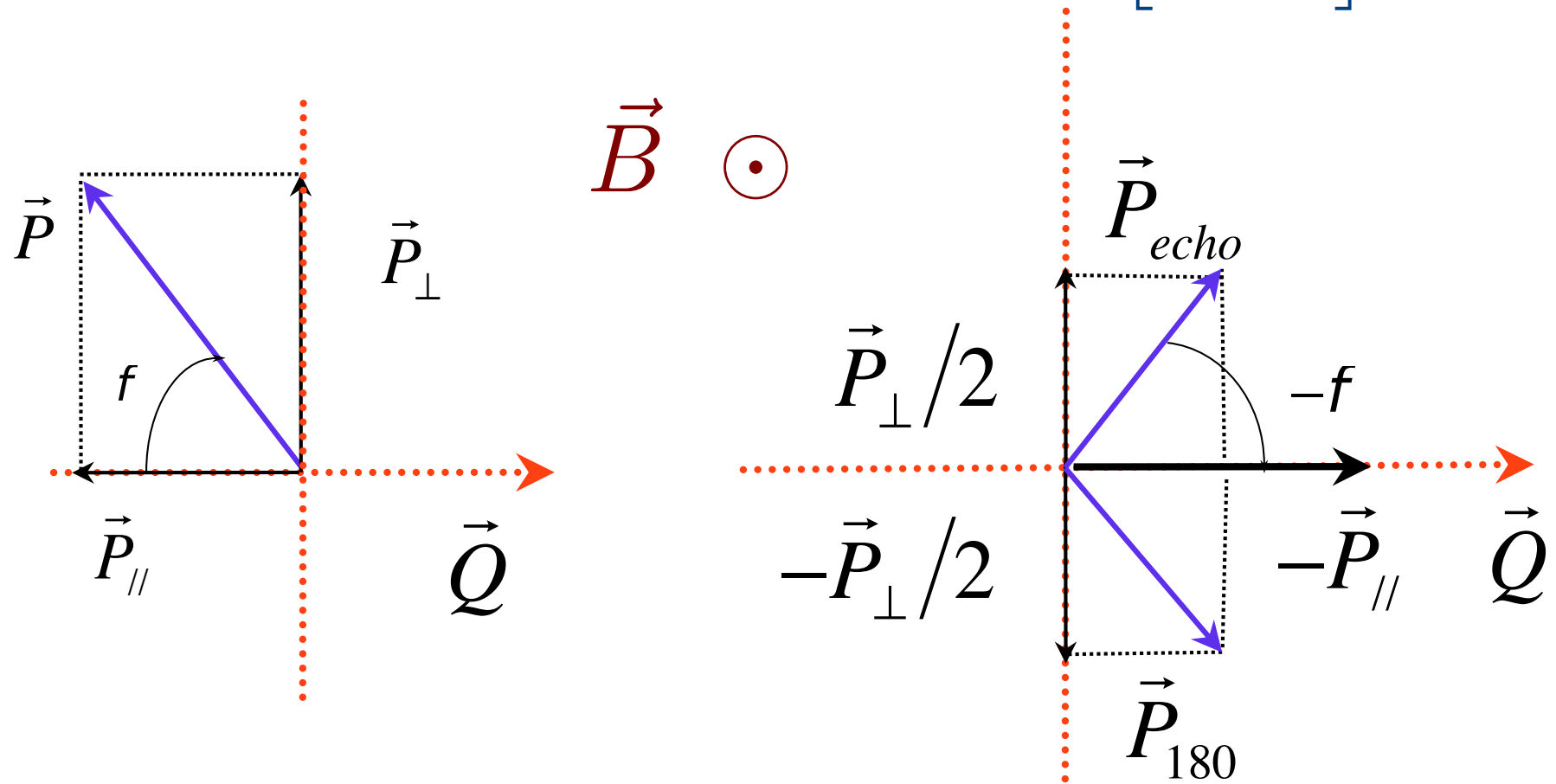
paramagnetic scattering : $\vec{P}_f = -\hat{Q} [\hat{Q} \cdot \vec{P}_i]$

$\Rightarrow \hat{Q}$ is of crucial importance

	paramagnetic scattering	chiral magnetic scattering
$\vec{P}_i \parallel \hat{Q}$		
$\vec{P}_i \perp \hat{Q}$		

magnetic scattering : $\vec{P}_f = -\hat{Q} \left[\hat{Q} \cdot \vec{P}_i + \zeta \eta \right]$

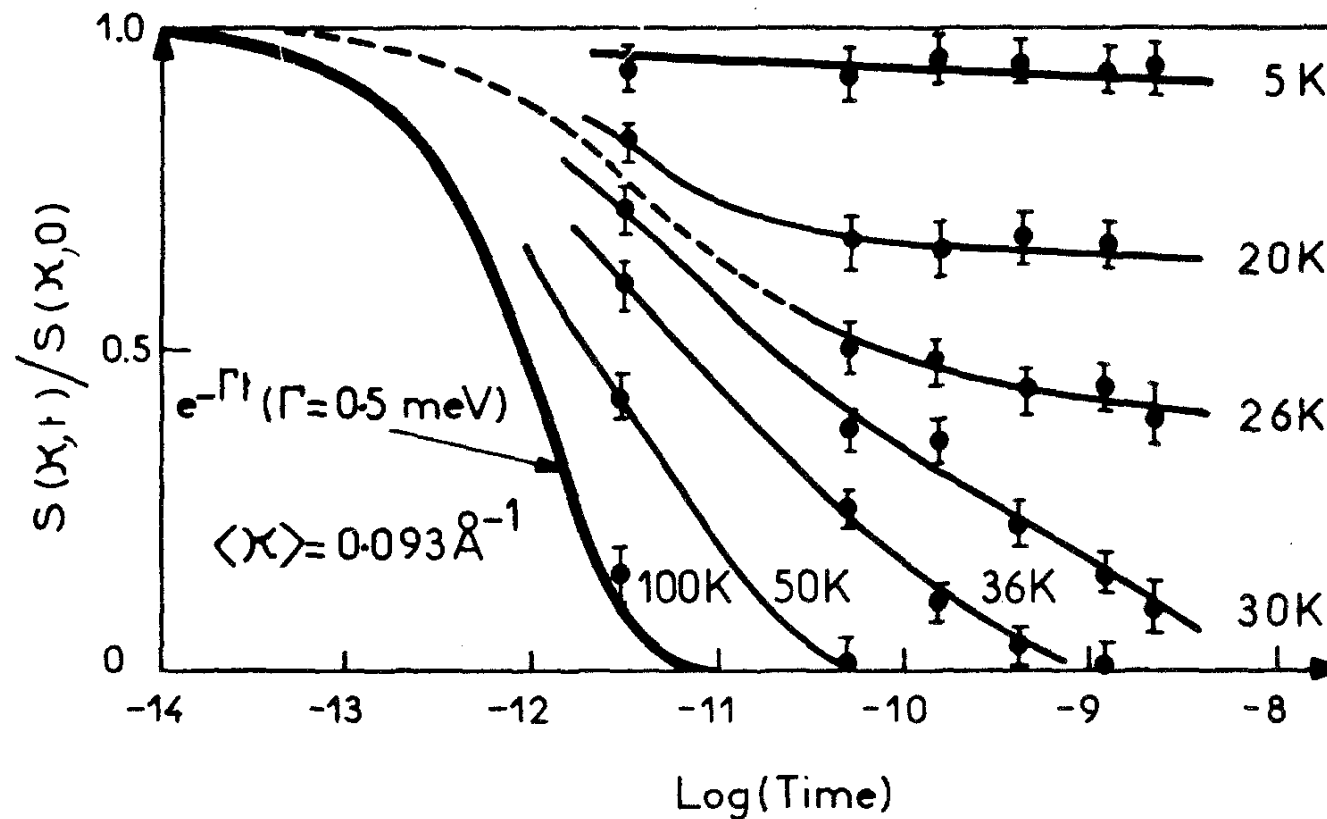
paramagnetic scattering : $\vec{P}_f = -\hat{Q} \left[\hat{Q} \cdot \vec{P}_i \right]$



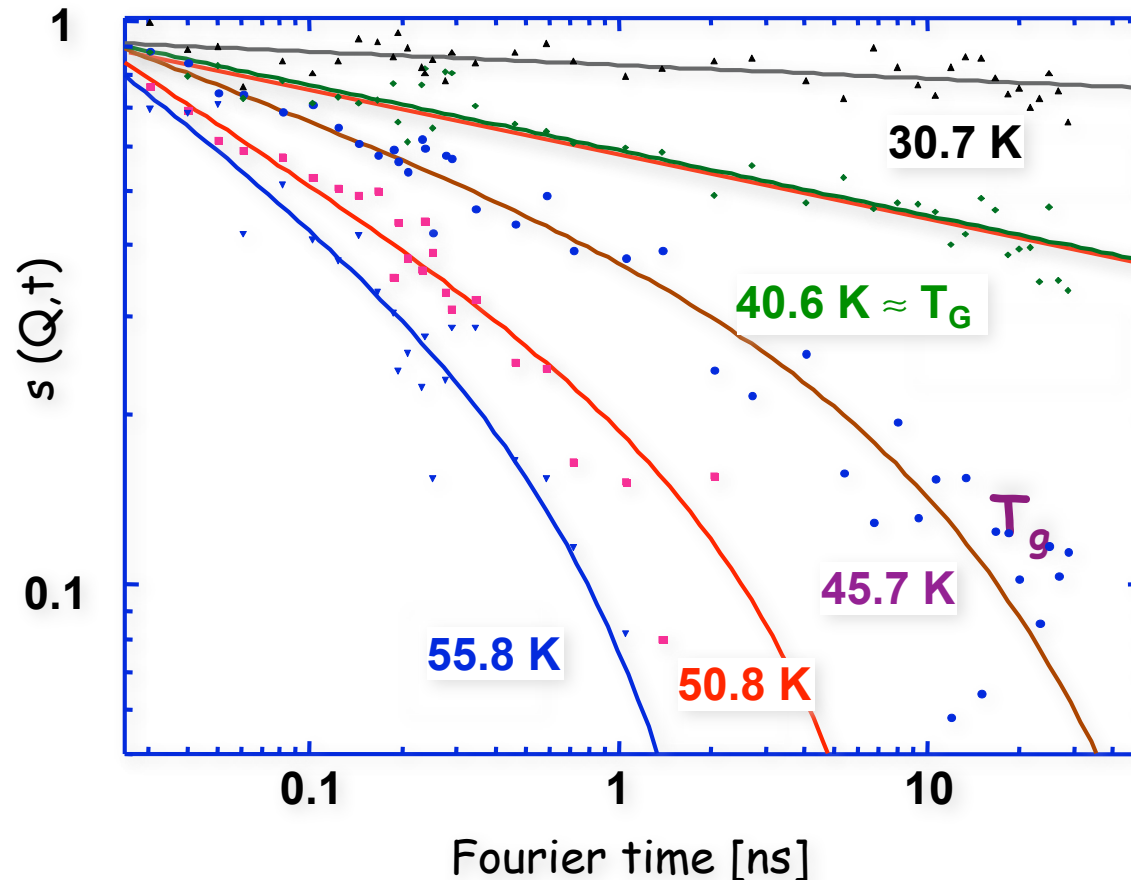
the π flipper is the sample

first direct observation of stretched exponential relaxation in glassy systems

CuMn 5%



more accurate measurements on AuFe 14% show deviations from the stretched exponential



$T < T_G$

$$q(t) \sim t^{-x}$$

dynamic scaling

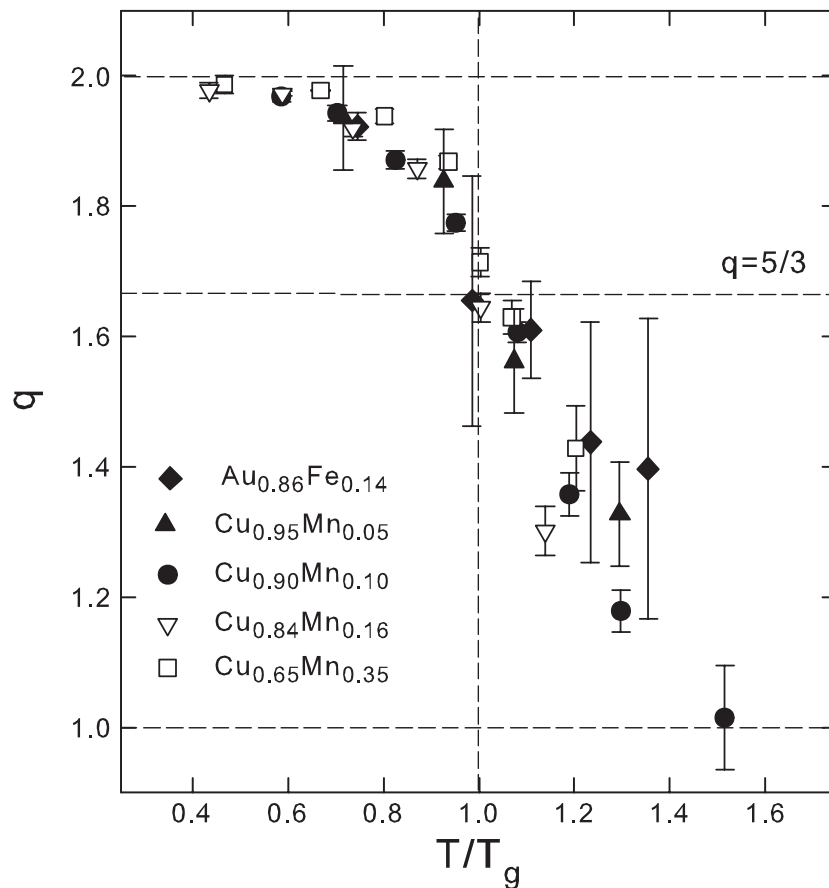
at T_g $q(t) \propto t^{-(d-2+\eta)/2z}$

$T > T_G$

$$q(t) \sim t^{-x} \exp(-t/\tau)^\beta$$

all relaxation functions of spin glasses follow the same universal function

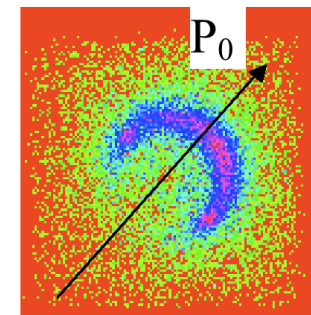
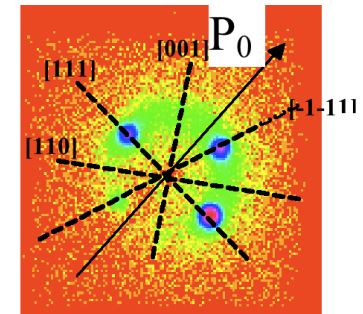
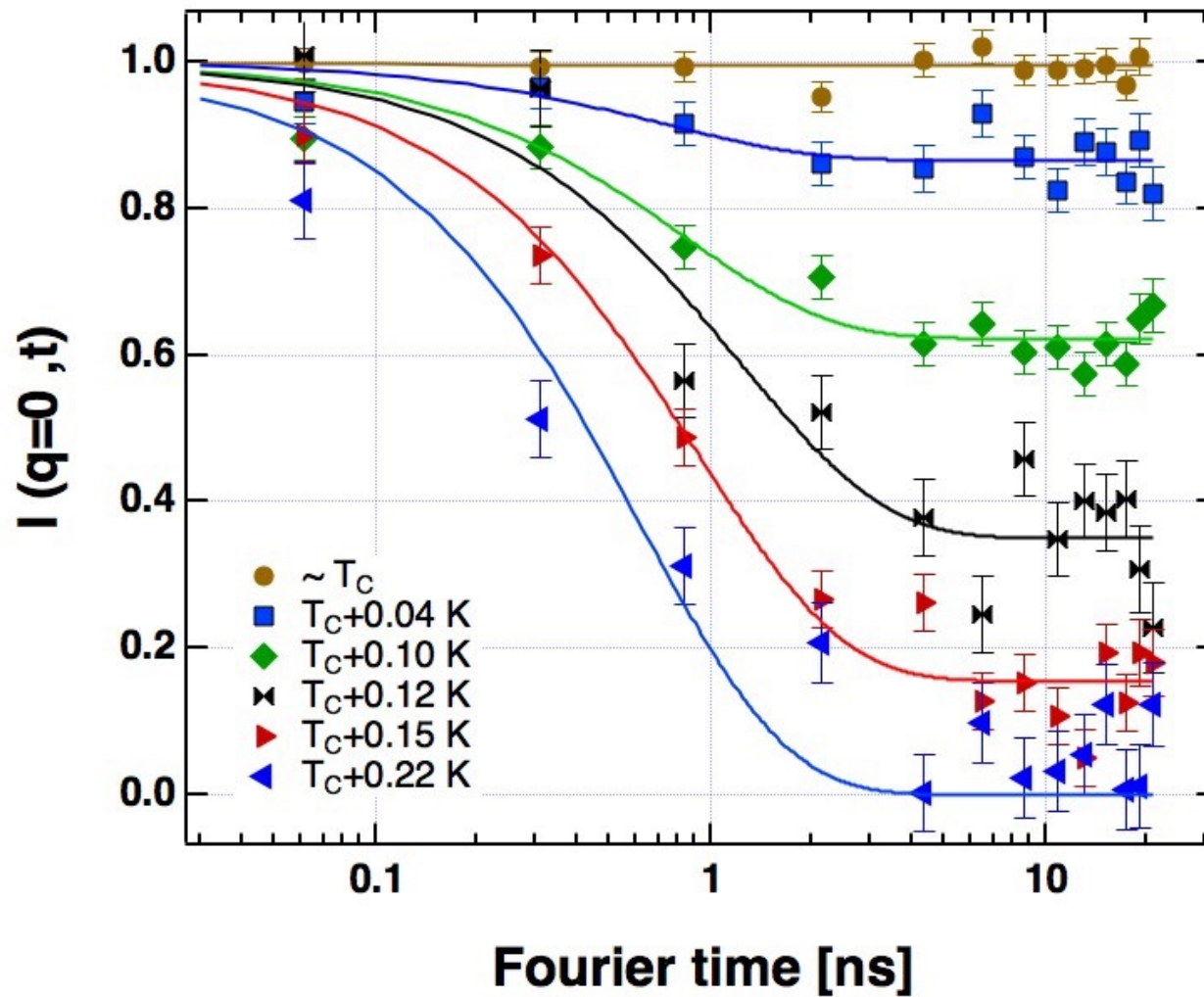
$$I(Q, t) = \left[1 + \left(\frac{q - 1}{2 - q} \right) \left(\frac{t}{\tau} \right) \right]^{(2-q)/(q-1)}$$



non extensive entropy breakdown
of Boltzmann
statistics at T_G

=> power law relaxation below T_G

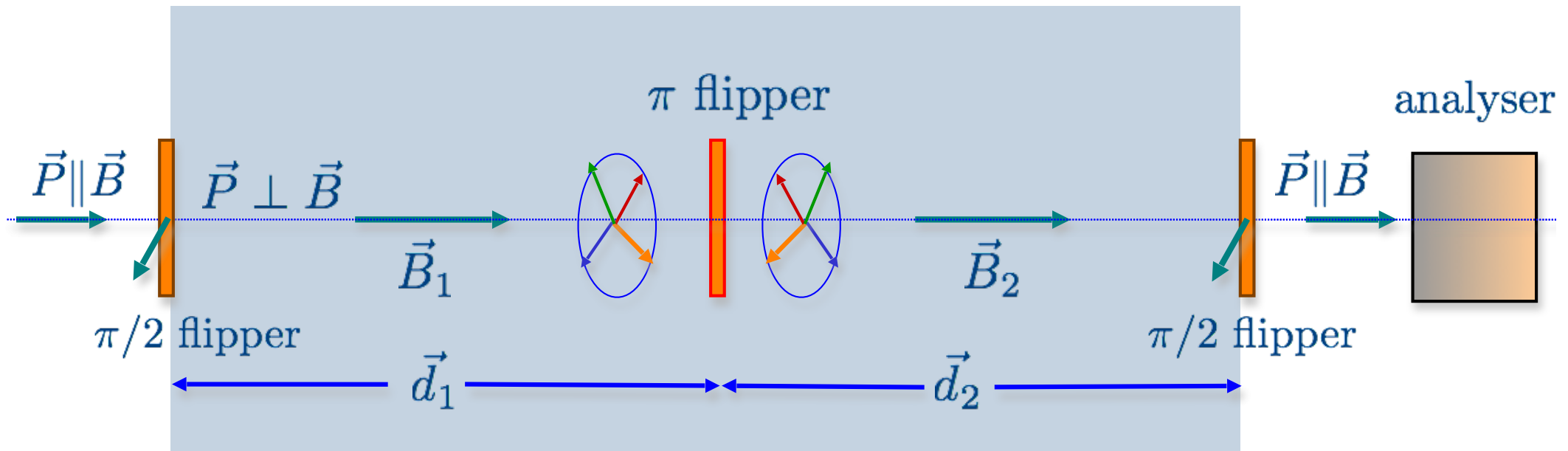
Paramagnetic NSE also works for chiral scattering the case of MnSi



after Grigoriev et al
PRB 2004

- Magnetic scattering
- Paramagnetic NSE
- **Ferromagnetic NSE: magnetic fields**
- Intensity modulated NSE: for samples depolarising the neutron beam: ferromagnets, superconductors
- Polarimetric NSE: chirality

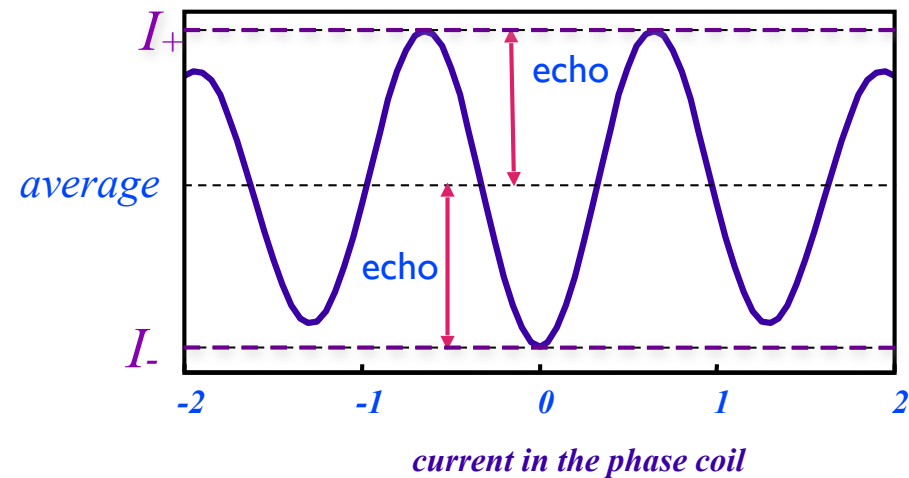
neutron spin echo spectroscopy



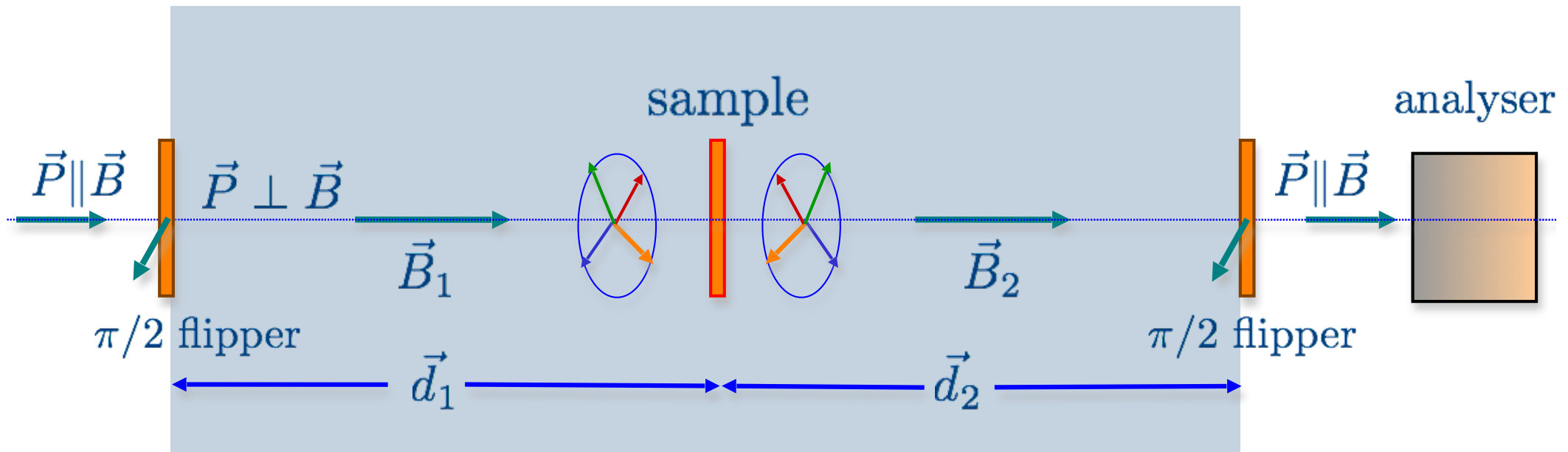
ideally

$$\text{echo modulation} = (I_+ - I_-) / 2$$

$$\text{for } |\vec{P}| = 1$$



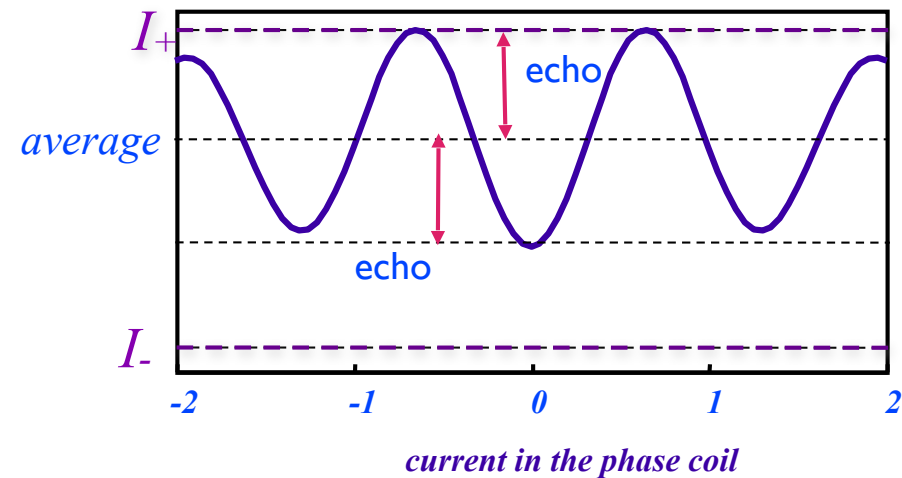
paramagnetic neutron spin echo spectroscopy



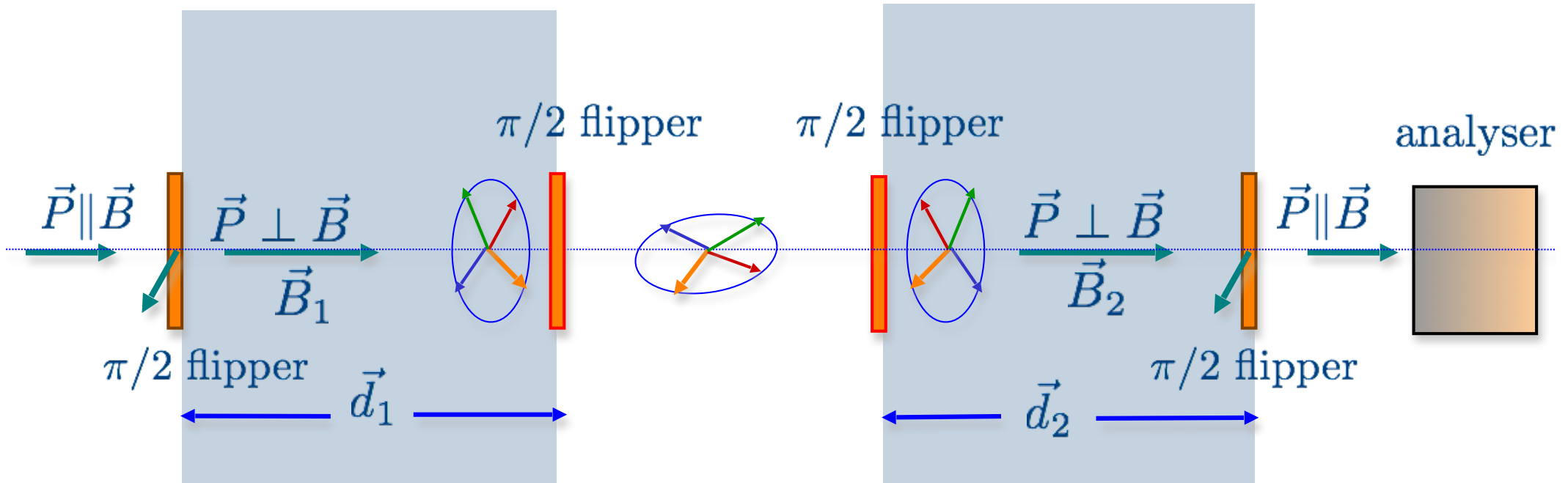
ideally

$$\text{echo modulation} = (I_+ - I_-) / 3$$

$$\text{for } |\vec{P}| = 1$$



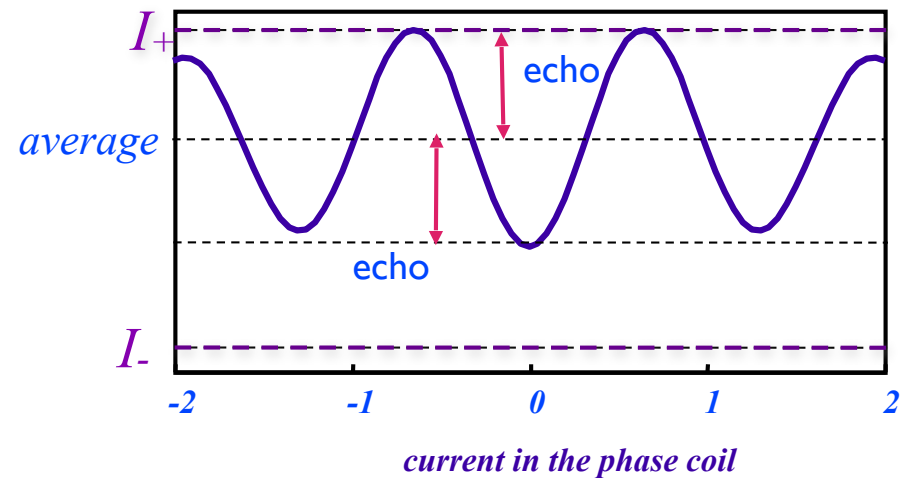
ferromagnetic neutron spin echo



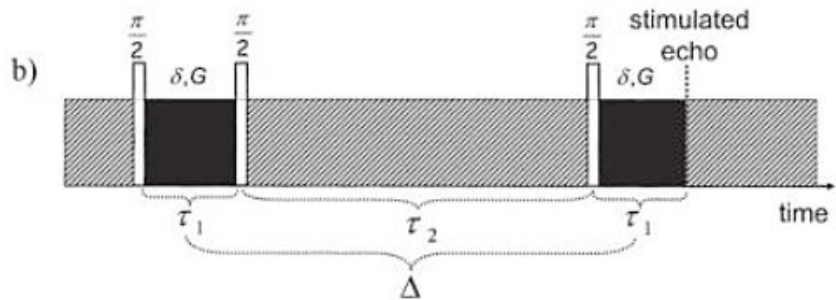
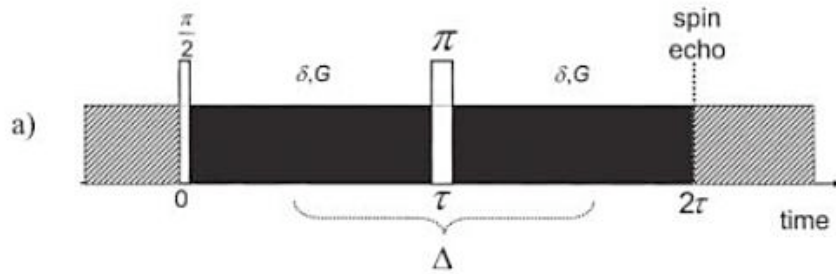
ideally

$$\text{echo modulation} = (I_+ - I_-) / 3$$

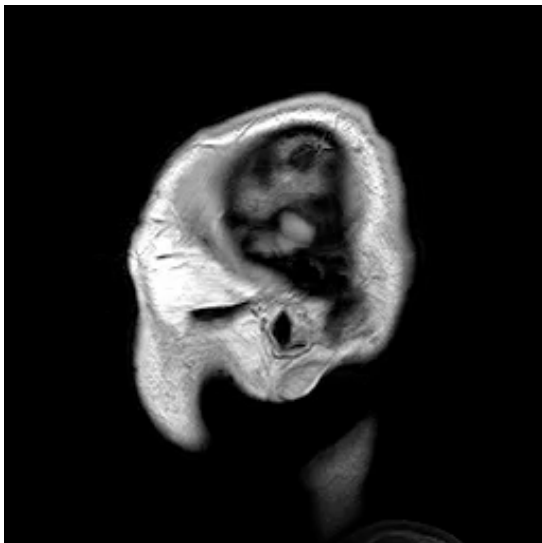
$$\text{for } |\vec{P}| = 1$$



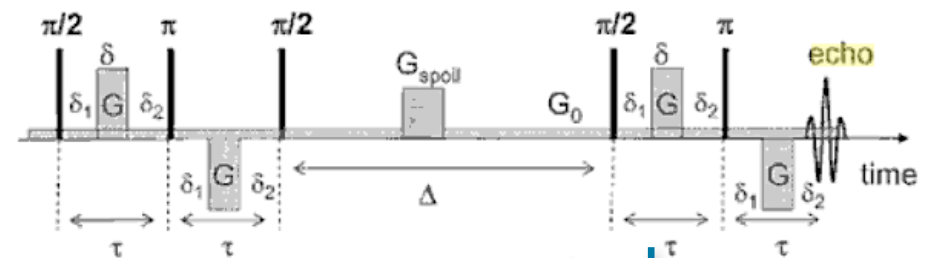
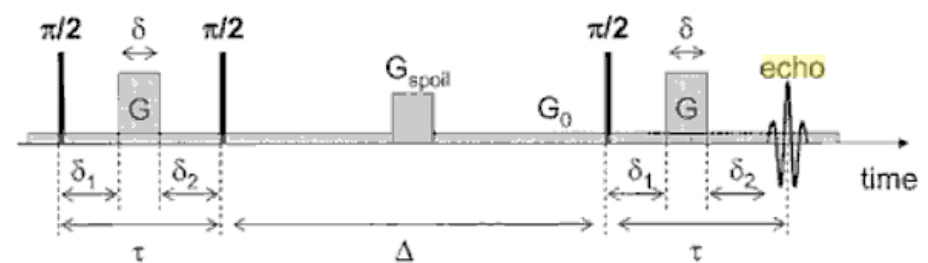
NMR spin echos



after Ardelean and Kimmich



pulsed field stimulated spin echo



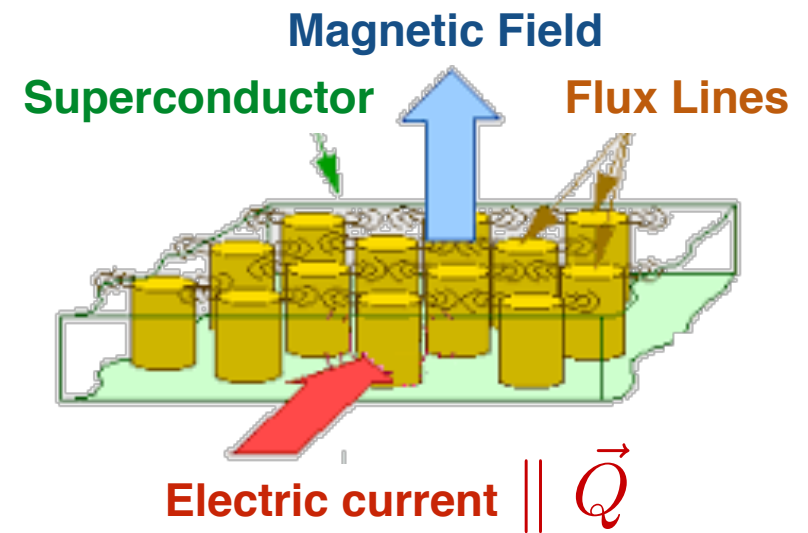
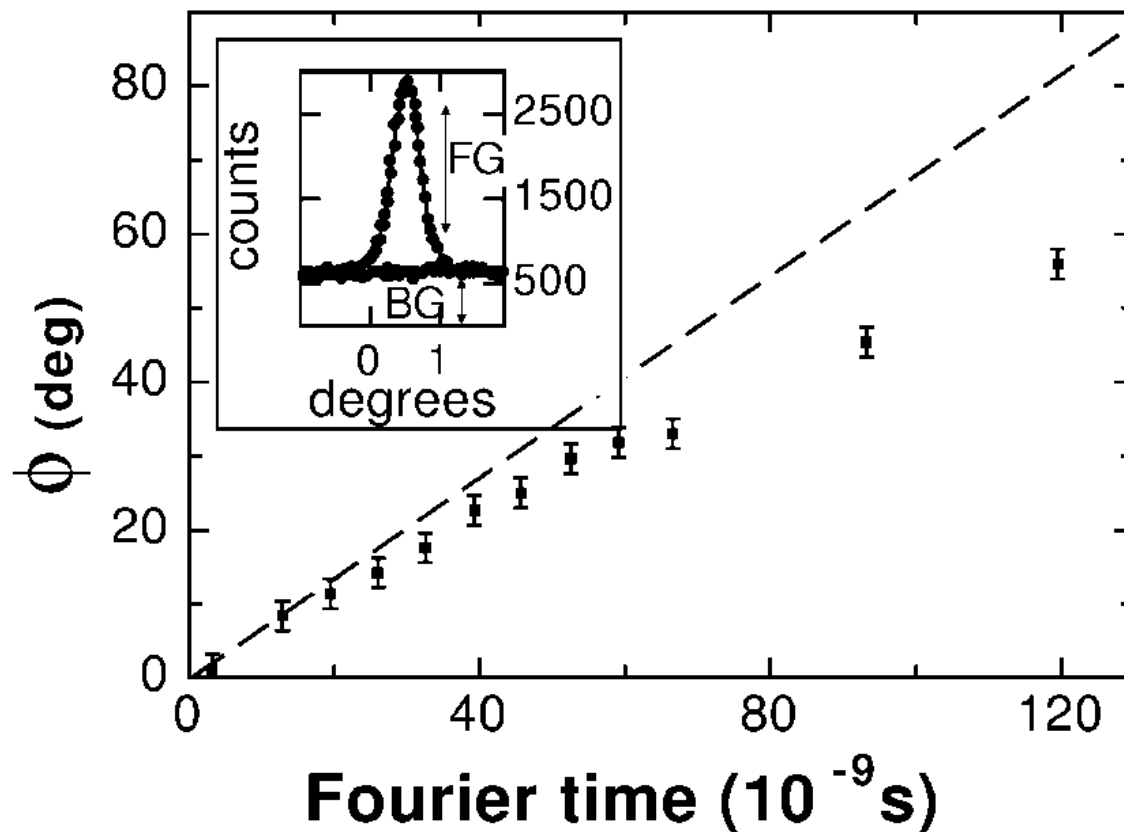
compensated pulsed field stimulated spin echo

Measurement of Vortex Motion in the Type-II Nb-Ta Superconductor

energy change of neutrons after diffraction by a moving Flux Line Lattice :

$$\omega = \hbar \vec{Q} \cdot \vec{v}_L \quad , \quad \phi = \omega t / \hbar \quad \Rightarrow \quad \phi = \vec{Q} \cdot \vec{v}_L t$$

Phase of the NSE group measured at 2.2 K, 0.3 T and 20 Å

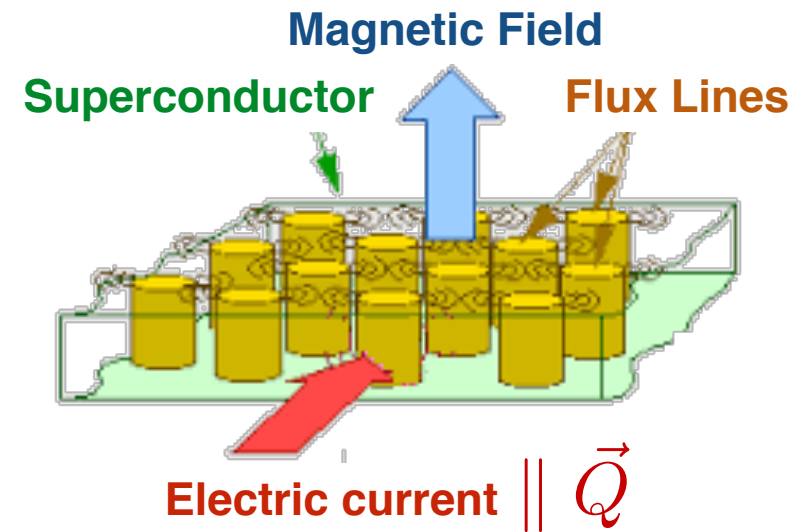
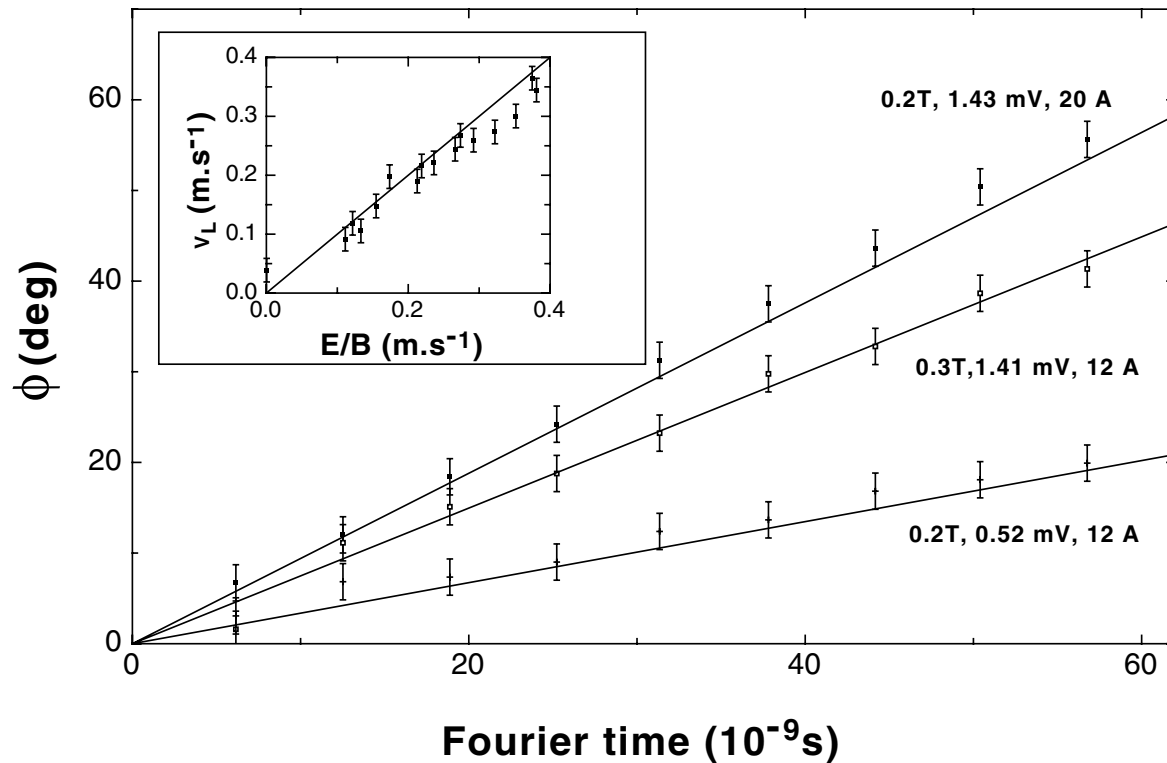


E.M. Forgan et al. PRL 2000

Measurement of Vortex Motion in the Type-II Nb-Ta Superconductor

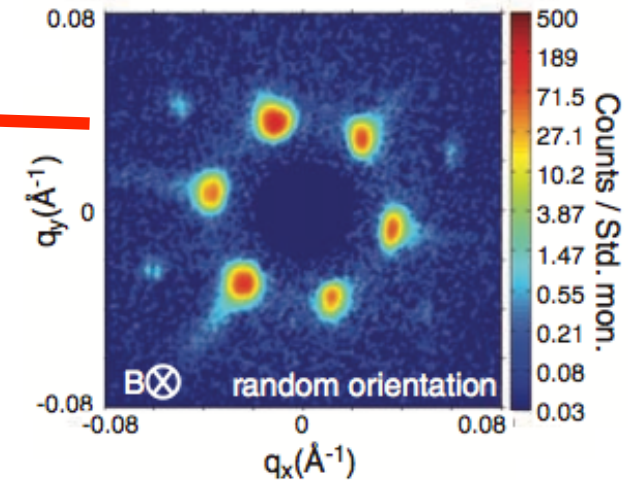
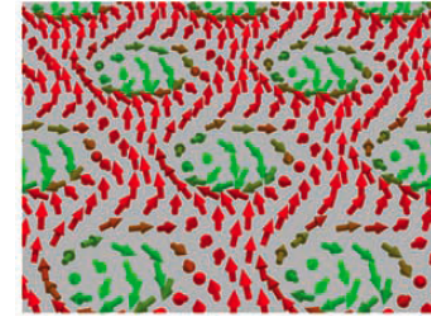
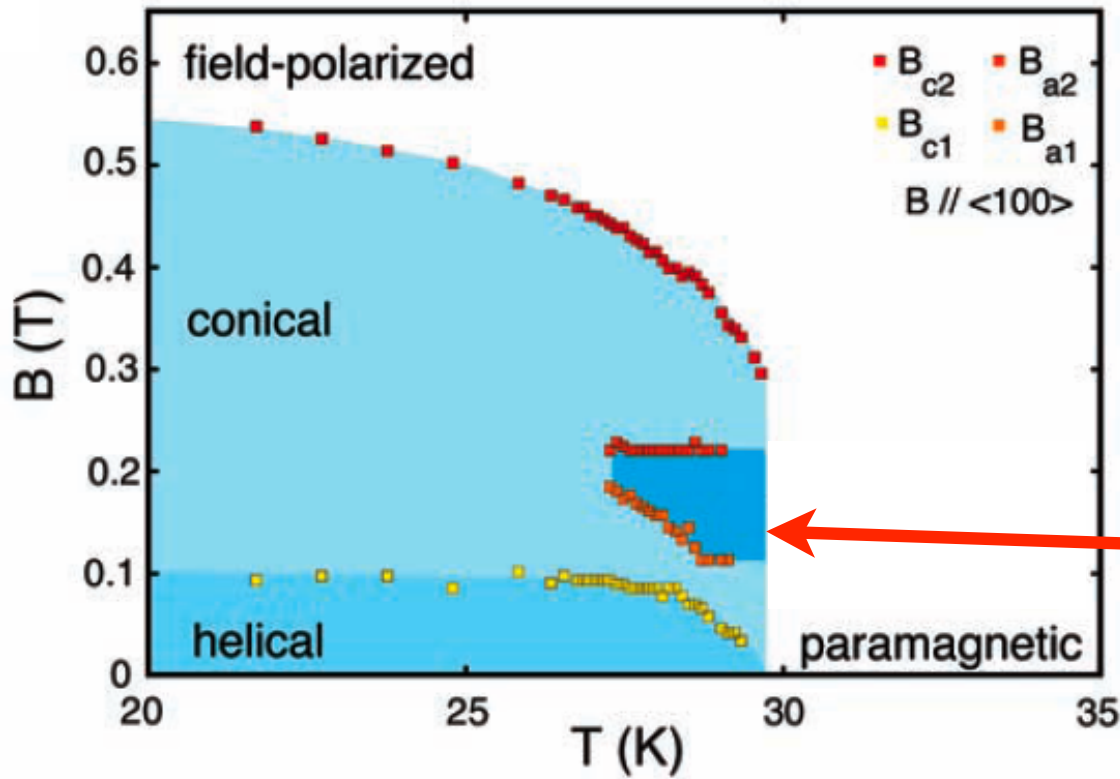
energy change of neutrons after diffraction by a moving Flux Line Lattice :

$$\epsilon = \hbar \vec{Q} \cdot \vec{v}_L \quad , \quad \phi = \epsilon t / \hbar \quad \Rightarrow \quad \phi = \vec{Q} \cdot \vec{v}_L t$$



E.M. Forgan et al. PRL 2000

.... and again the case of MnSi

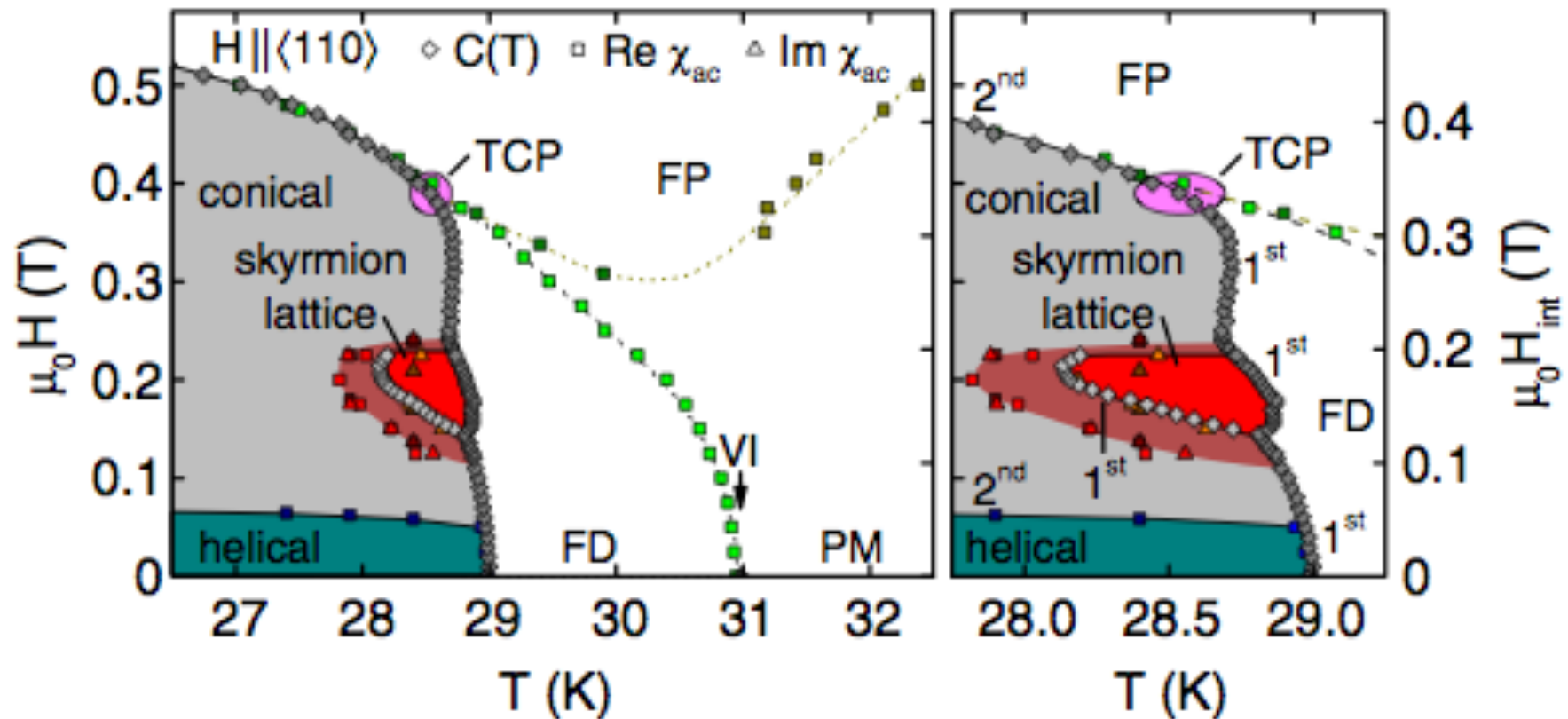


S. Mühlbauer et al., Science 2009

Phase diagram of MnSi

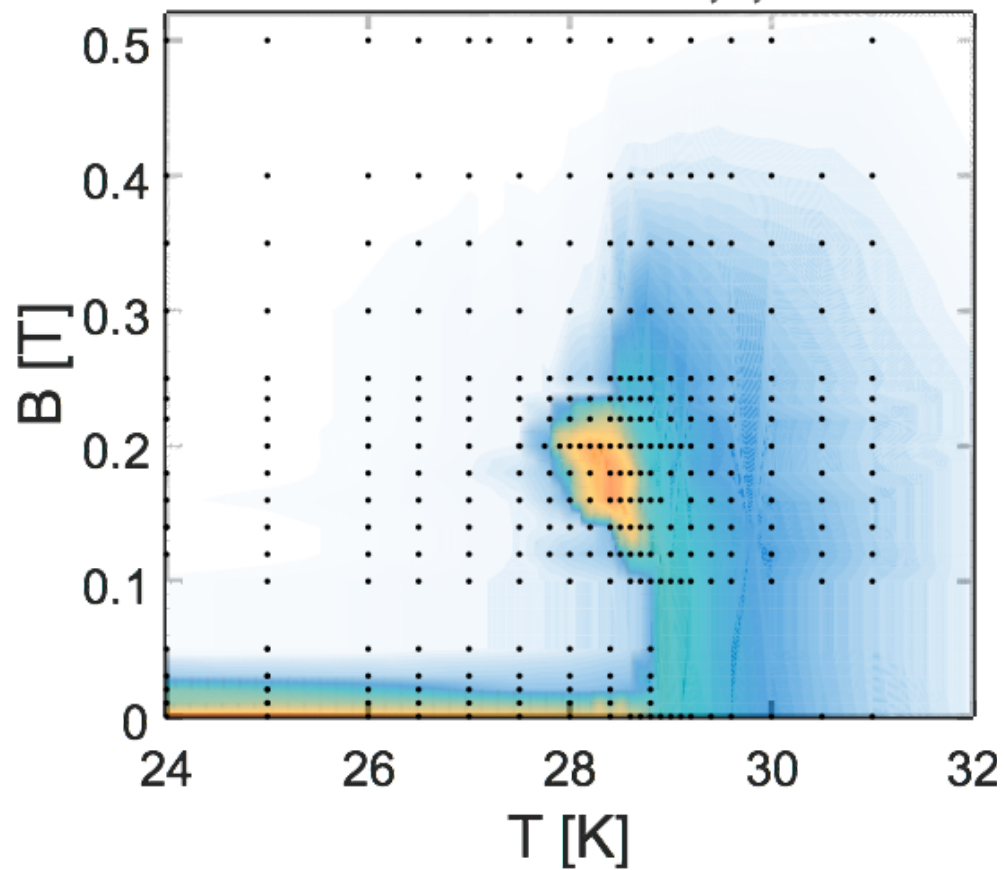
Hierarchy of energies – Bak and Jensen

existence of a TCP ? What are the implications ?

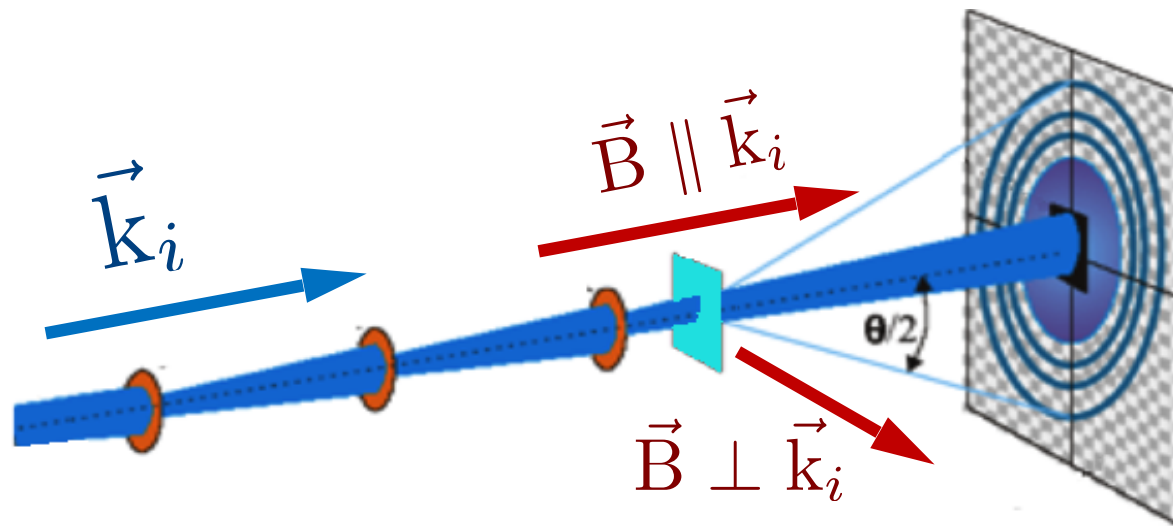
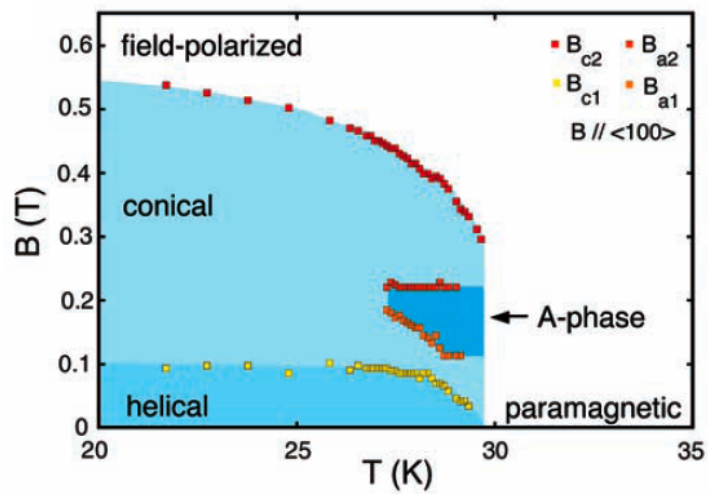
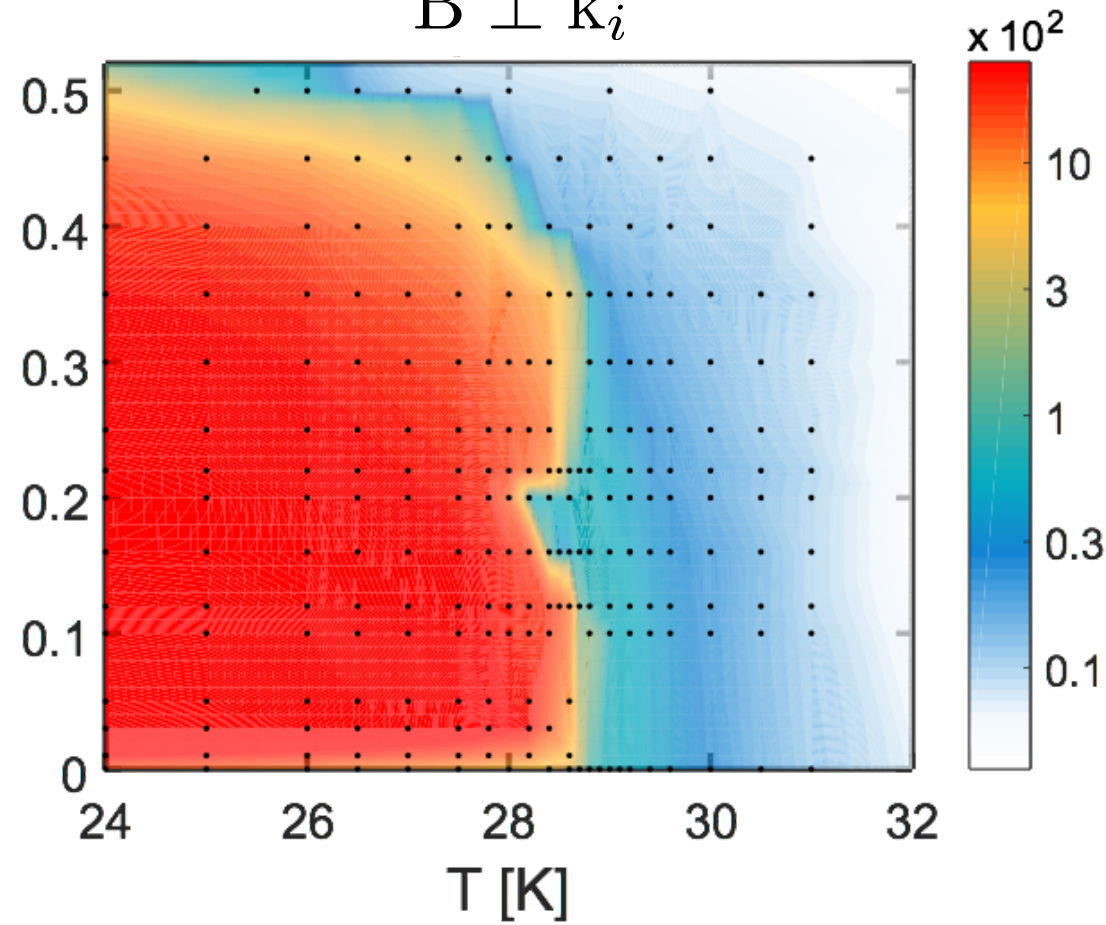


A. Bauer et al. PRL 110 (2013)

$$\vec{B} \parallel \vec{k}_i$$



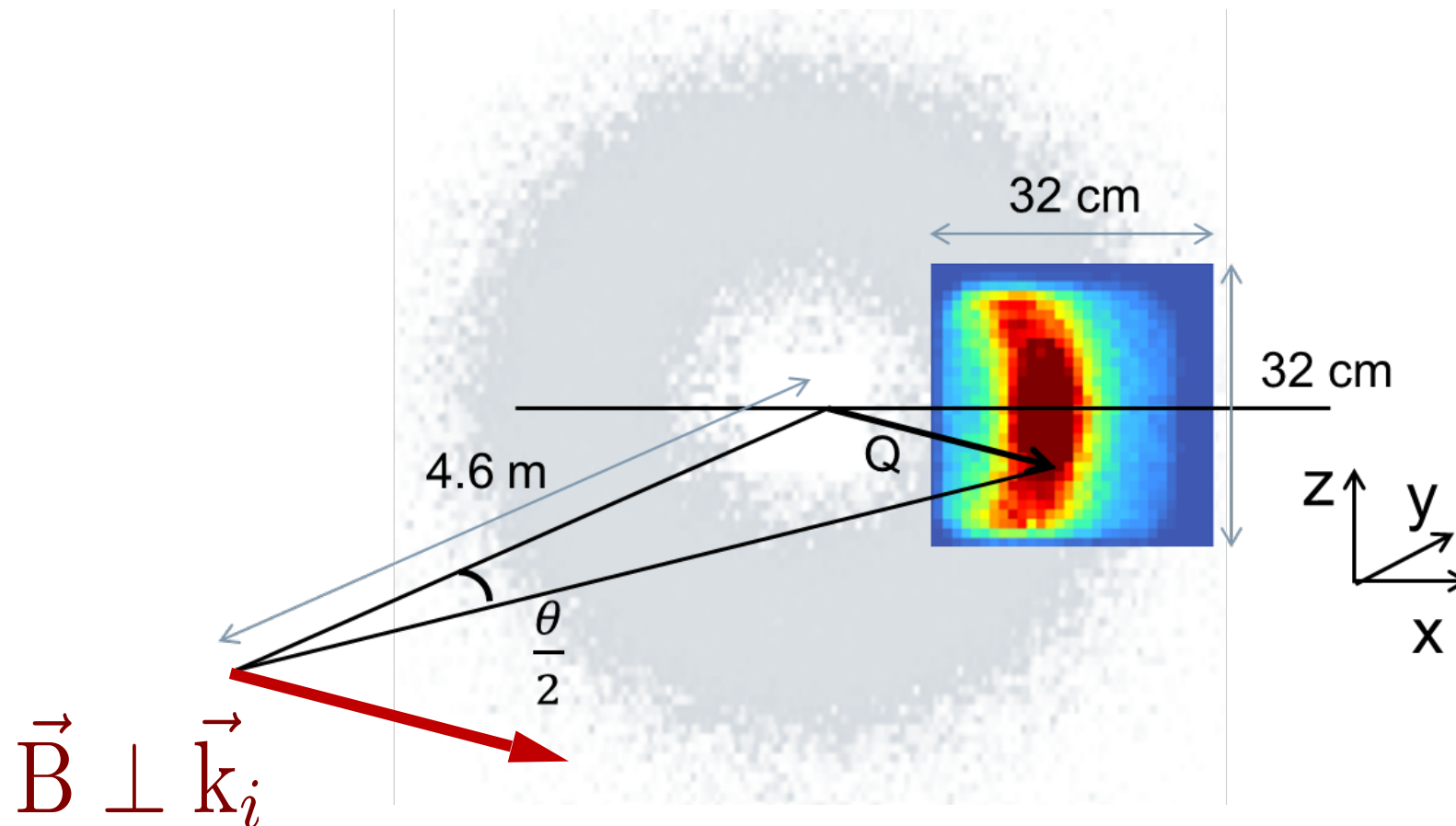
$$\vec{B} \perp \vec{k}_i$$



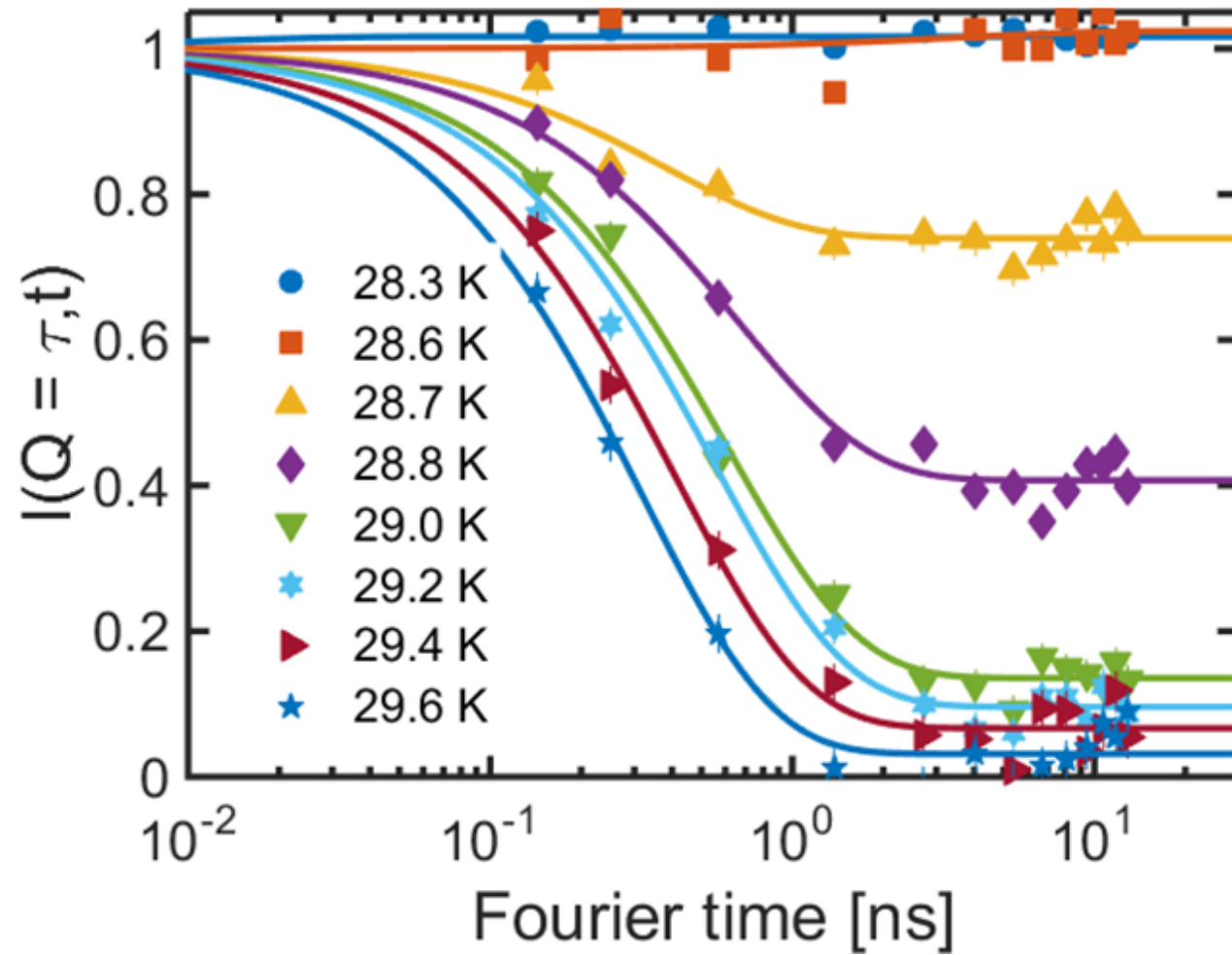
Evolution of fluctuations

Seen by with ferromagnetic NSE on IN15

$$I(Q, t) = \frac{C}{(Q - 2\pi/\ell)^2 + 1/\xi^2} e^{[-t/\tau_0]} = S(Q) e^{[-t/\tau_0]}$$

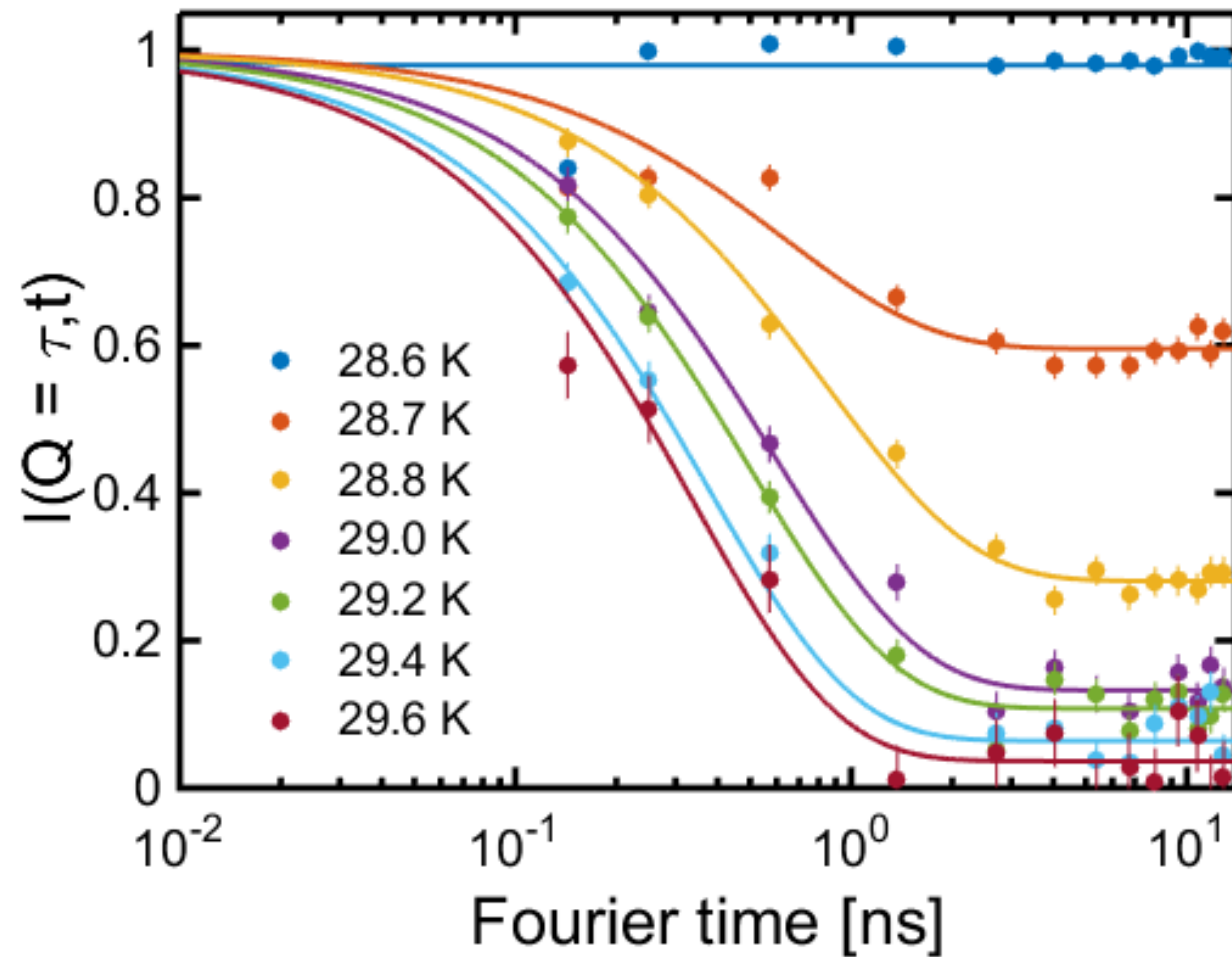


RELAXATION DOES NOT CHANGE WITH FIELD !



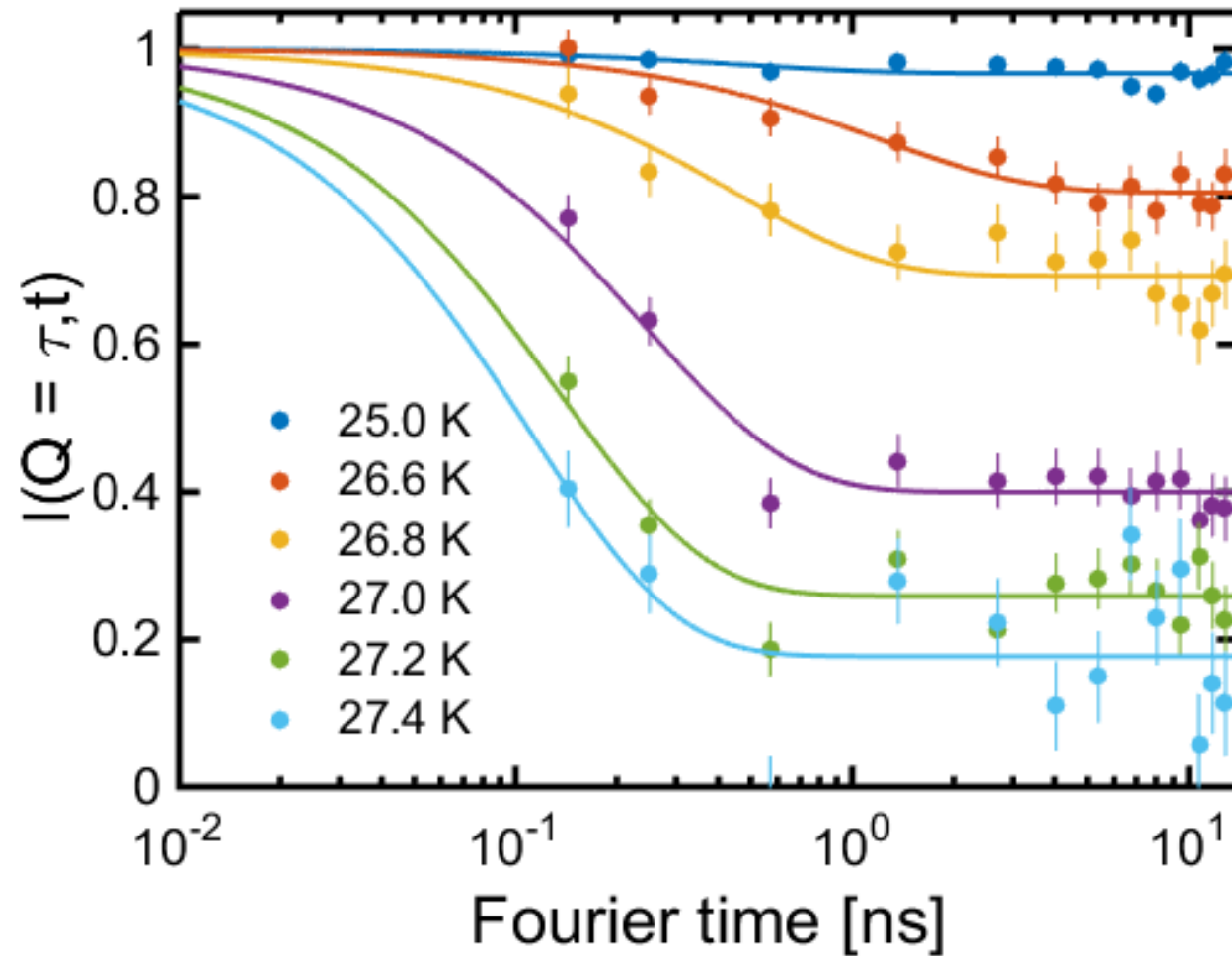
$B = 0.16 \text{ T}$

RELAXATION DOES NOT CHANGE WITH FIELD !



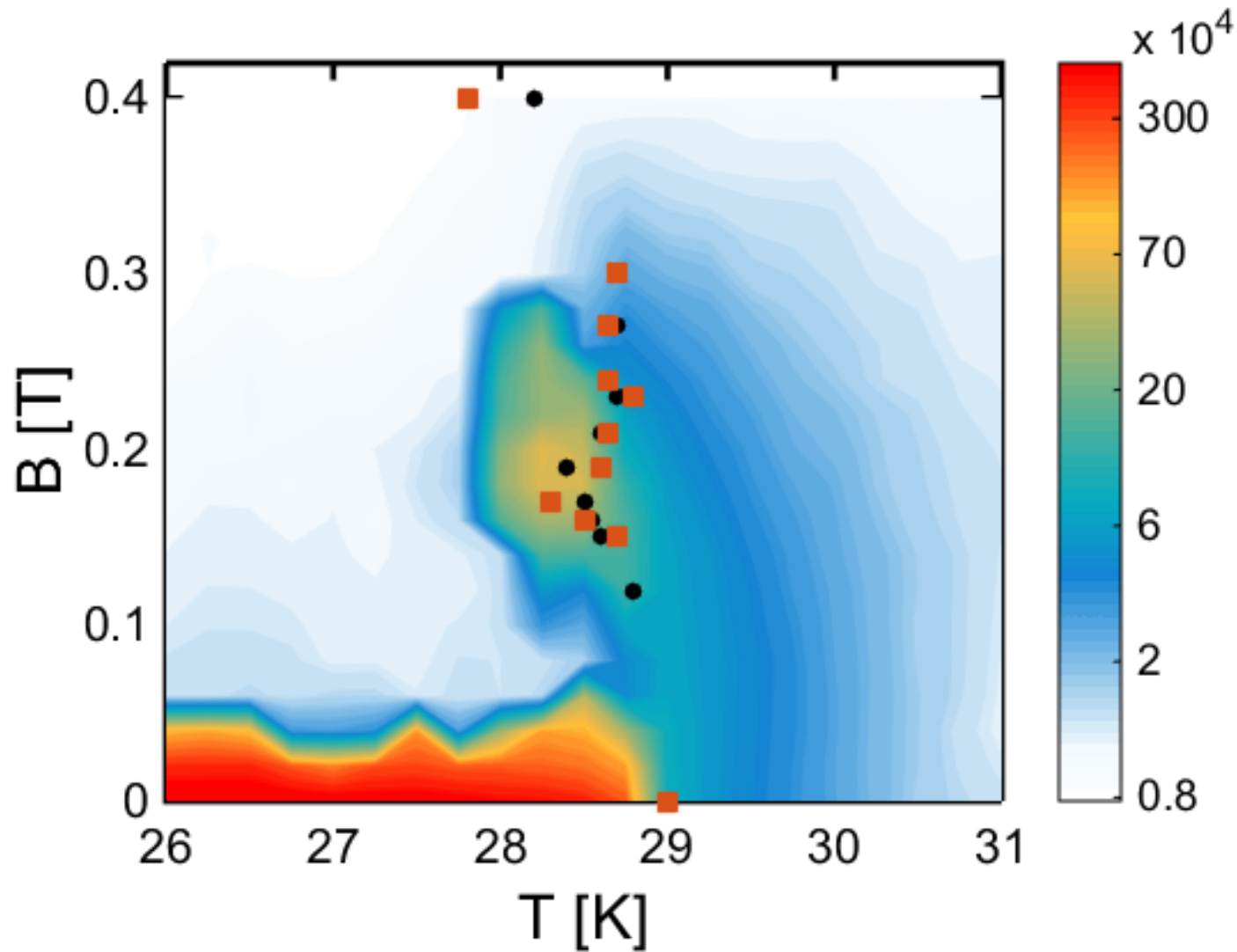
$B = 0.24 \text{ T}$

RELAXATION DOES NOT CHANGE WITH FIELD !



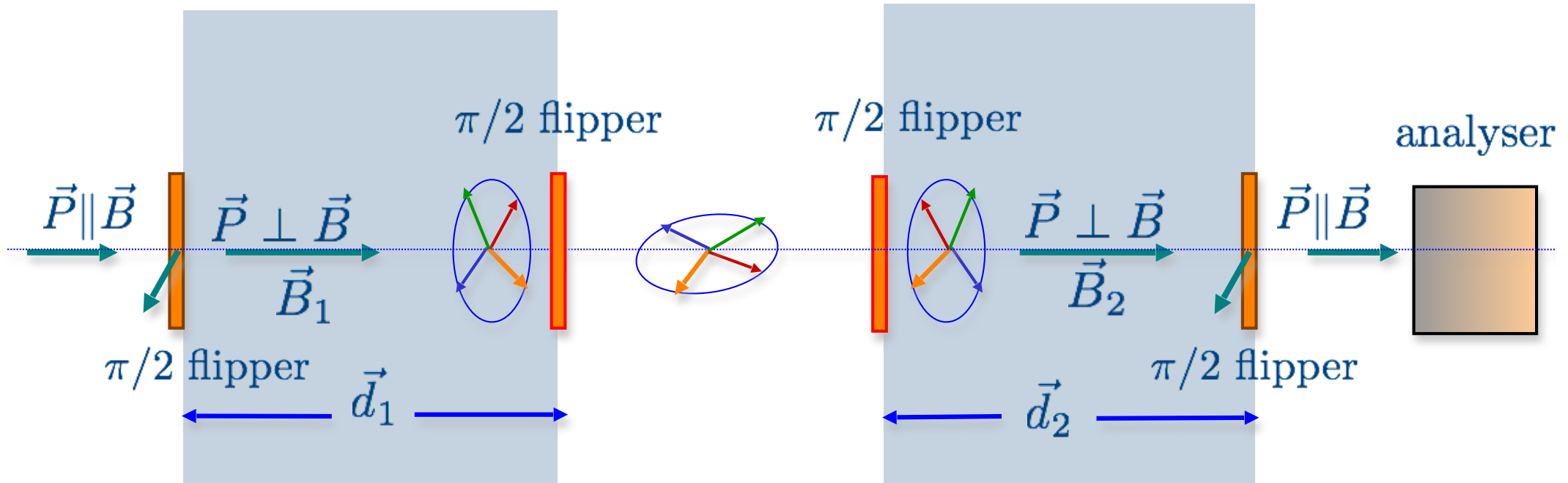
EXCEPT
for
 $B = 0.5 \text{ T}$

Fluctuations co-exist with the SKL phase



- Magnetic scattering
- Paramagnetic NSE
- Ferromagnetic NSE: magnetic fields
- **Intensity modulated NSE: for samples depolarising the neutron beam: ferromagnets, superconductors**
- Polarimetric NSE: chirality

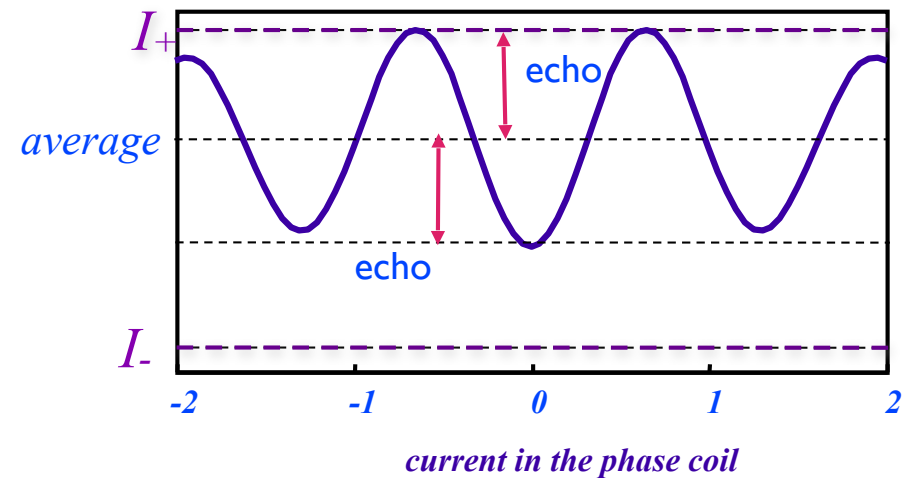
ferromagnetic neutron spin echo



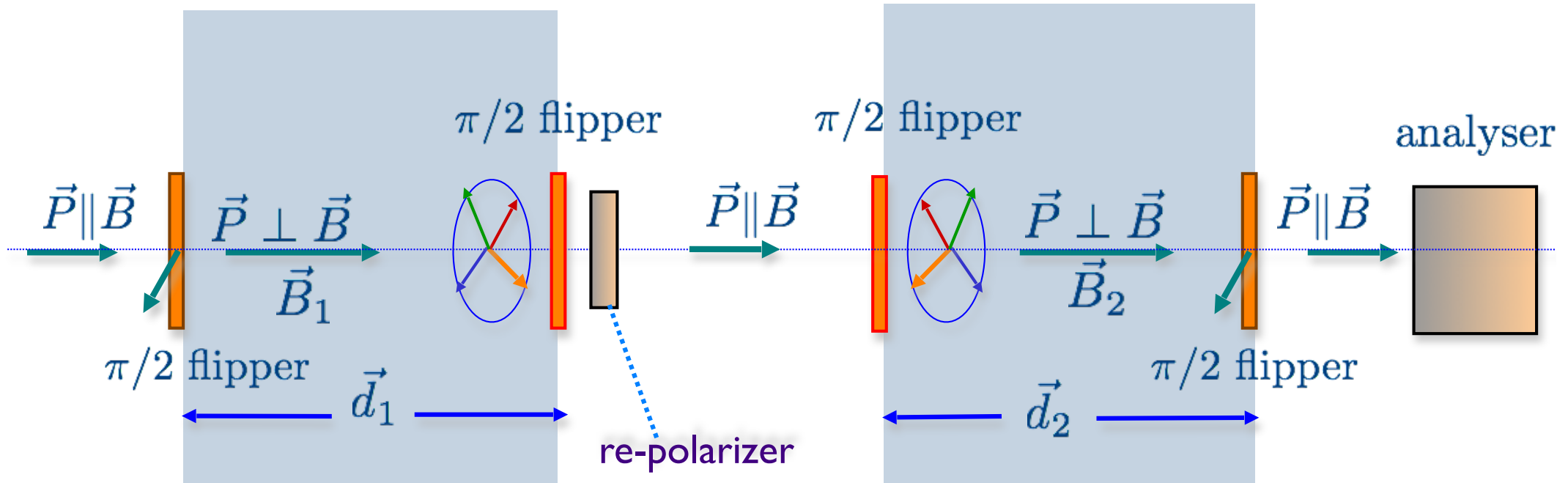
ideally

$$\text{echo modulation} = (I_+ - I_-) / 3$$

$$\text{for } |\vec{P}| = 1$$



intensity modulated neutron spin echo

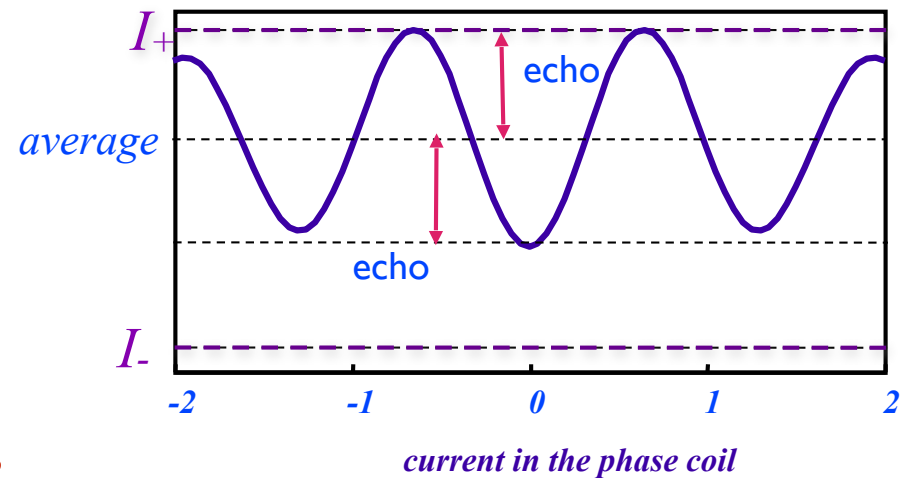


ideally

$$\text{echo modulation} = (I_+ - I_-) / 3$$

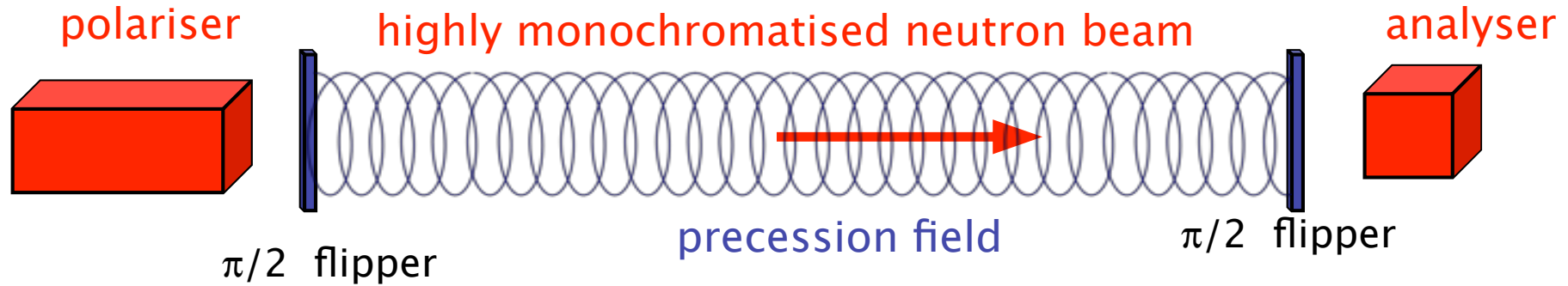
$$\text{for } |\vec{P}| = 1$$

factor of 2 intensity loss



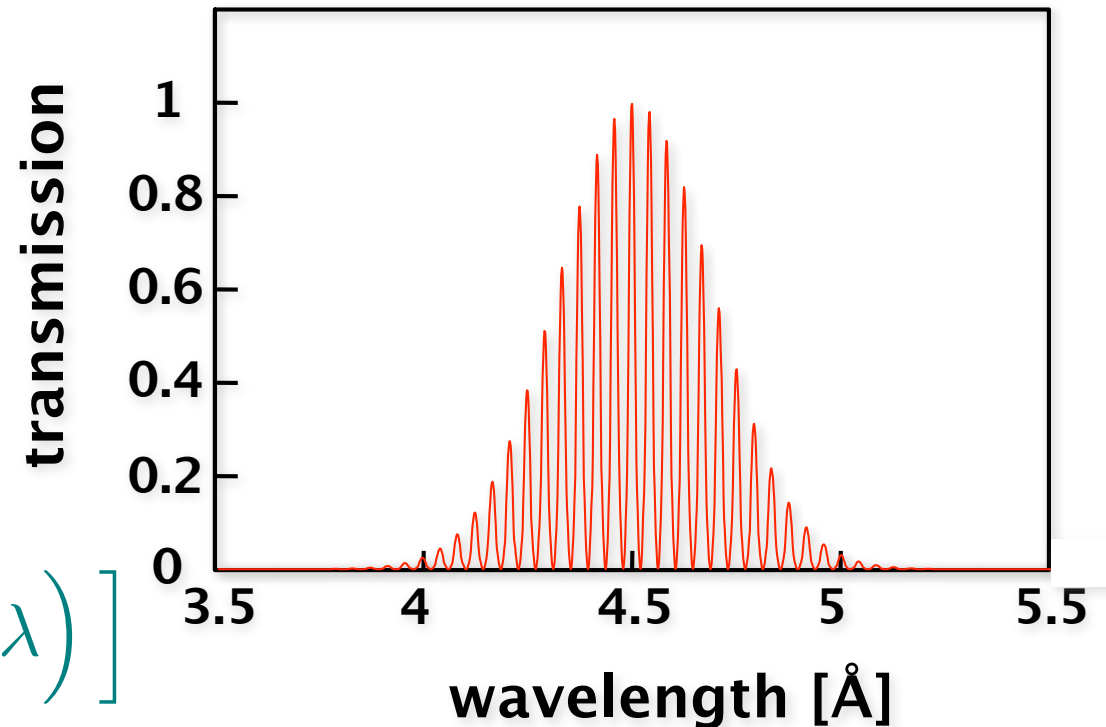
IMNSE - polarimetric NSE

transmission of the sequence



$$\begin{aligned}\phi &= \gamma B t_{tof} = \gamma B \ell / v \\ &= \frac{\gamma m}{h} B \ell \lambda\end{aligned}$$

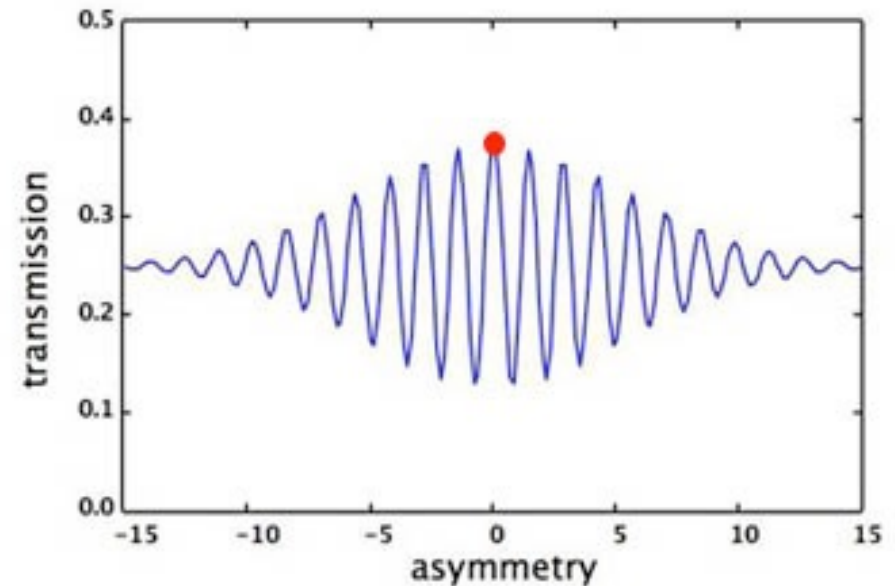
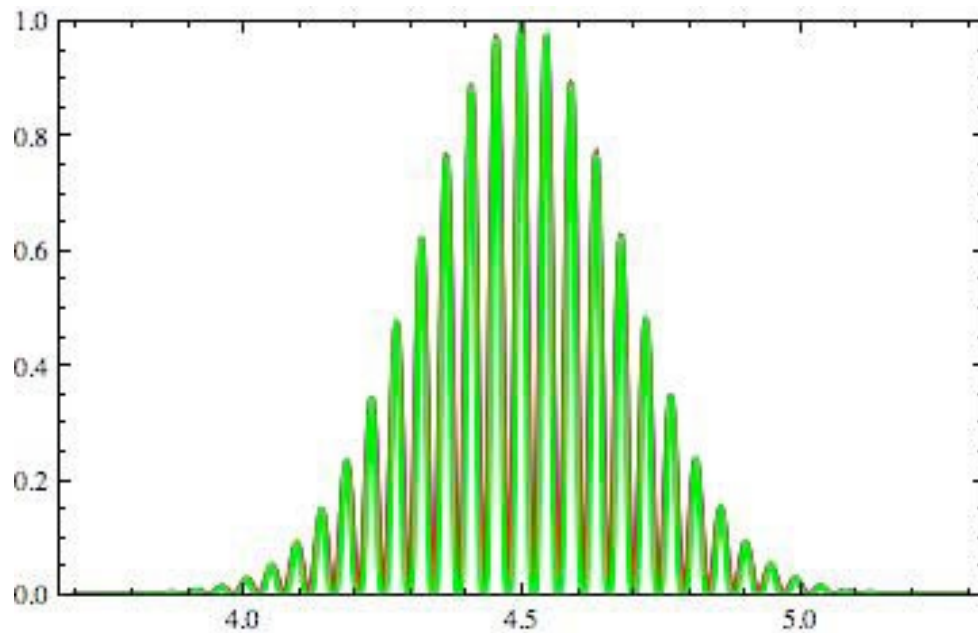
$$T(B, \lambda) = \left[1 + \sin \left(\frac{\gamma m}{h} B \ell \lambda \right) \right]$$



IMNSE - polarimetric NSE

transmission of the setup

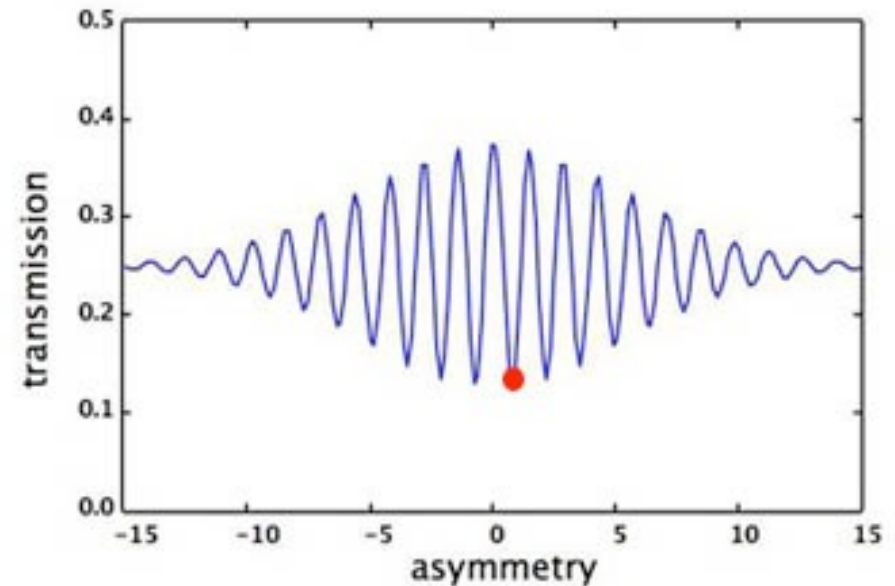
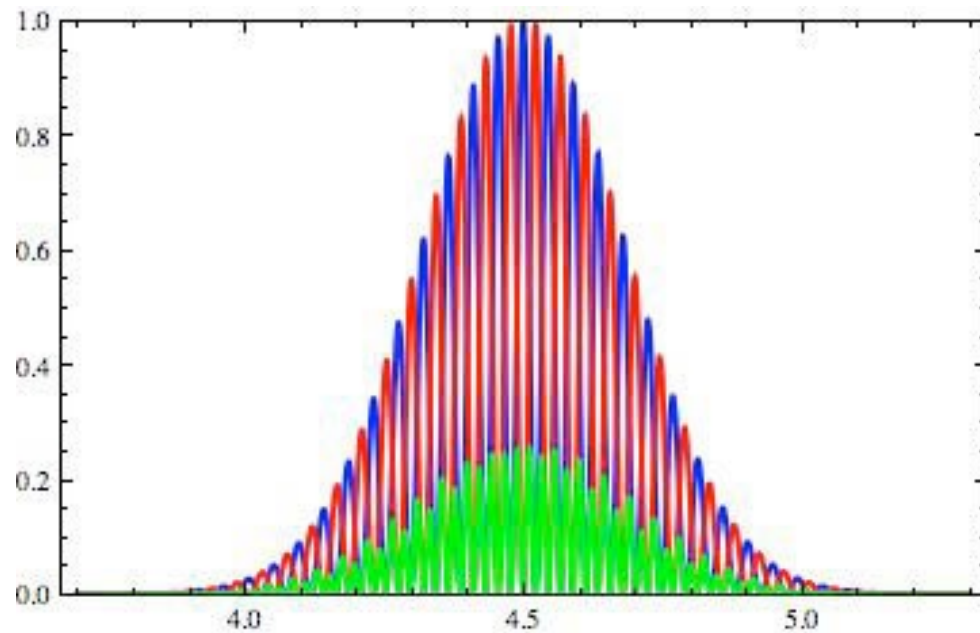
$$\frac{I_{IMNSE}(\Delta I)}{I_0} = \int T_1(I + \Delta I, \lambda) \cdot T_2(I, \lambda) \cdot g(\lambda) d\lambda$$
$$g(\lambda) = \frac{1}{\sqrt{2\pi\sigma^2}} \exp\left(-\frac{(\lambda - \lambda_0)^2}{2\sigma^2}\right)$$



IMNSE - polarimetric NSE

transmission of the setup

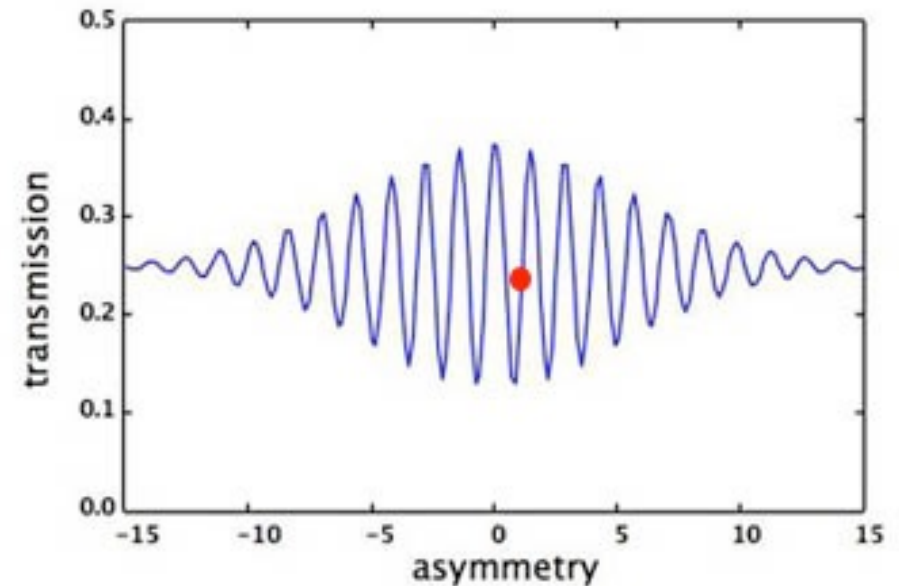
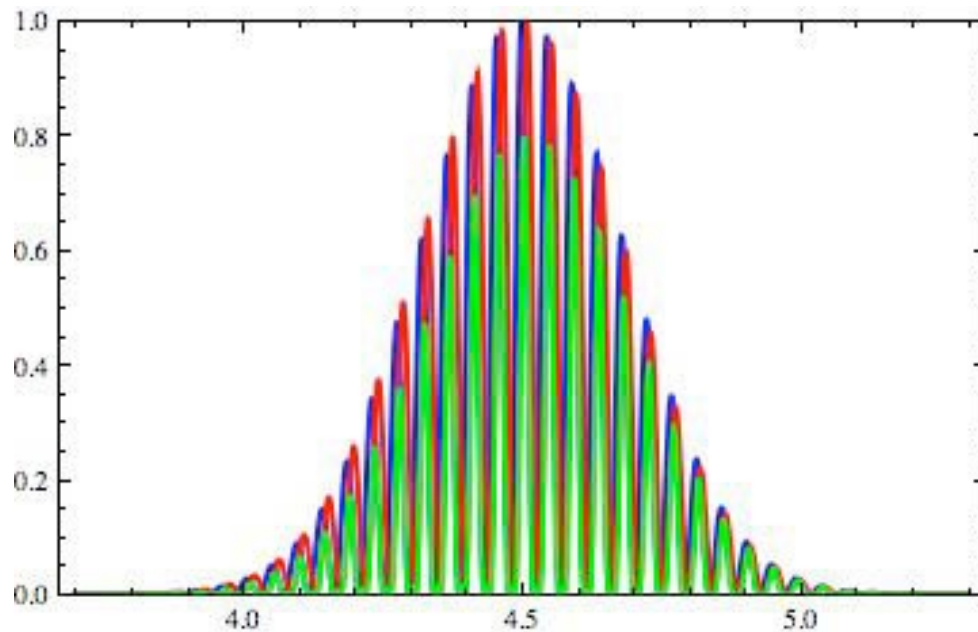
$$\frac{I_{IMNSE}(\Delta I)}{I_0} = \int T_1(I + \Delta I, \lambda) \cdot T_2(I, \lambda) \cdot g(\lambda) d\lambda$$
$$g(\lambda) = \frac{1}{\sqrt{2\pi\sigma^2}} \exp\left(-\frac{(\lambda - \lambda_0)^2}{2\sigma^2}\right)$$



IMNSE - polarimetric NSE

transmission of the setup

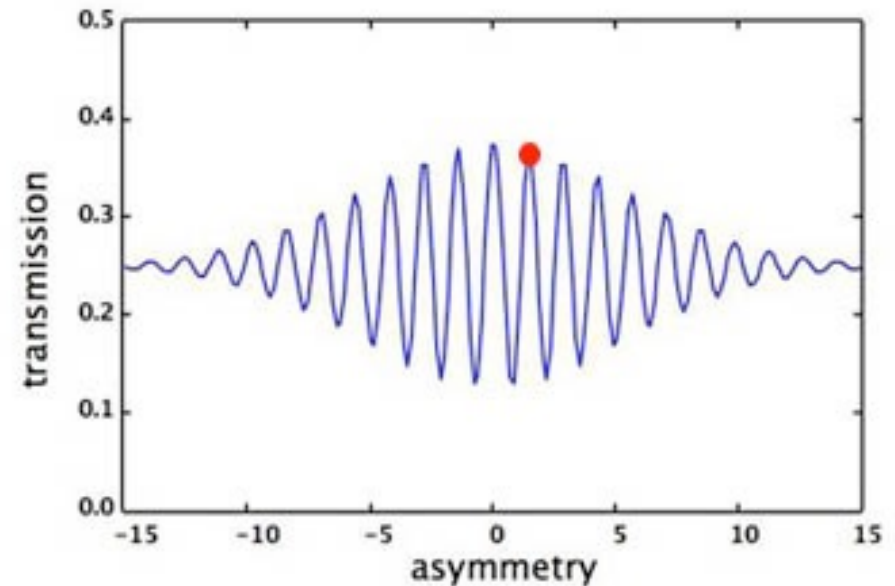
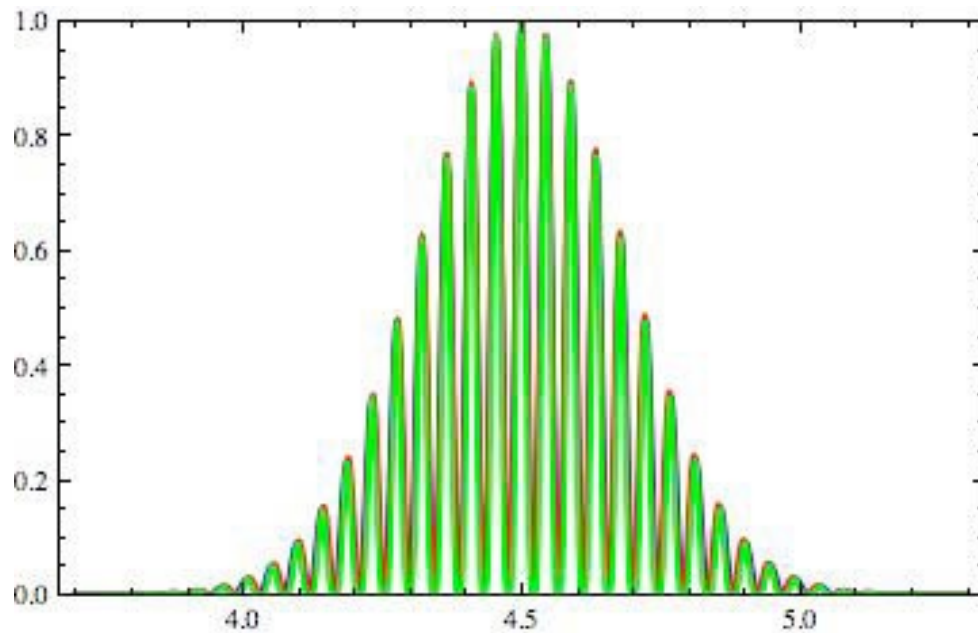
$$\frac{I_{IMNSE}(\Delta I)}{I_0} = \int T_1(I + \Delta I, \lambda) \cdot T_2(I, \lambda) \cdot g(\lambda) d\lambda$$
$$g(\lambda) = \frac{1}{\sqrt{2\pi\sigma^2}} \exp\left(-\frac{(\lambda - \lambda_0)^2}{2\sigma^2}\right)$$



IMNSE - polarimetric NSE

transmission of the setup

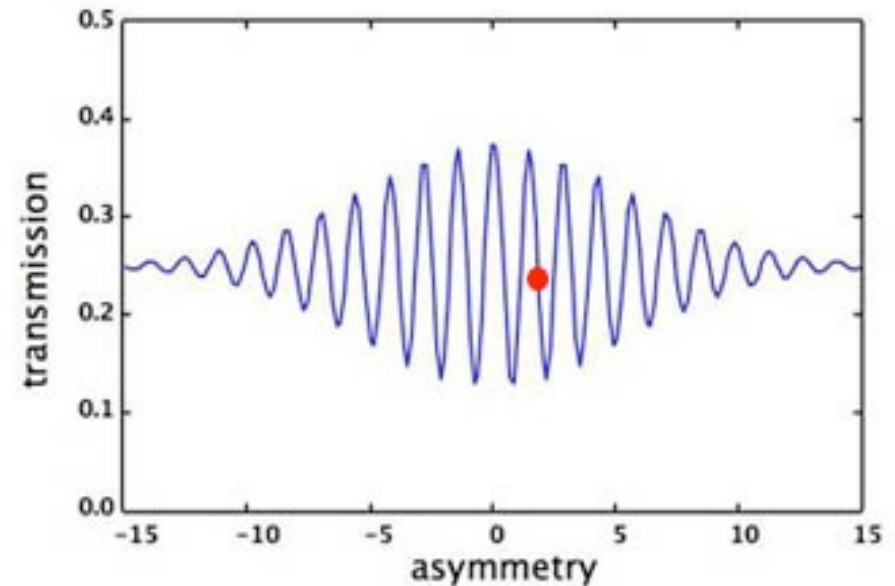
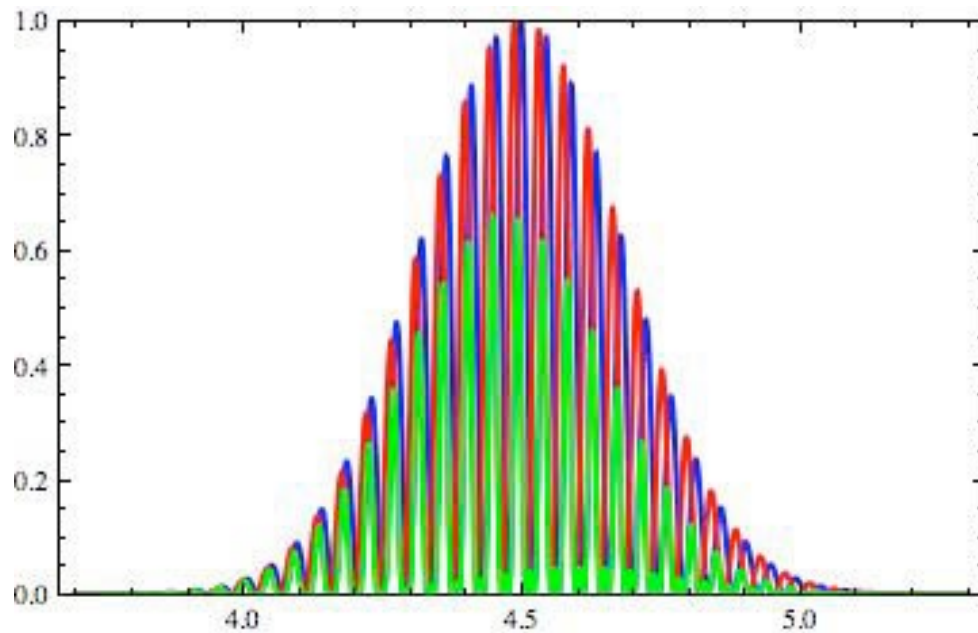
$$\frac{I_{IMNSE}(\Delta I)}{I_0} = \int T_1(I + \Delta I, \lambda) \cdot T_2(I, \lambda) \cdot g(\lambda) d\lambda$$
$$g(\lambda) = \frac{1}{\sqrt{2\pi\sigma^2}} \exp\left(-\frac{(\lambda - \lambda_0)^2}{2\sigma^2}\right)$$



IMNSE - polarimetric NSE

transmission of the setup

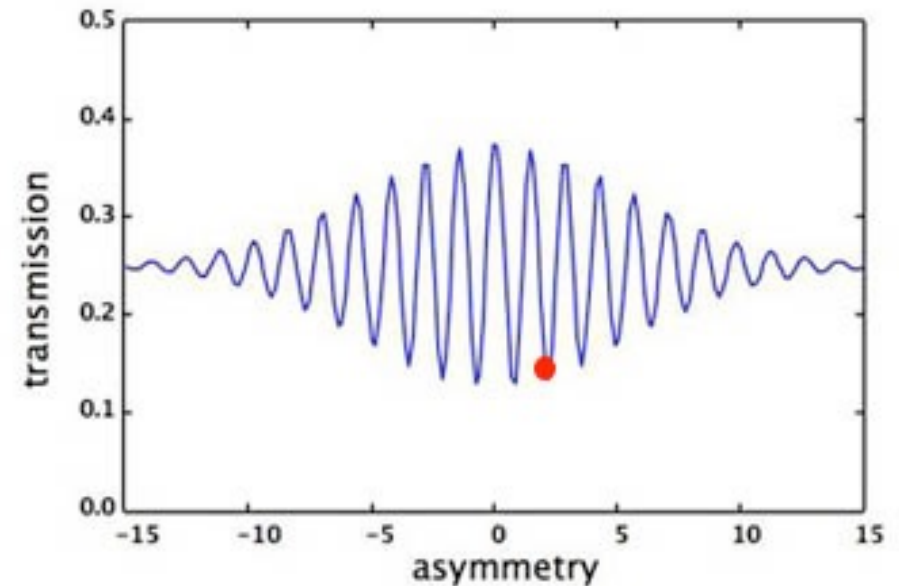
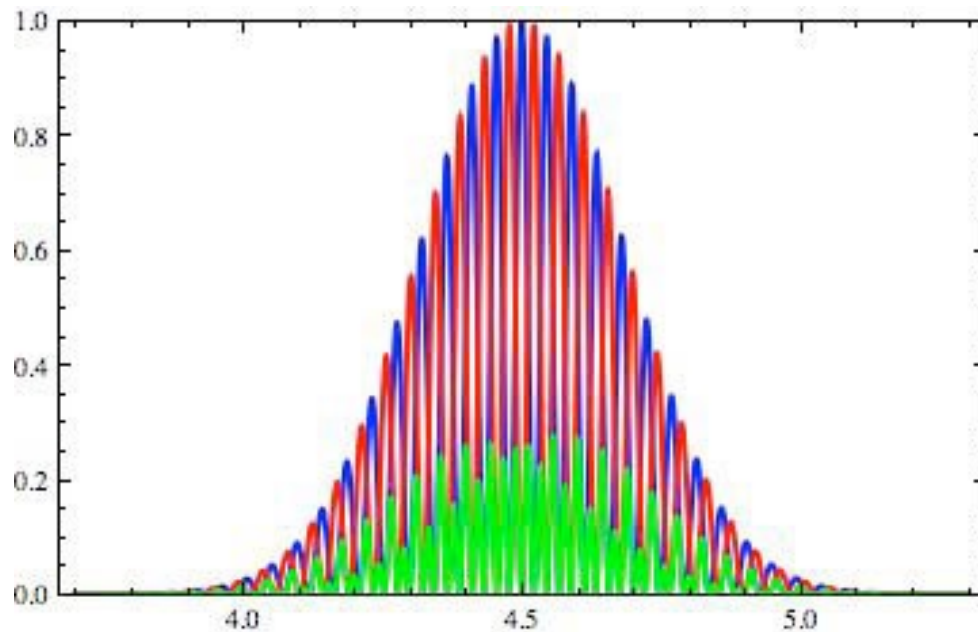
$$\frac{I_{IMNSE}(\Delta I)}{I_0} = \int T_1(I + \Delta I, \lambda) \cdot T_2(I, \lambda) \cdot g(\lambda) d\lambda$$
$$g(\lambda) = \frac{1}{\sqrt{2\pi\sigma^2}} \exp\left(-\frac{(\lambda - \lambda_0)^2}{2\sigma^2}\right)$$



IMNSE - polarimetric NSE

transmission of the setup

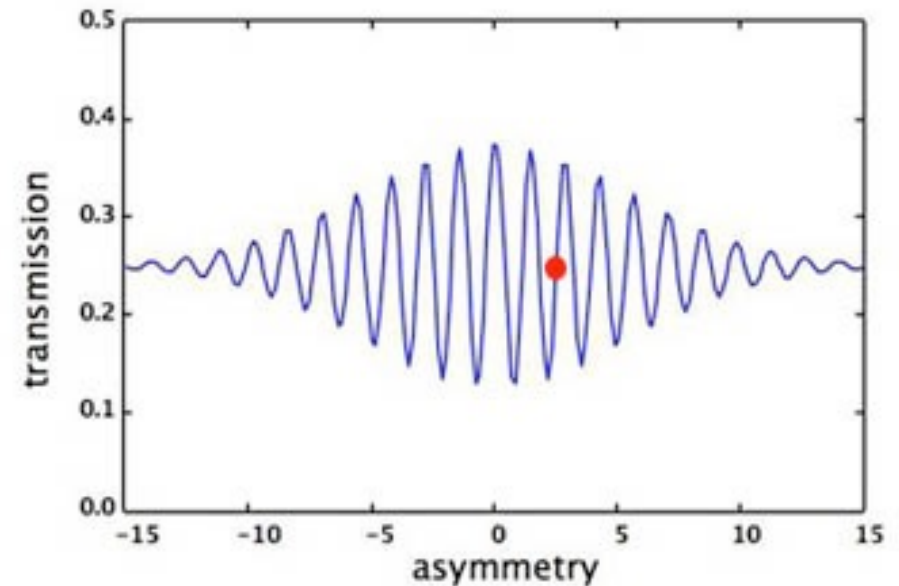
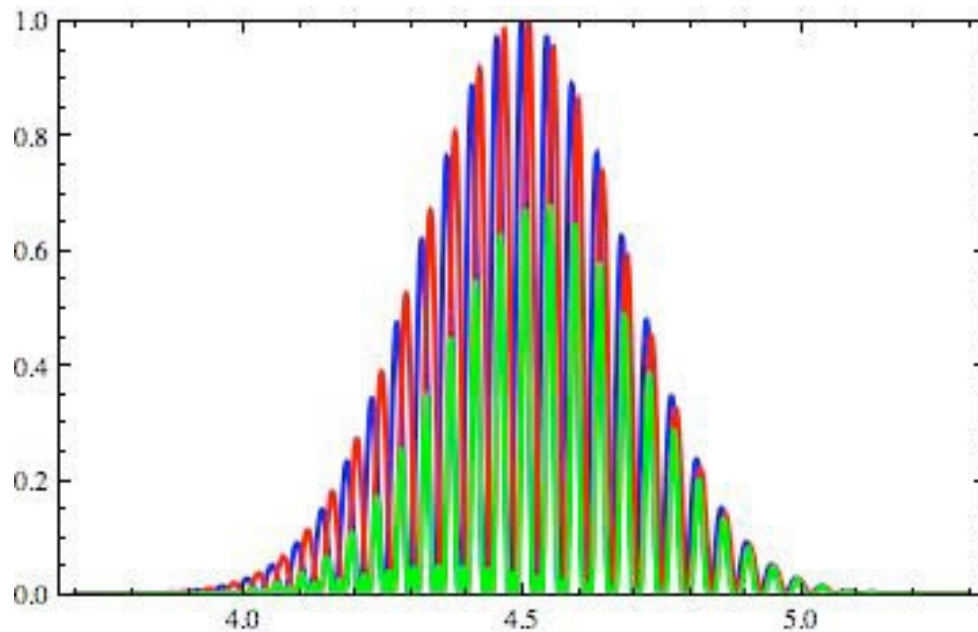
$$\frac{I_{IMNSE}(\Delta I)}{I_0} = \int T_1(I + \Delta I, \lambda) \cdot T_2(I, \lambda) \cdot g(\lambda) d\lambda$$
$$g(\lambda) = \frac{1}{\sqrt{2\pi\sigma^2}} \exp\left(-\frac{(\lambda - \lambda_0)^2}{2\sigma^2}\right)$$



IMNSE - polarimetric NSE

transmission of the setup

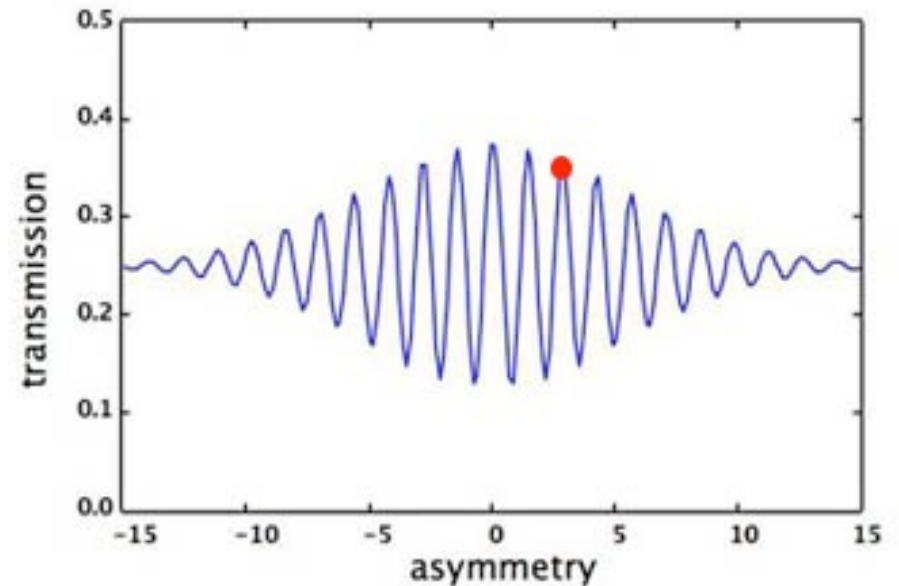
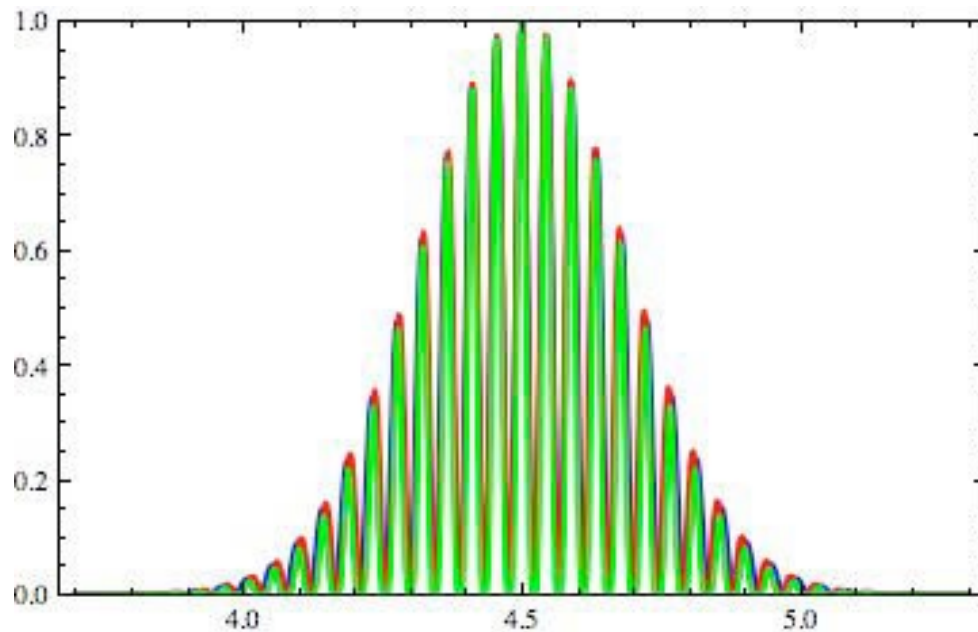
$$\frac{I_{IMNSE}(\Delta I)}{I_0} = \int T_1(I + \Delta I, \lambda) \cdot T_2(I, \lambda) \cdot g(\lambda) d\lambda$$
$$g(\lambda) = \frac{1}{\sqrt{2\pi\sigma^2}} \exp\left(-\frac{(\lambda - \lambda_0)^2}{2\sigma^2}\right)$$



IMNSE - polarimetric NSE

transmission of the setup

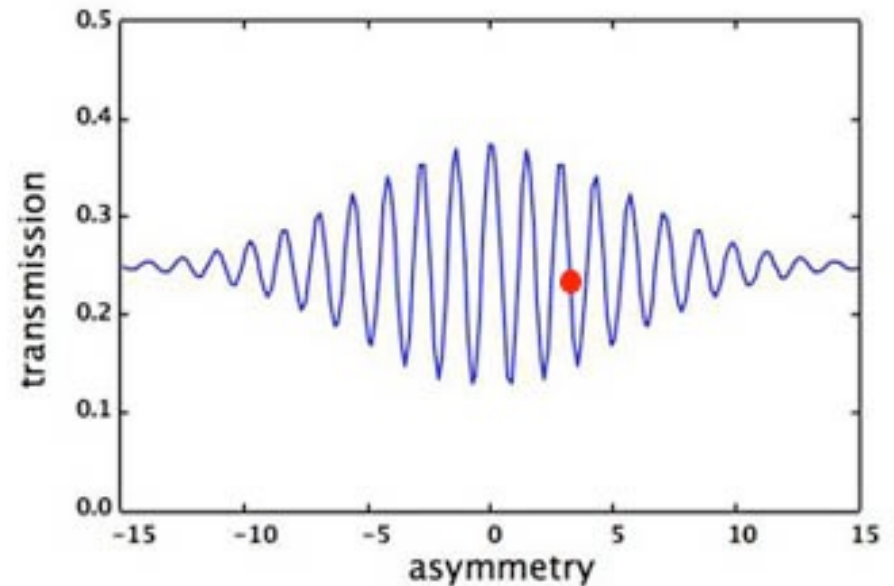
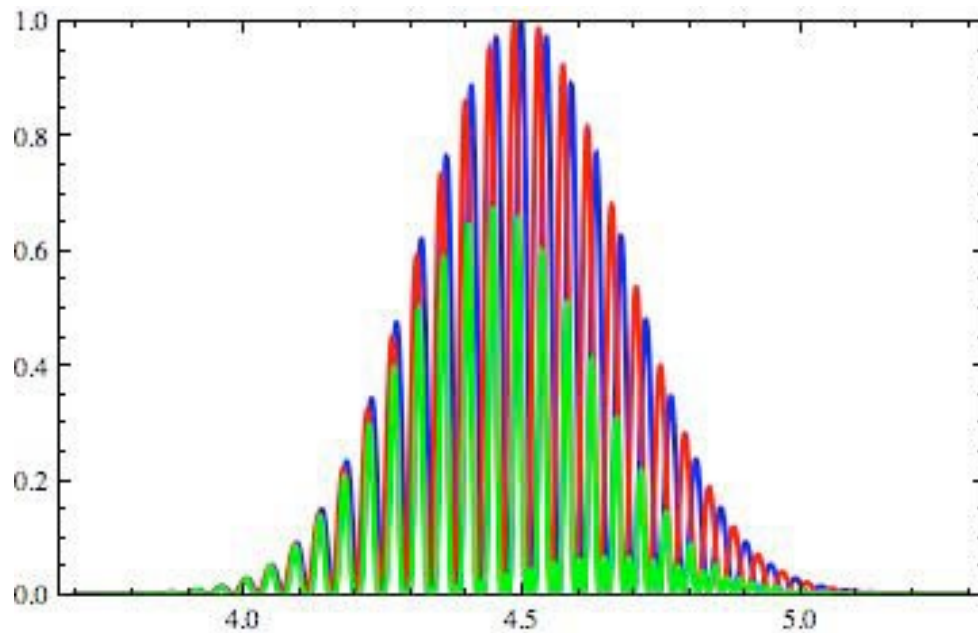
$$\frac{I_{IMNSE}(\Delta I)}{I_0} = \int T_1(I + \Delta I, \lambda) \cdot T_2(I, \lambda) \cdot g(\lambda) d\lambda$$
$$g(\lambda) = \frac{1}{\sqrt{2\pi\sigma^2}} \exp\left(-\frac{(\lambda - \lambda_0)^2}{2\sigma^2}\right)$$



IMNSE - polarimetric NSE

transmission of the setup

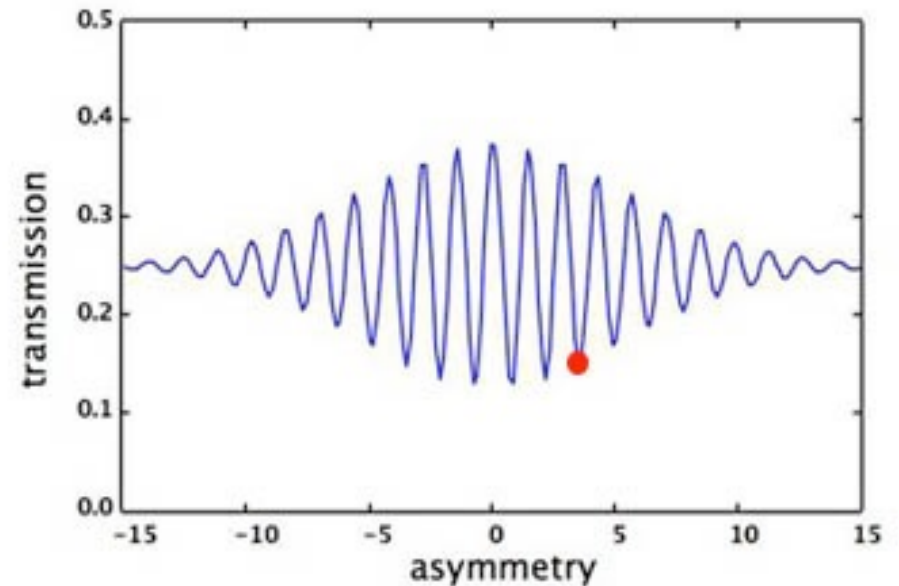
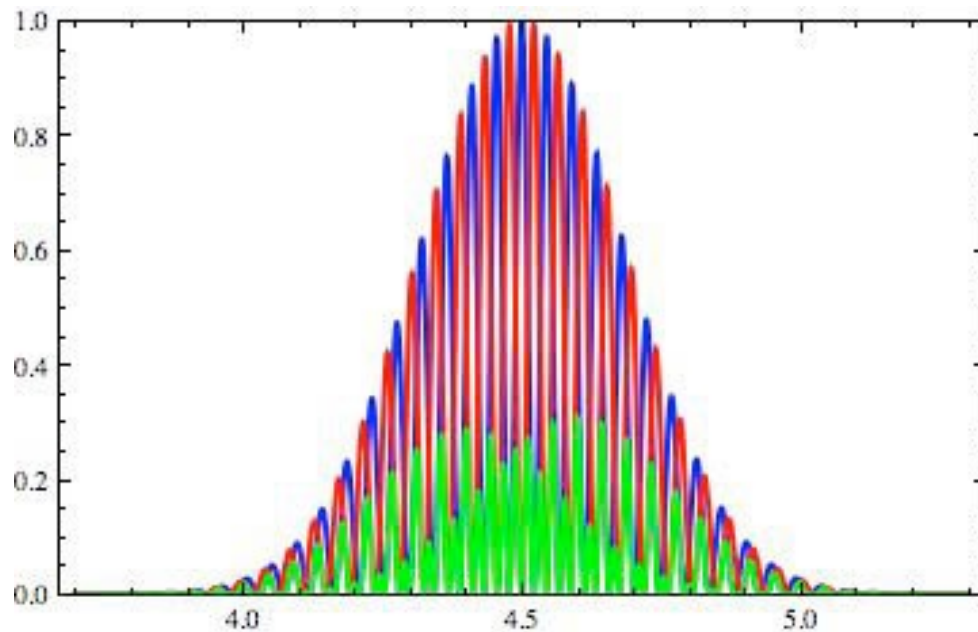
$$\frac{I_{IMNSE}(\Delta I)}{I_0} = \int T_1(I + \Delta I, \lambda) \cdot T_2(I, \lambda) \cdot g(\lambda) d\lambda$$
$$g(\lambda) = \frac{1}{\sqrt{2\pi\sigma^2}} \exp\left(-\frac{(\lambda - \lambda_0)^2}{2\sigma^2}\right)$$



IMNSE - polarimetric NSE

transmission of the setup

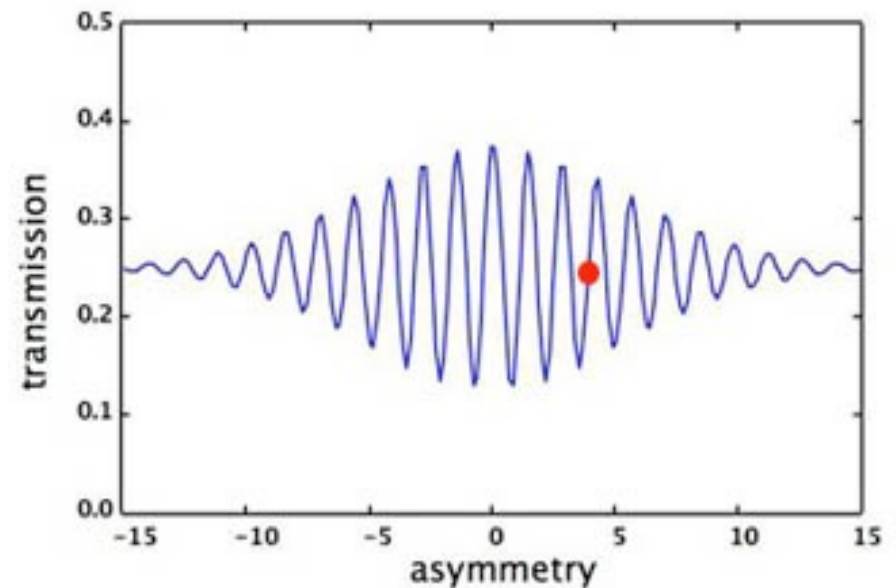
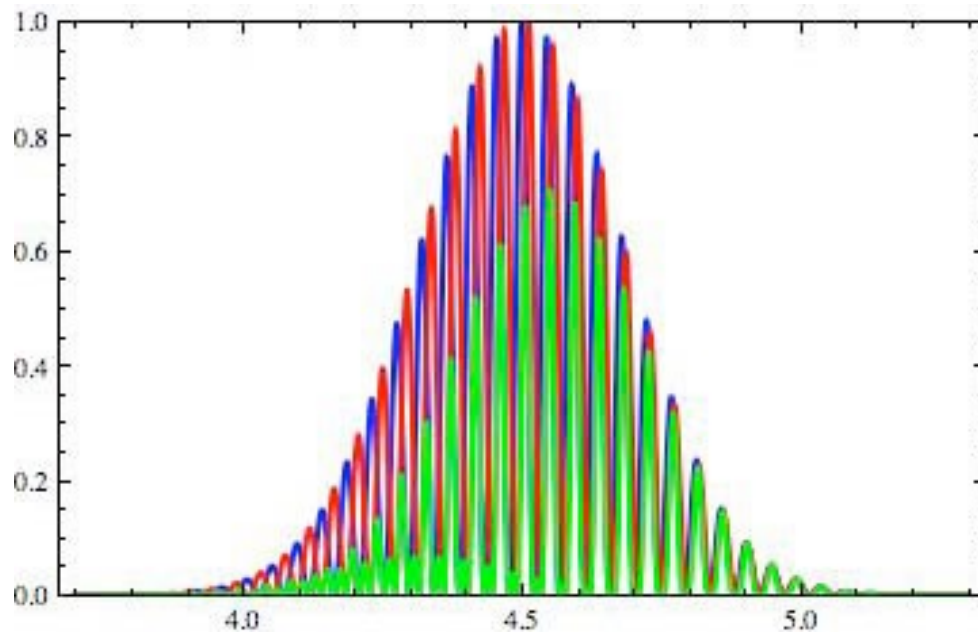
$$\frac{I_{IMNSE}(\Delta I)}{I_0} = \int T_1(I + \Delta I, \lambda) \cdot T_2(I, \lambda) \cdot g(\lambda) d\lambda$$
$$g(\lambda) = \frac{1}{\sqrt{2\pi\sigma^2}} \exp\left(-\frac{(\lambda - \lambda_0)^2}{2\sigma^2}\right)$$



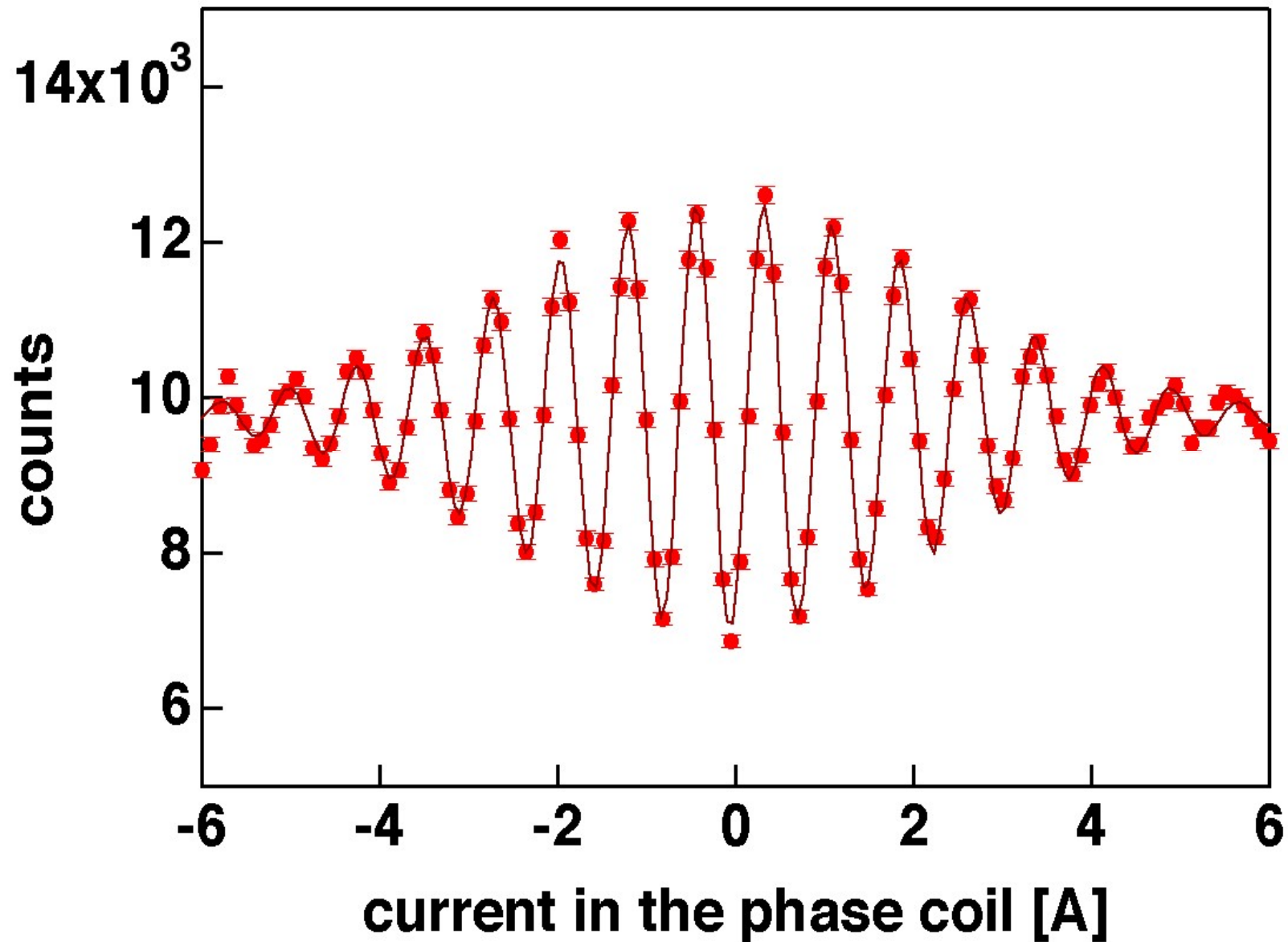
IMNSE - polarimetric NSE

transmission of the setup

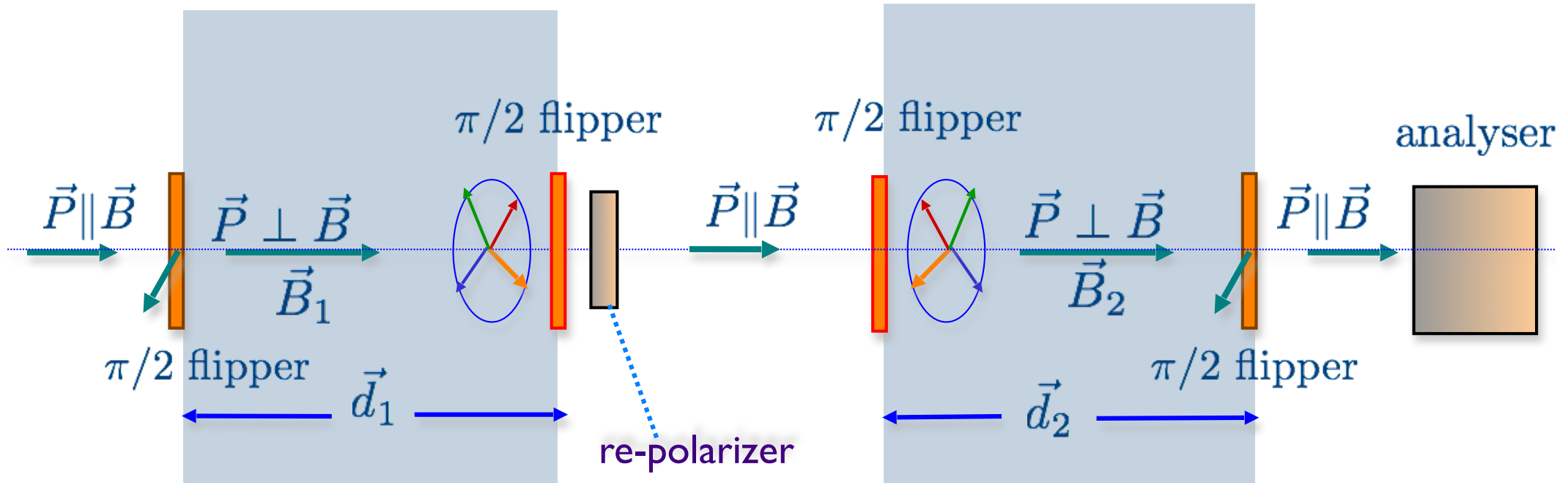
$$\frac{I_{IMNSE}(\Delta I)}{I_0} = \int T_1(I + \Delta I, \lambda) \cdot T_2(I, \lambda) \cdot g(\lambda) d\lambda$$
$$g(\lambda) = \frac{1}{\sqrt{2\pi\sigma^2}} \exp\left(-\frac{(\lambda - \lambda_0)^2}{2\sigma^2}\right)$$



spin-flip scattering on the helical Bragg peak of MnSi below T_c



intensity modulated neutron spin echo

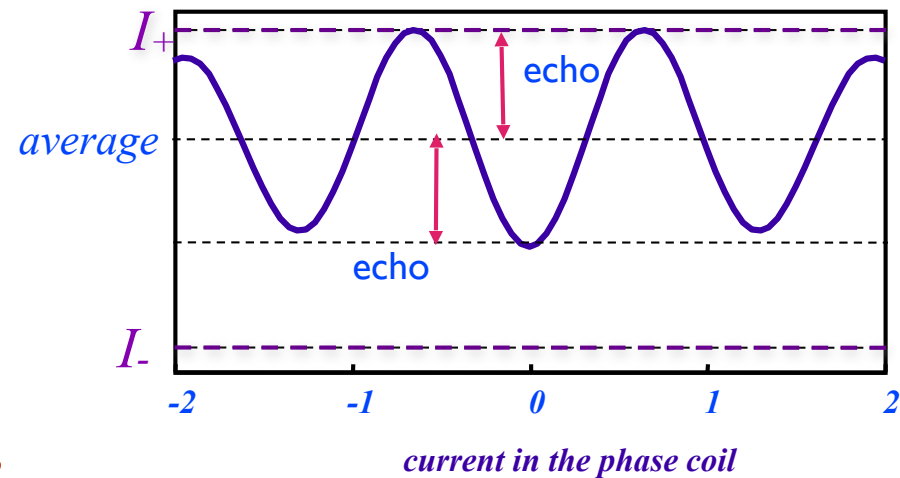


ideally

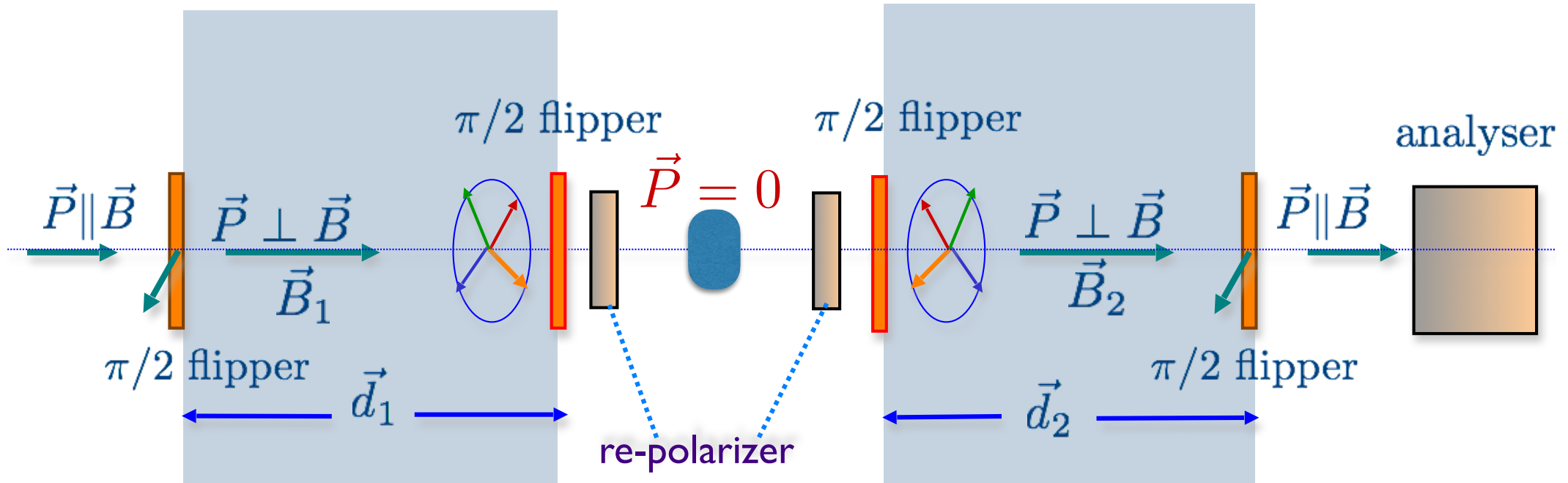
$$\text{echo modulation} = (I_+ - I_-) / 3$$

$$\text{for } |\vec{P}| = 1$$

factor of 2 intensity loss



intensity modulated neutron spin echo

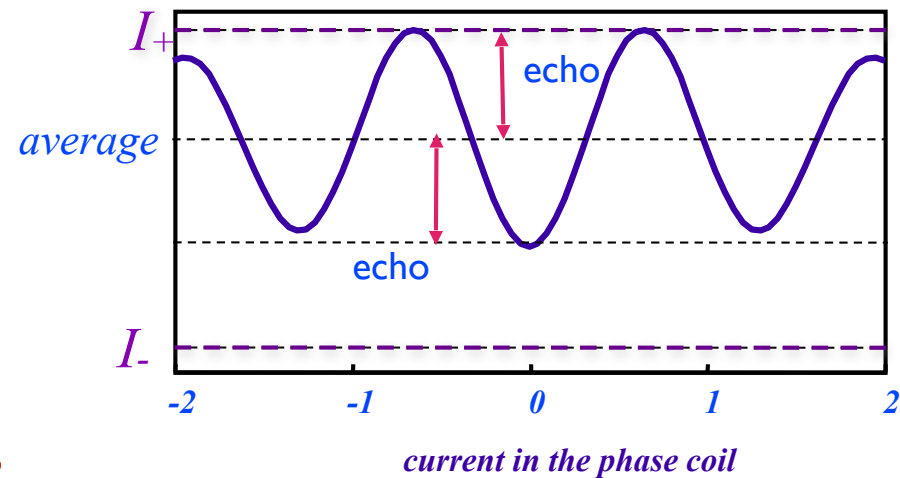


ideally

$$\text{echo modulation} = (I_+ - I_-) / 3$$

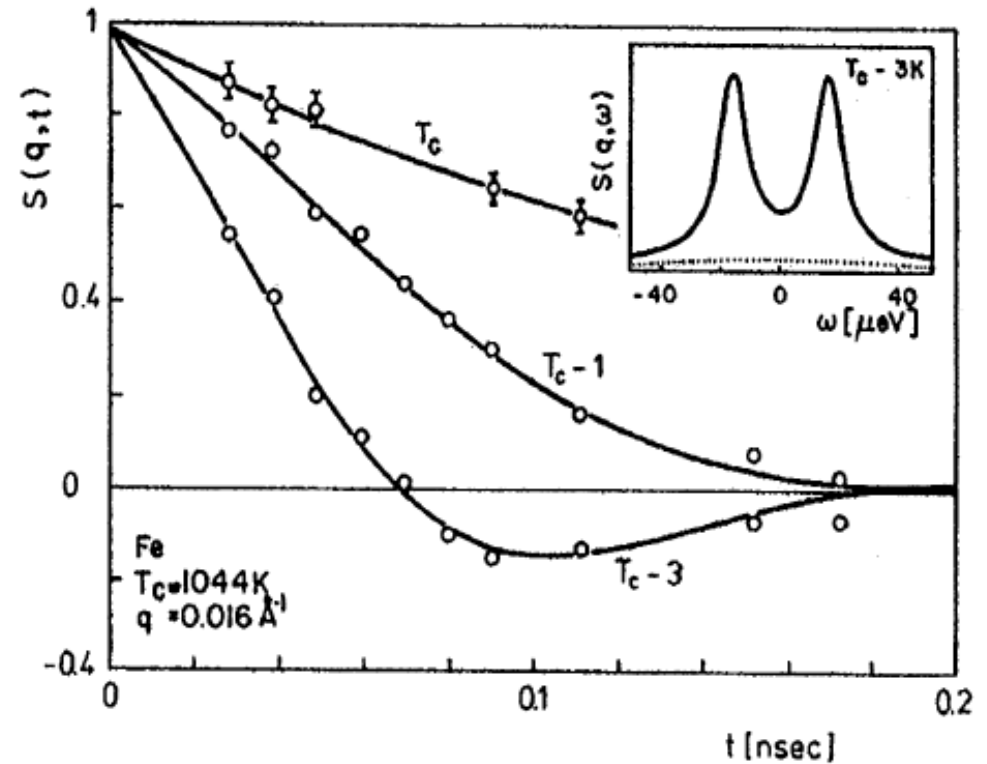
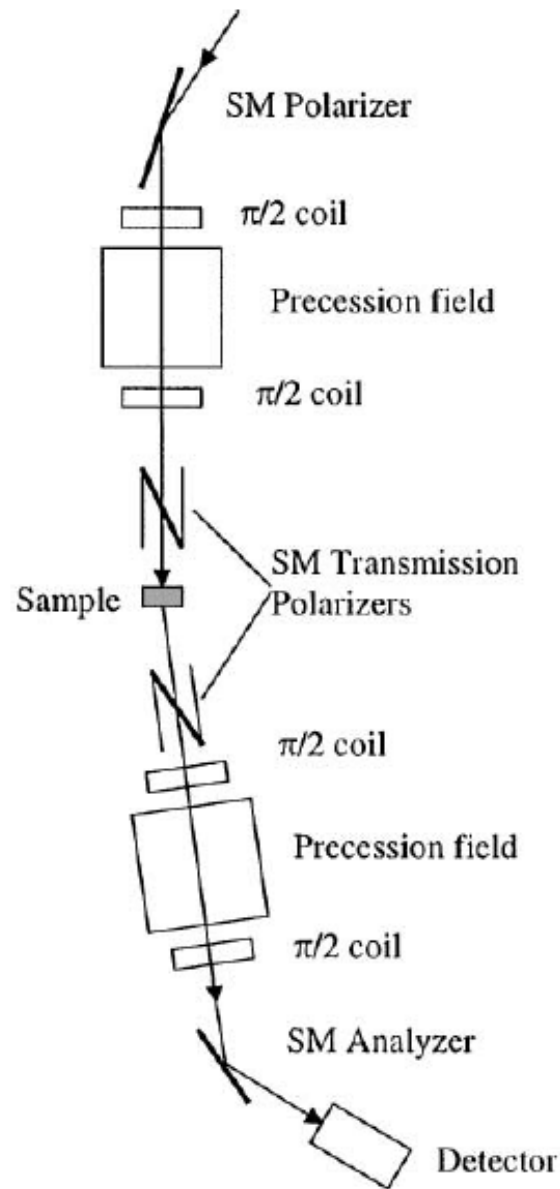
$$\text{for } |\vec{P}| = 1$$

factor of $\frac{2}{3}$ intensity loss



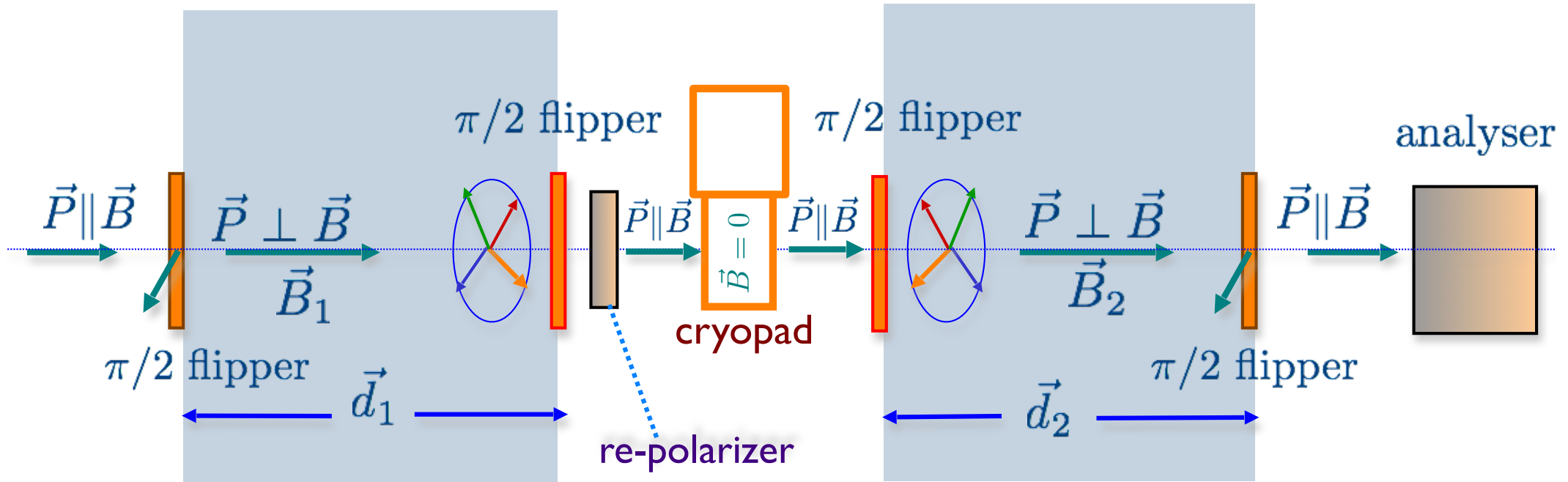
first IMNSE measurements emergence of magnons in Fe

B. Farago, F. Mezei, Physica B (1986)



- Magnetic scattering
- Paramagnetic NSE
- Ferromagnetic NSE: magnetic fields
- Intensity modulated NSE: for samples depolarising the neutron beam: ferromagnets, superconductors
- Polarimetric NSE: chirality

ferromagnetic neutron spin echo

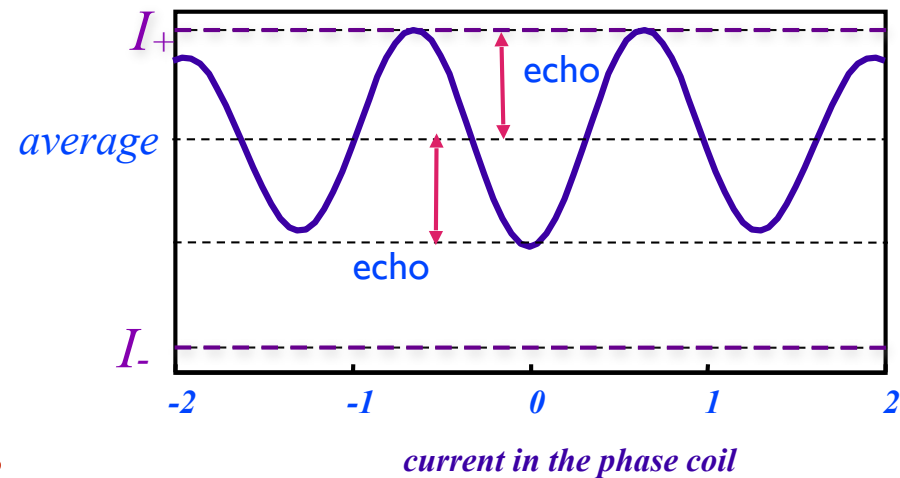


ideally

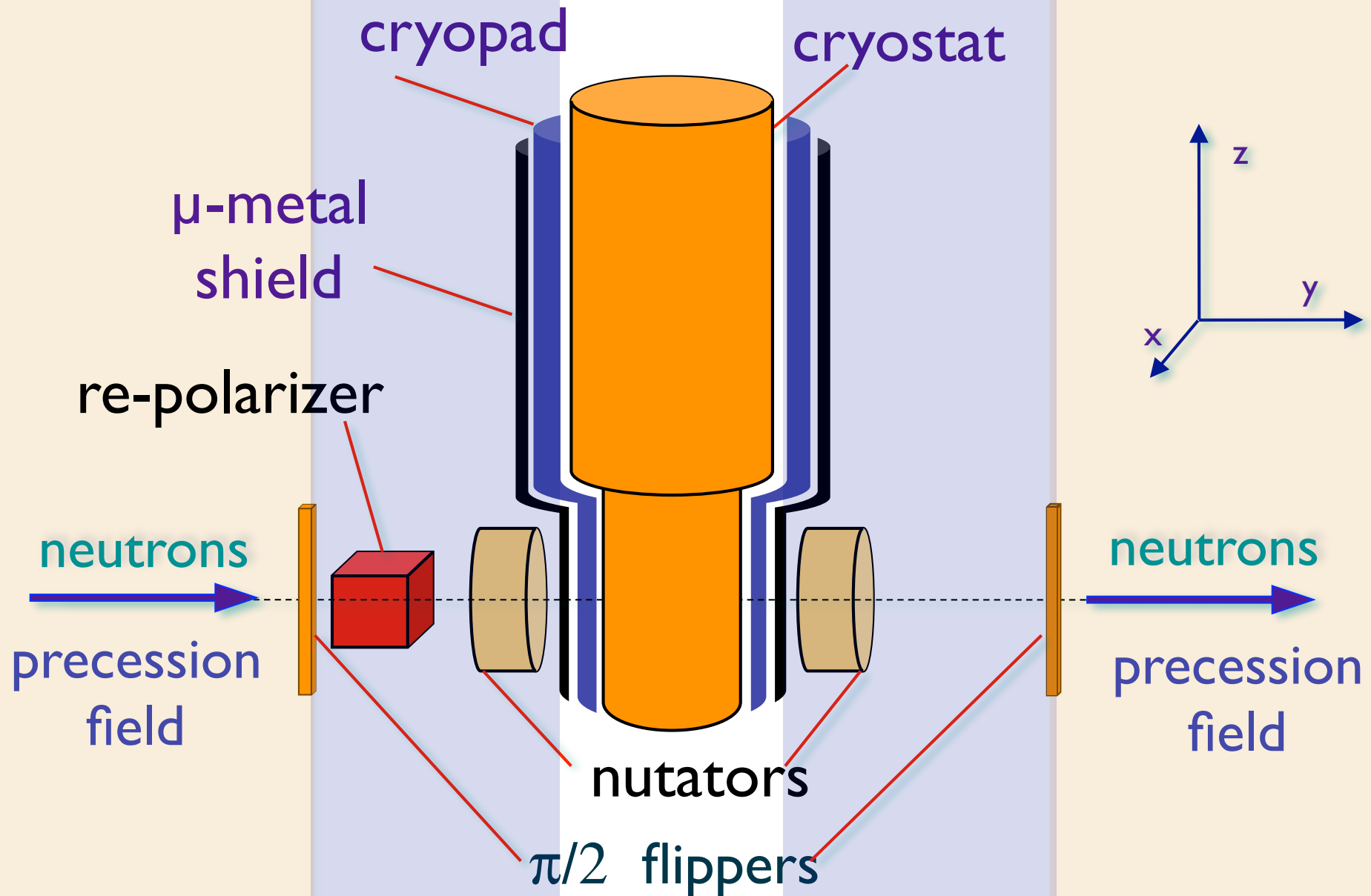
$$\text{echo modulation} = (I_+ - I_-) / 3$$

$$\text{for } |\vec{P}| = 1$$

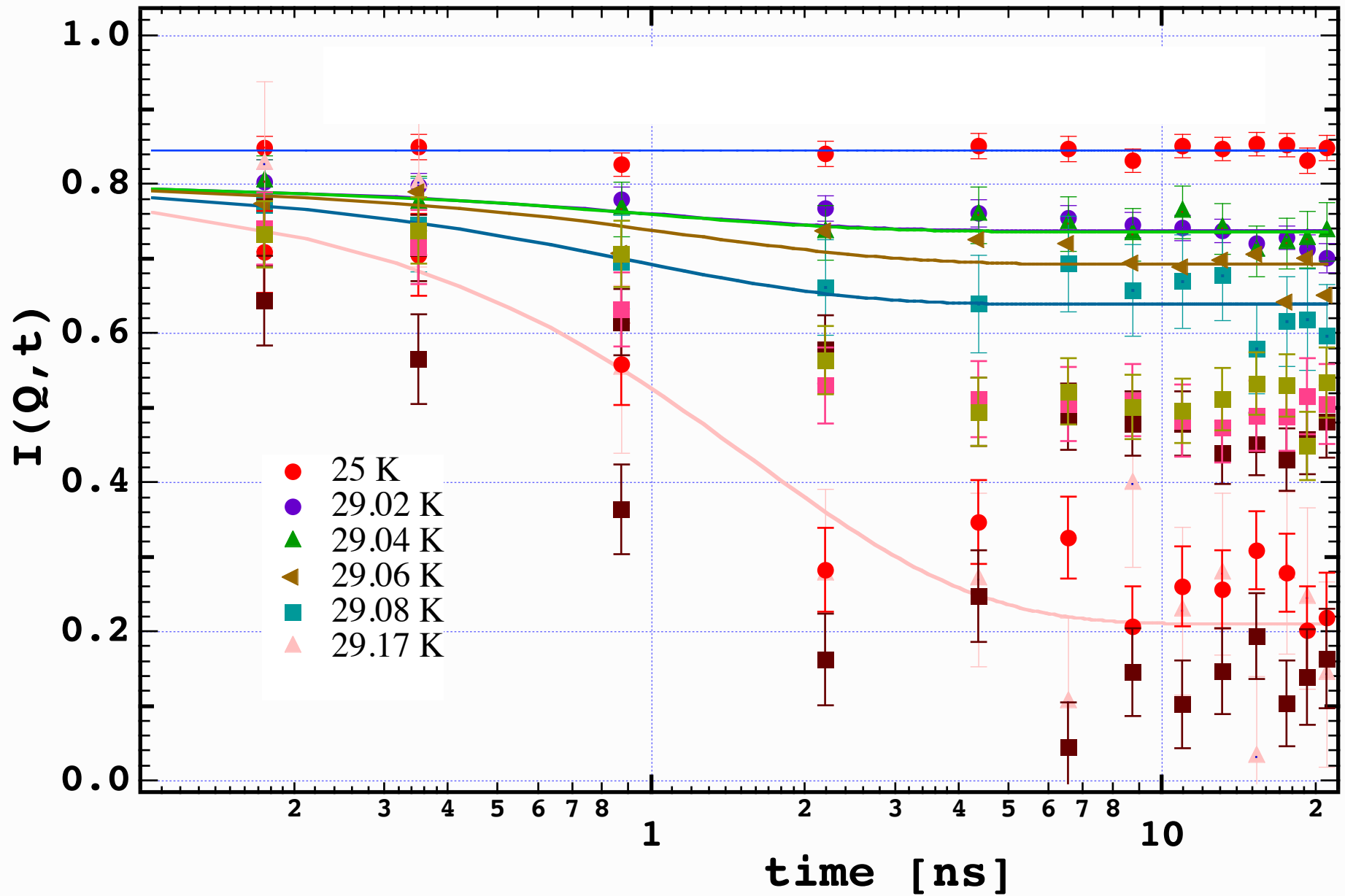
factor of 2 intensity loss



polarimetric neutron spin echo



chiral fluctuations in MnSi above T_c



Acknowledgments

Ferenc Mezei
Peter Falus
Peter Fouquet
Georg Ehlers
Bela Farago

Eddy Lelièvre Berna
Bob Cywinski
Ruth Pickup
Phillip Bentley
Sergey Grigoriev

Lars Bannenberg
Rob Dalgliesh
Fengjiao Qian
Charles Dewhurst

and you for your attention !