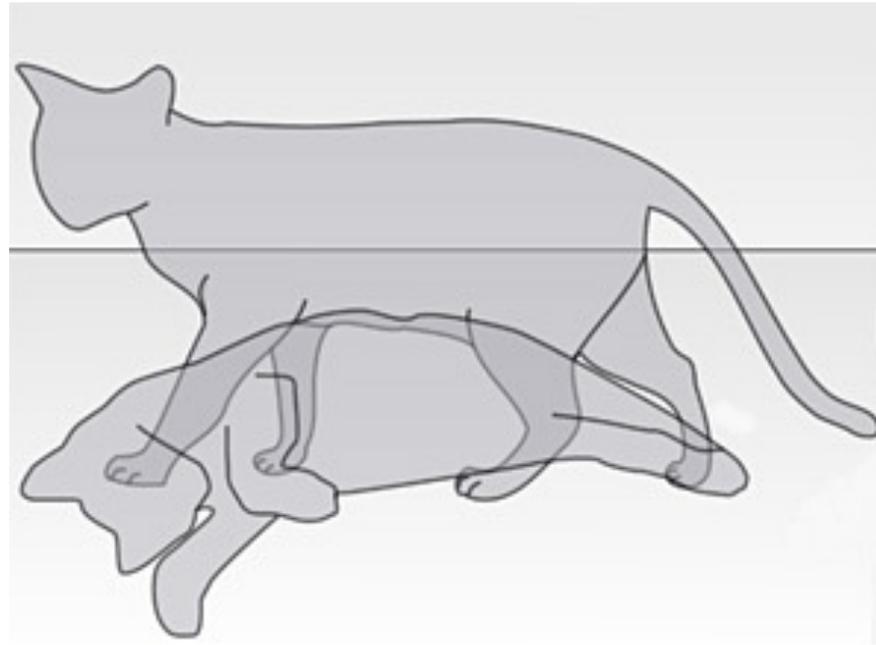


# Towards the Quantum Mechanical approach



Katia Pappas

# Classical Mechanics

Newton's law of motion

well defined particles and  
trajectories

deterministic

local realism

# Quantum Mechanics

Schrödinger equation

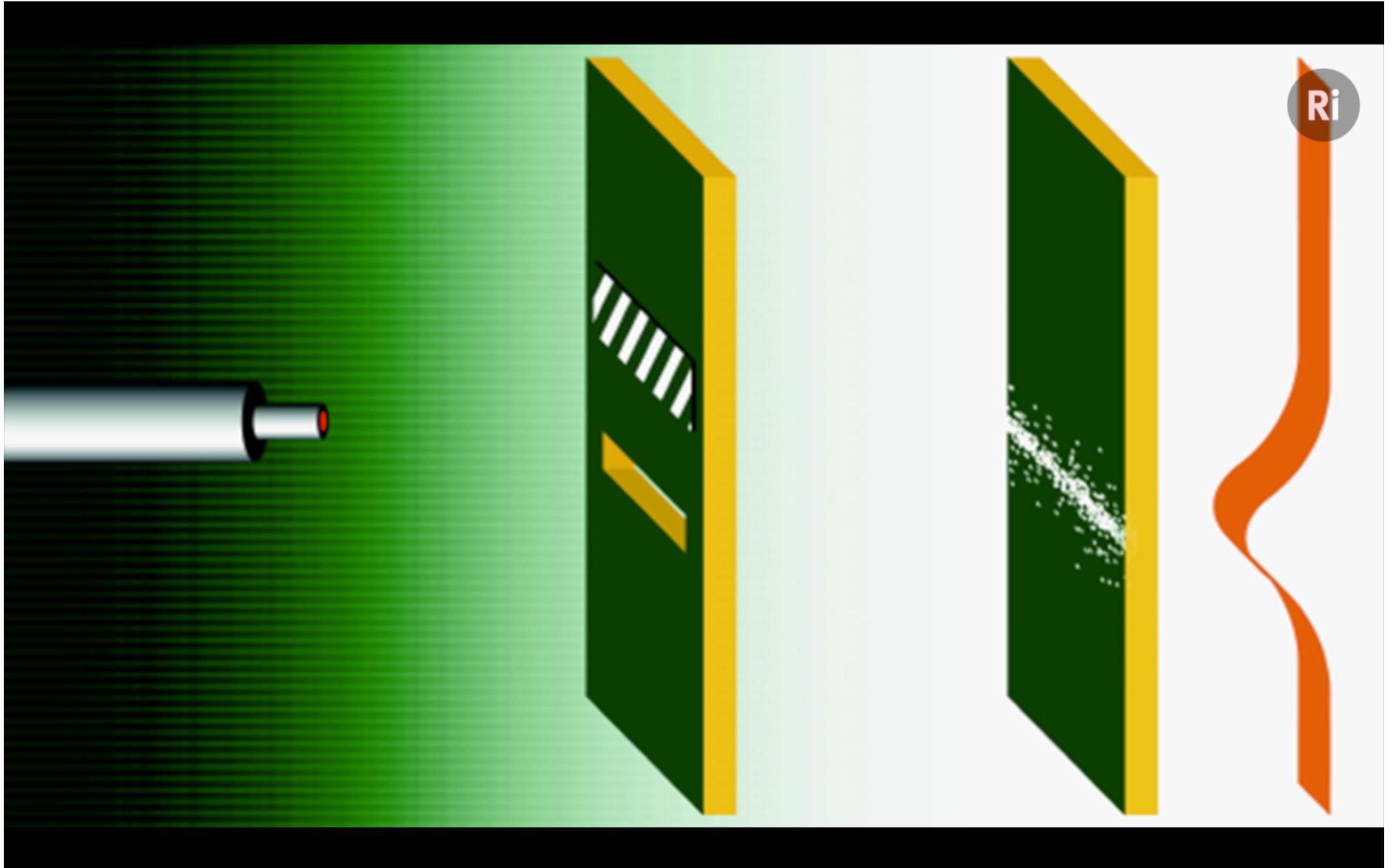
wave functions

probabilistic

quantum nonlocality

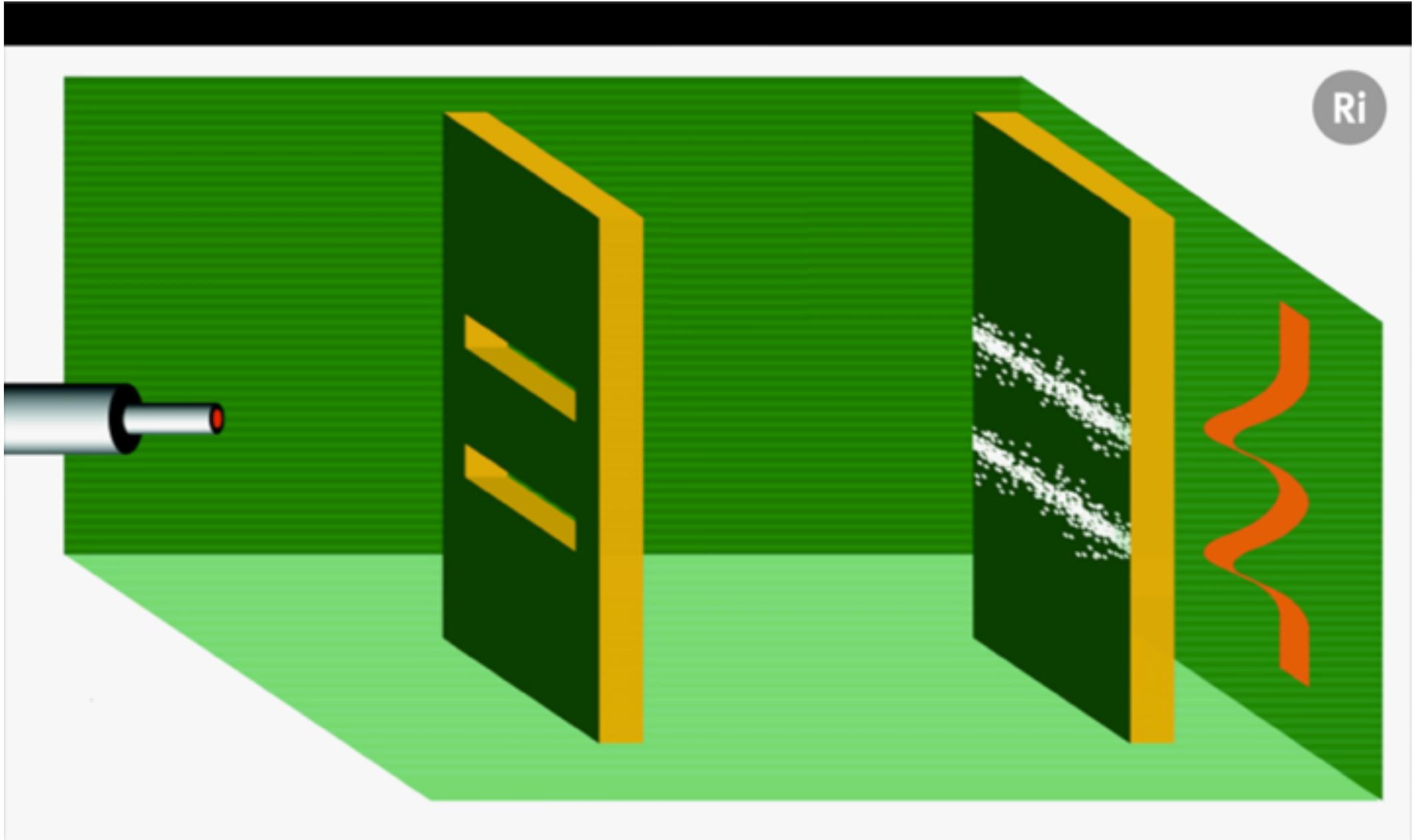
# Classical Particles



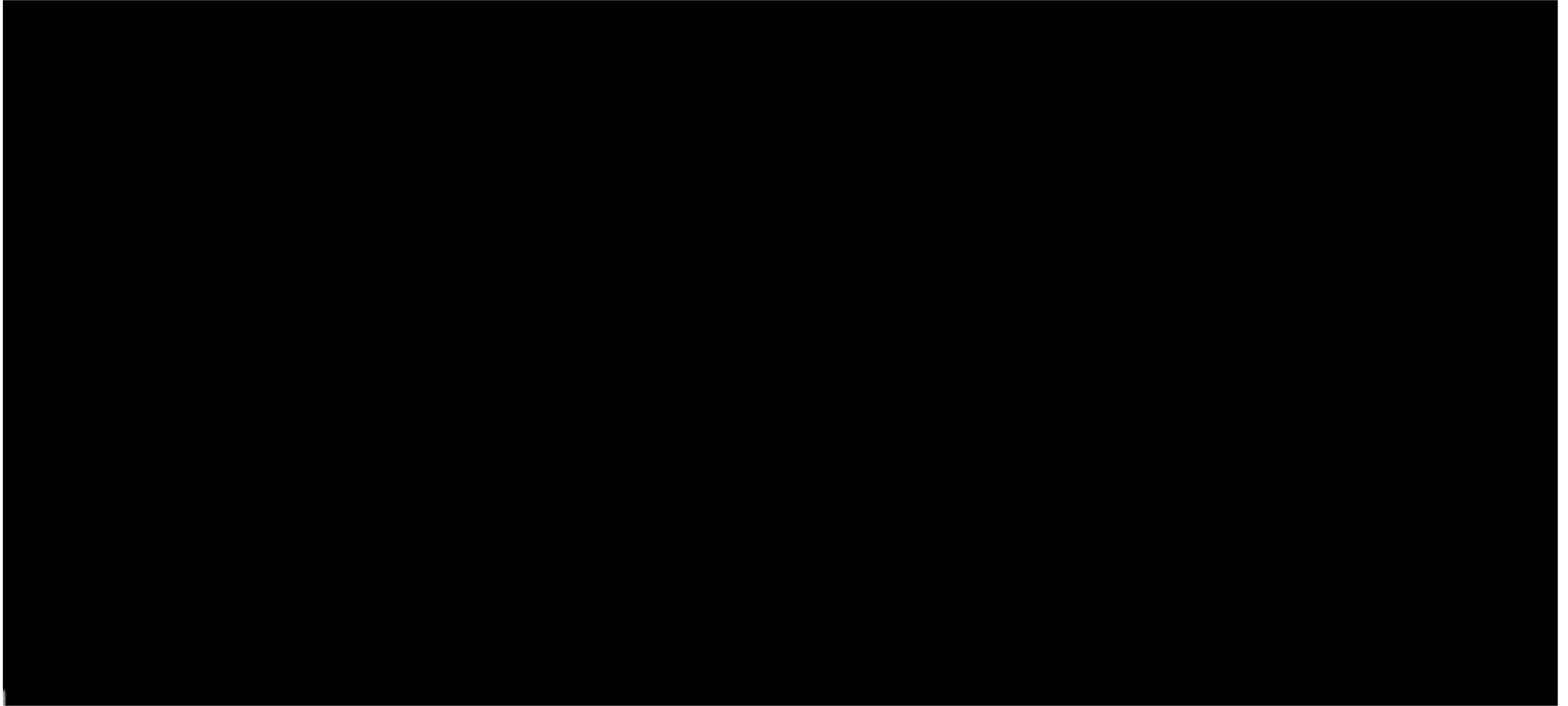


Double-slit experiment explained by Jim Al-Khalili

# Classical Particles

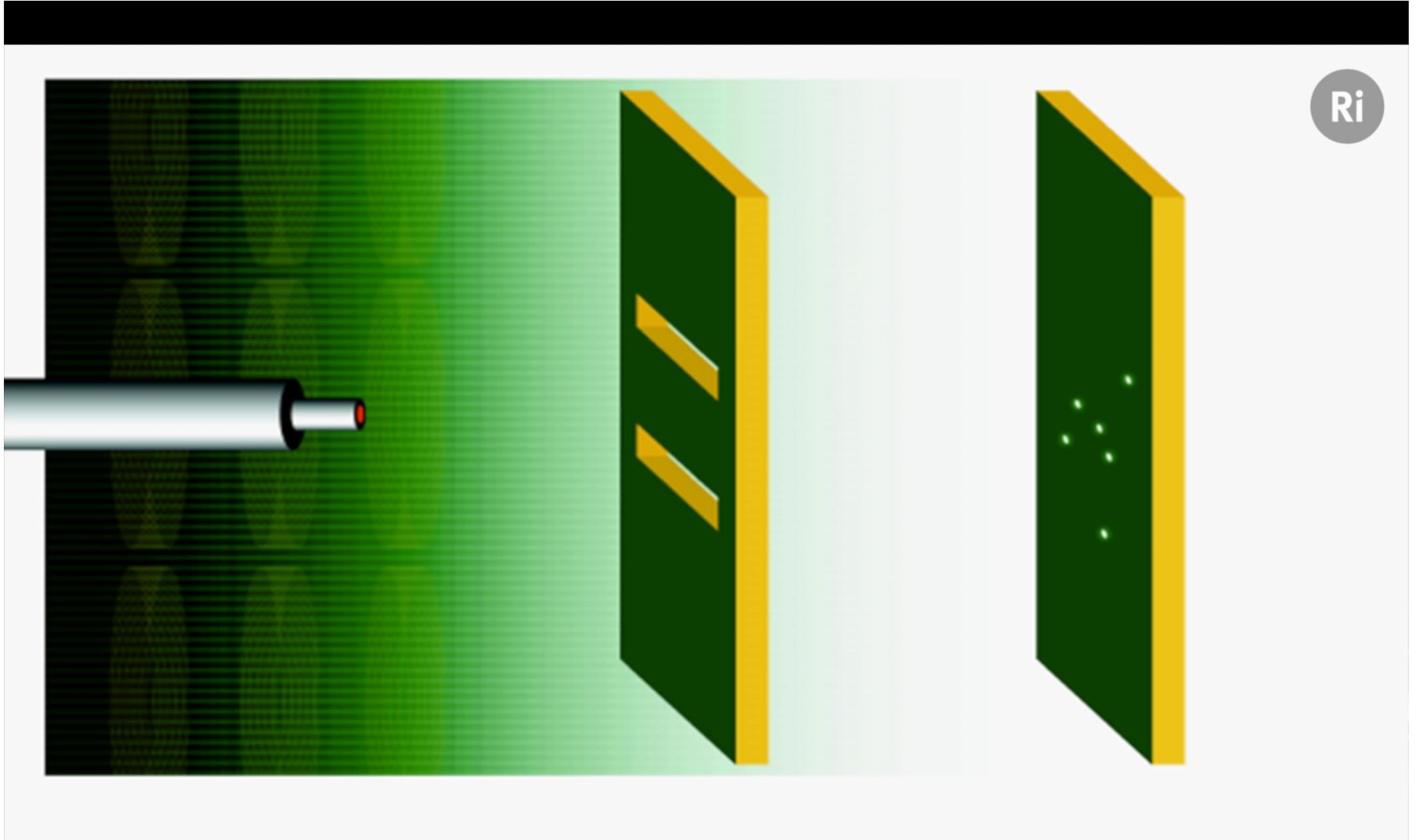


# Double-slit experiment with electrons

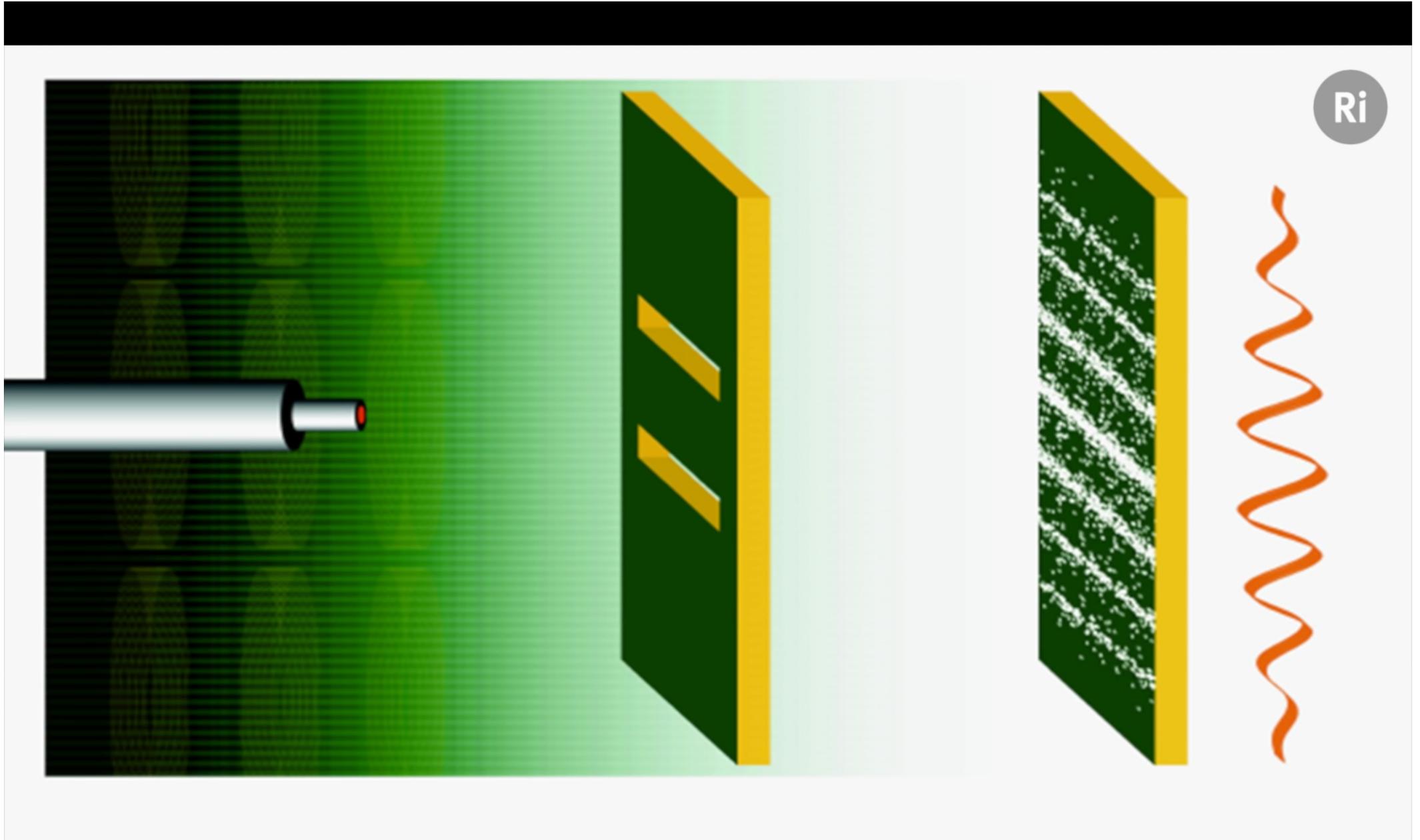


<http://iopscience.iop.org/article/10.1088/1367-2630/15/3/033018/meta>

# Quantum System



# Quantum System



## QUANTUM MECHANICS: **Probabilistic**

information from one particle is zero !!!

There is no such thing as

**polarisation or wave function** of one particle

The measurement is at the heart of the  
interpretation of QM

probabilistic

wave function collapses to its eigenstates

=> observables **e.g. the polarisation of a beam**

**Ehrenfest Theorem:**

**The observables of a QM system follow Newtons' law**

# QUANTUM MECHANICS: non local

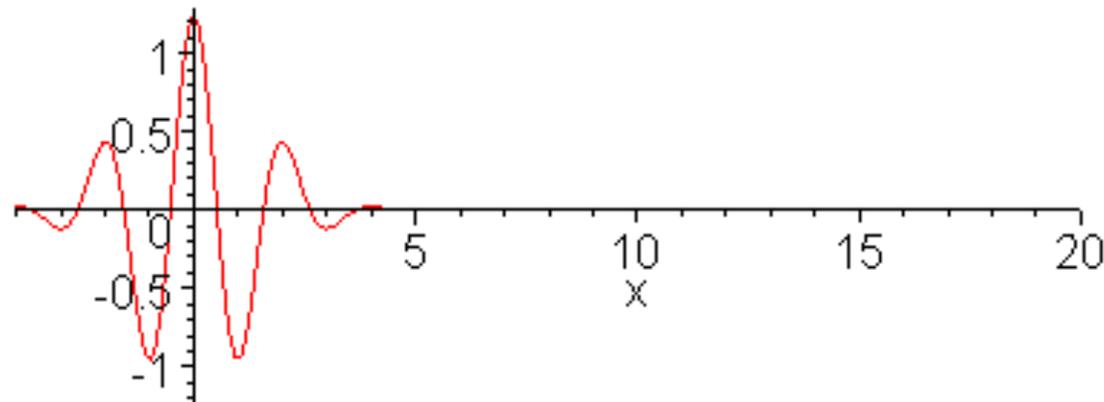
a particle can be everywhere in the universe !!!

Richard Feynman, Douglas Robb Lectures Auckland 1979  
available on Youtube, don't miss it !

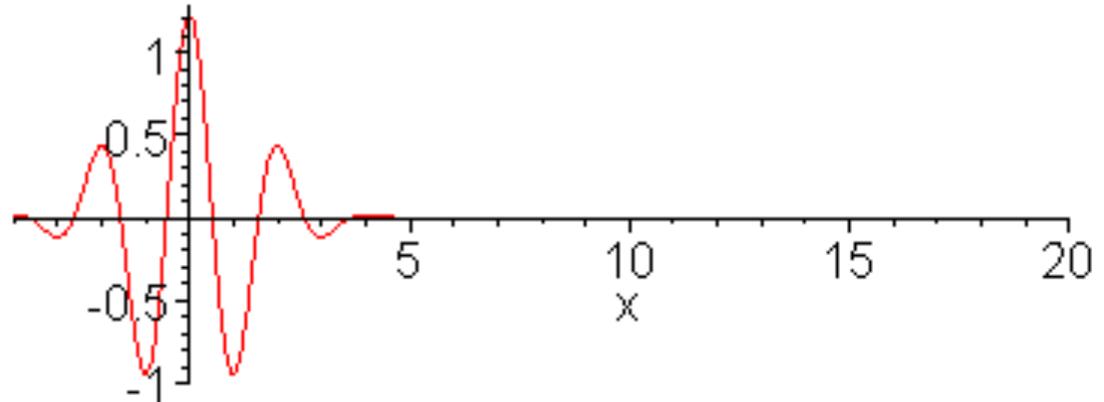
A way out: the wave packet

satisfies our classical thinking but not fundamental

because  
dispersive



absence of  
dispersion  
is a solitonic  
solution



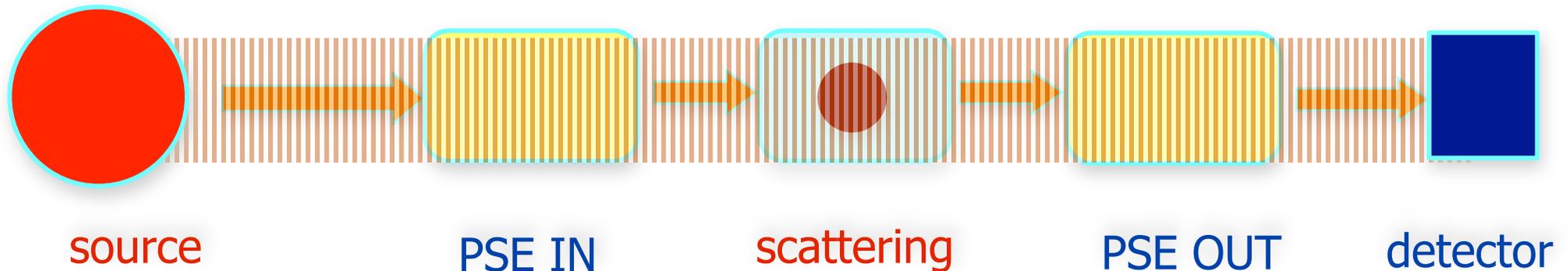
## **Neutron scattering : the beam defines a QM system leading to observables that can be understood by CM**

Between probabilistic scattering and absorption events one can consider that neutrons propagate deterministically as point like classical particles with “infinitely” well-defined trajectories  $r(t)$ , each carrying a classical magnetic moment with perfectly well-defined direction at any instance of time.

**we can optimise our instruments with ray tracing Monte Carlo simulation software e.g. McSTAS**

**at the origin of some confusion between CM and QM**

# Neutron scattering : the beam defines a QM system leading to observables that can be understood by CM

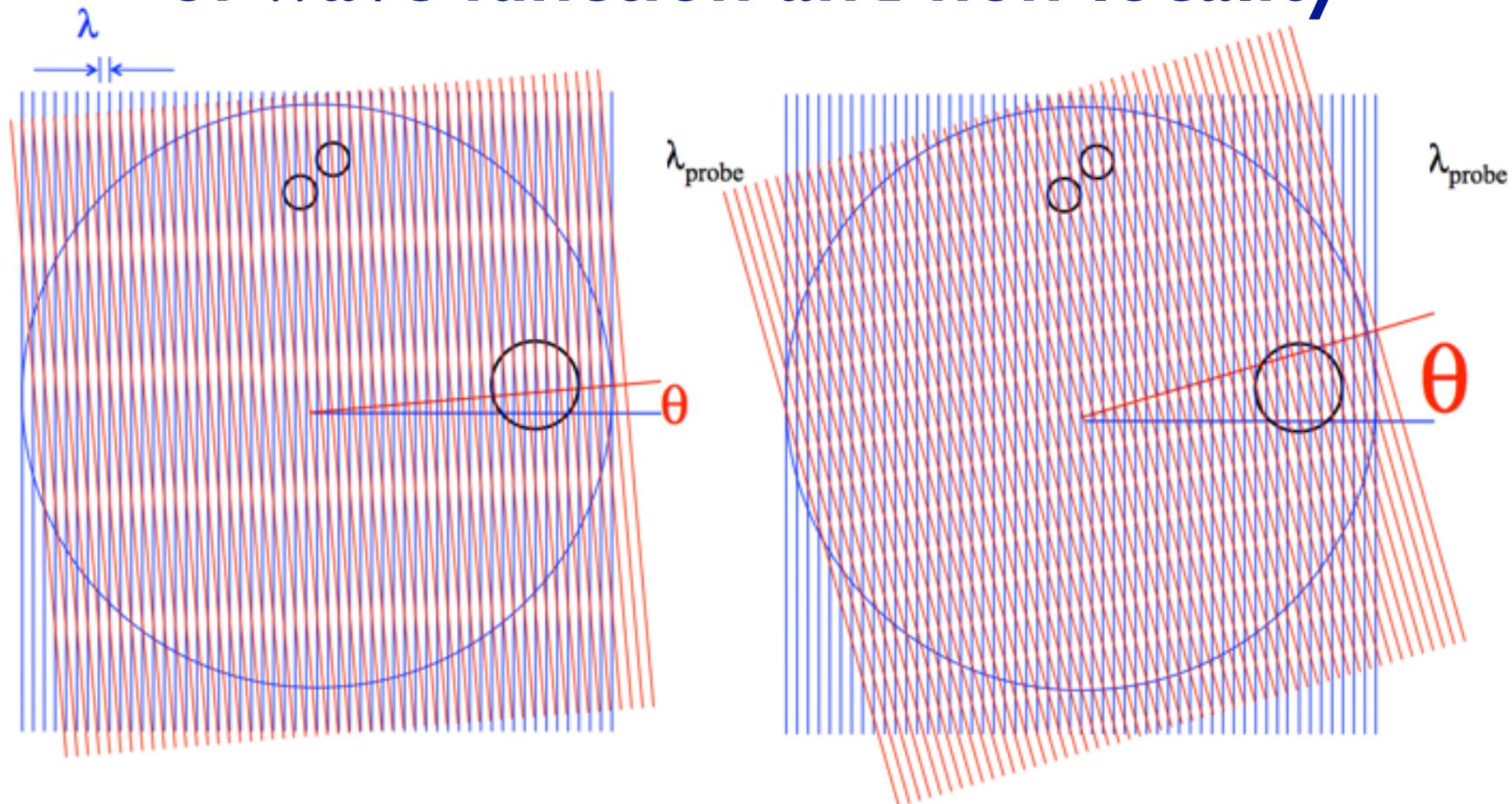


observables defining a neutron beam :  
Energy, polarisation, wave vector, position of the beam  
etc

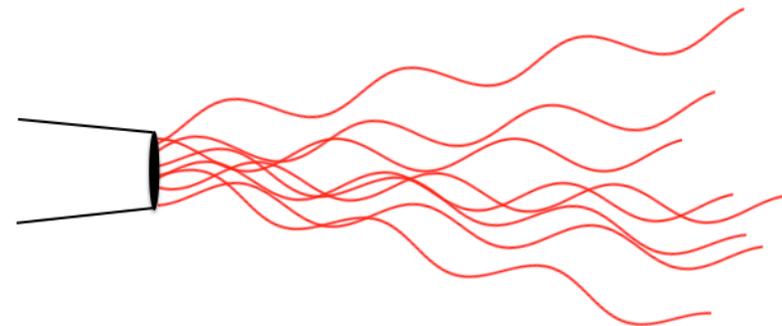
but interference phenomena, like scattering or the  
doubt slit experiment, are purely QM  
and cannot be understood by CM.

but interference phenomena, like scattering or the double slit experiment, are purely QM and cannot be understood by CM.

their understanding require the concepts of wave function and non-locality



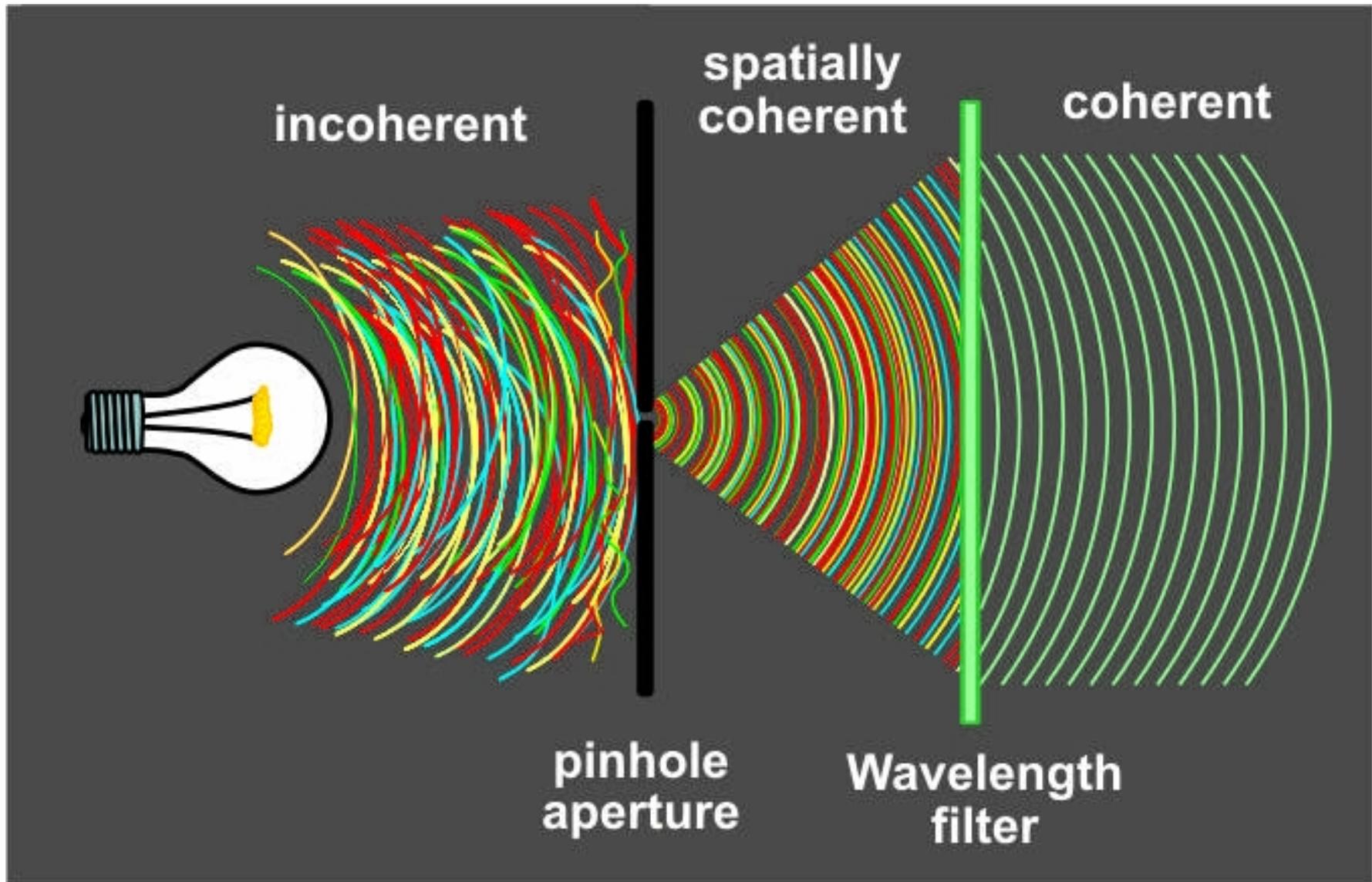
Coherent Laser Light



Incoherent LED Light

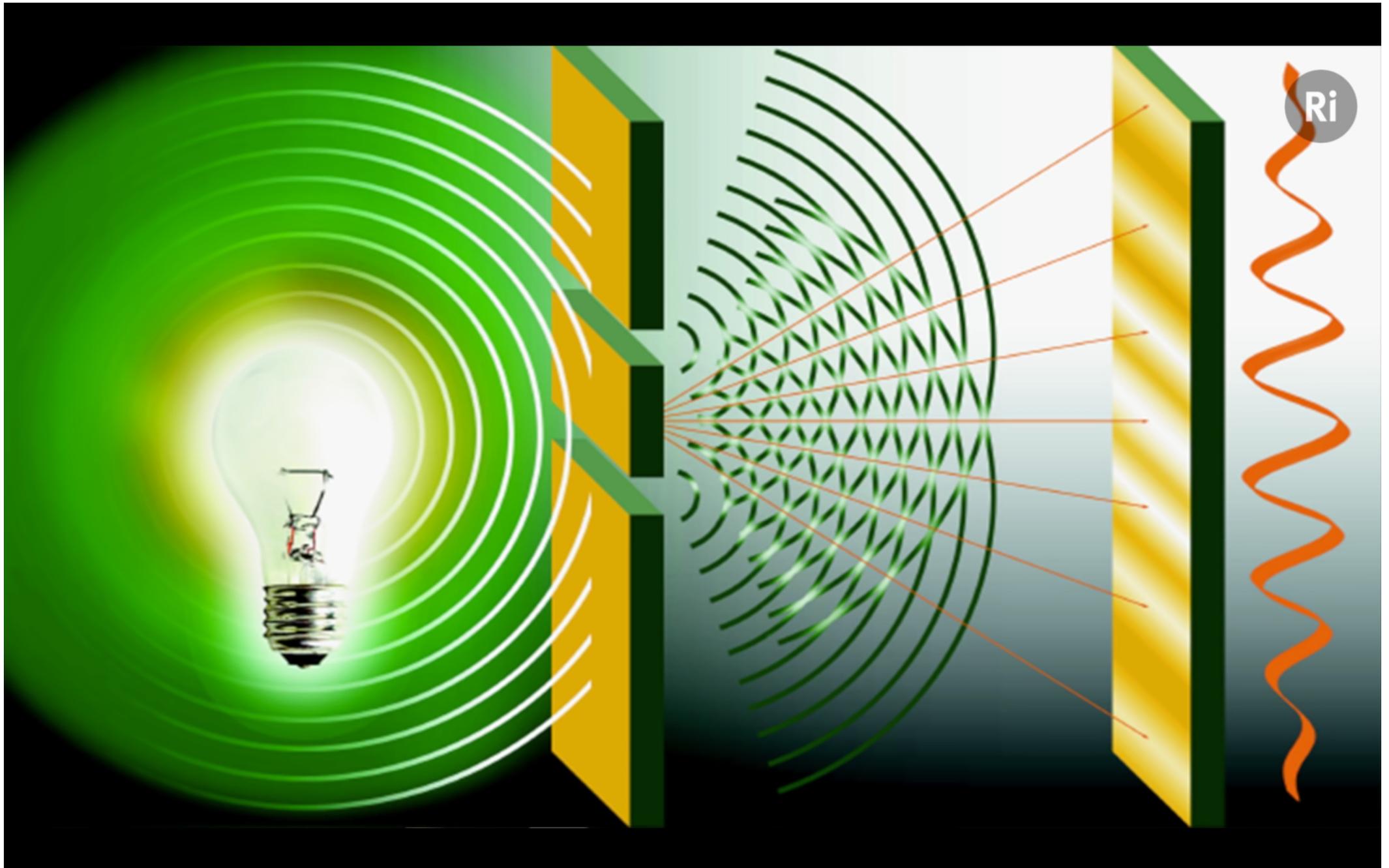


Miridia Technology Inc

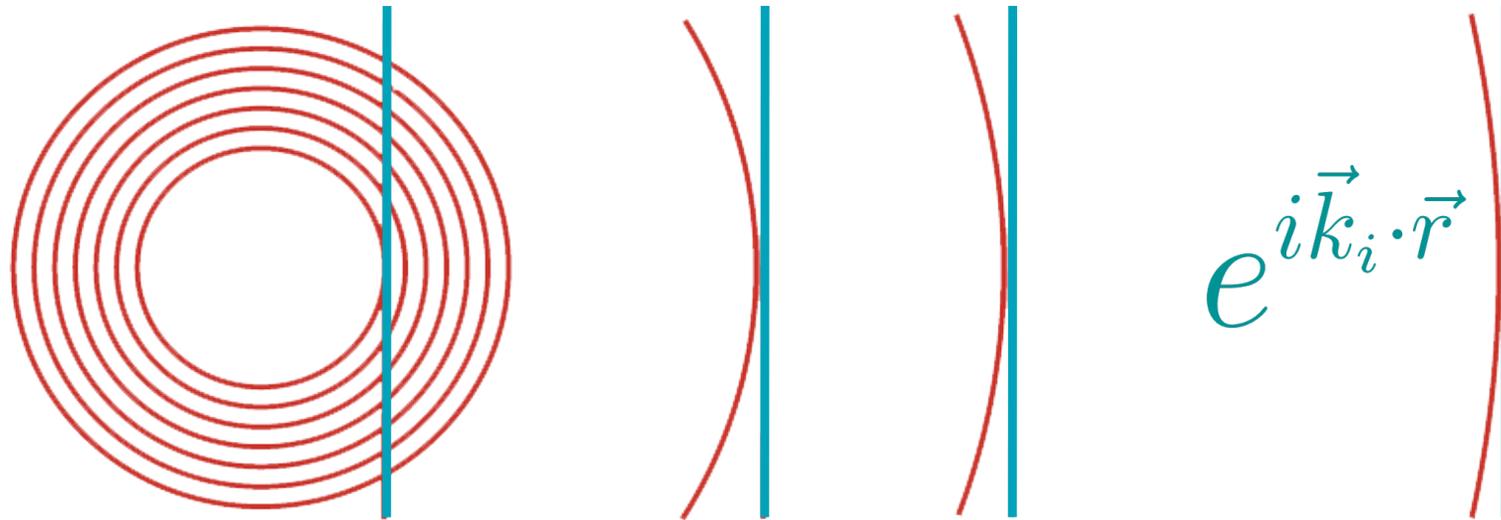


<http://amasci.com>

# Double-slit experiment explained by Jim Al-Khalili



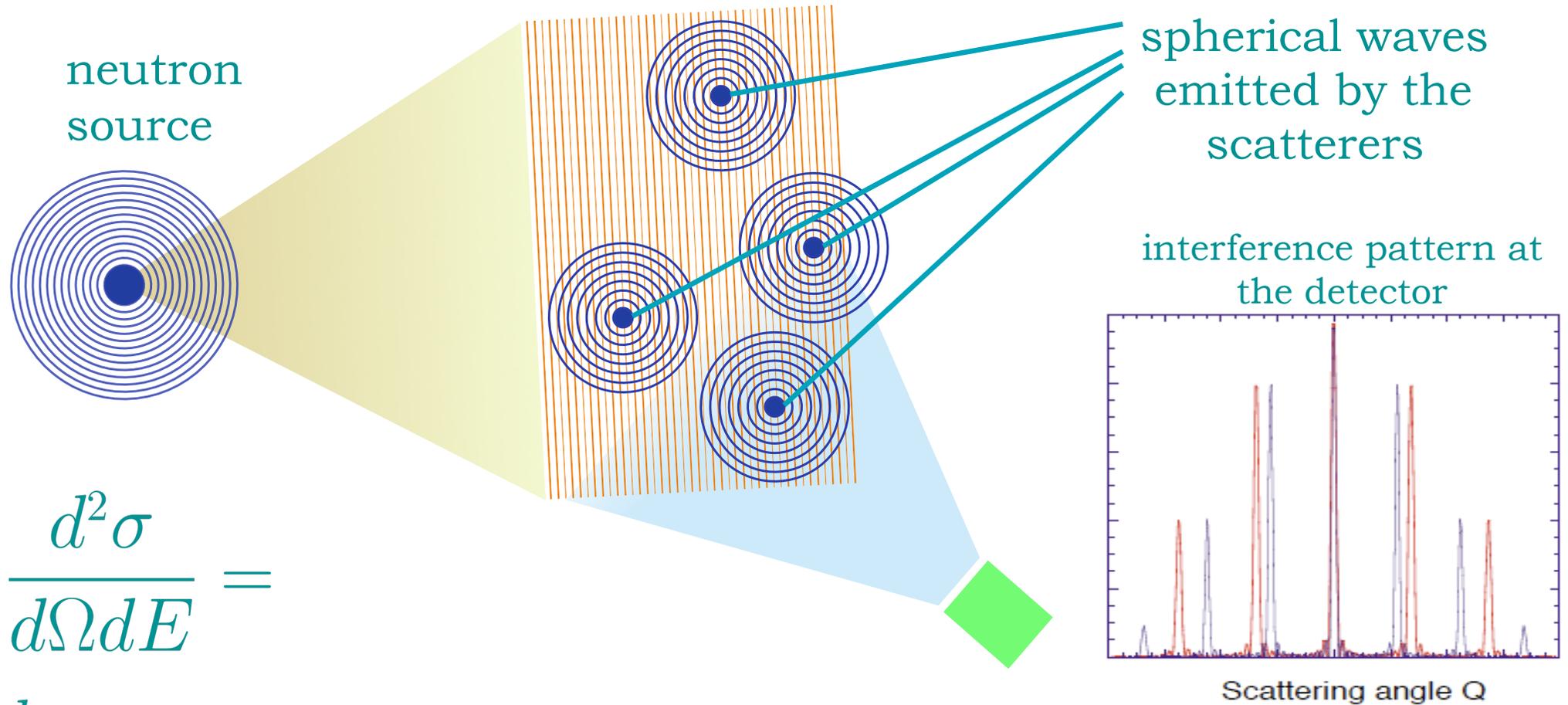
# Neutron scattering : waves and particles



at sufficiently large distances from the source the neutron beam may be approximated by a plane wave

Everything ever observed can be explained by identifying “one neutron” with an infinite plane wave and classically (incoherently) averaging over the beam

# Neutron scattering : waves and particles

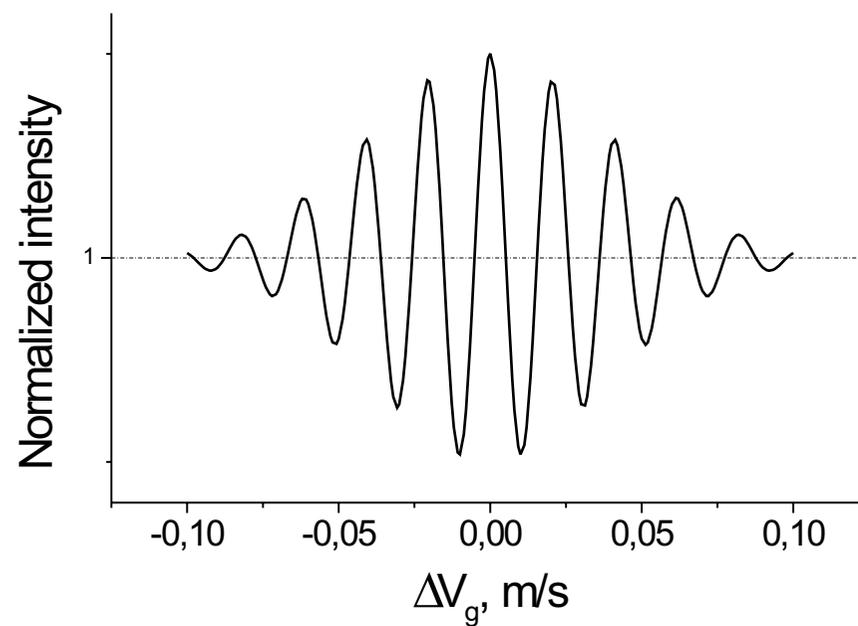
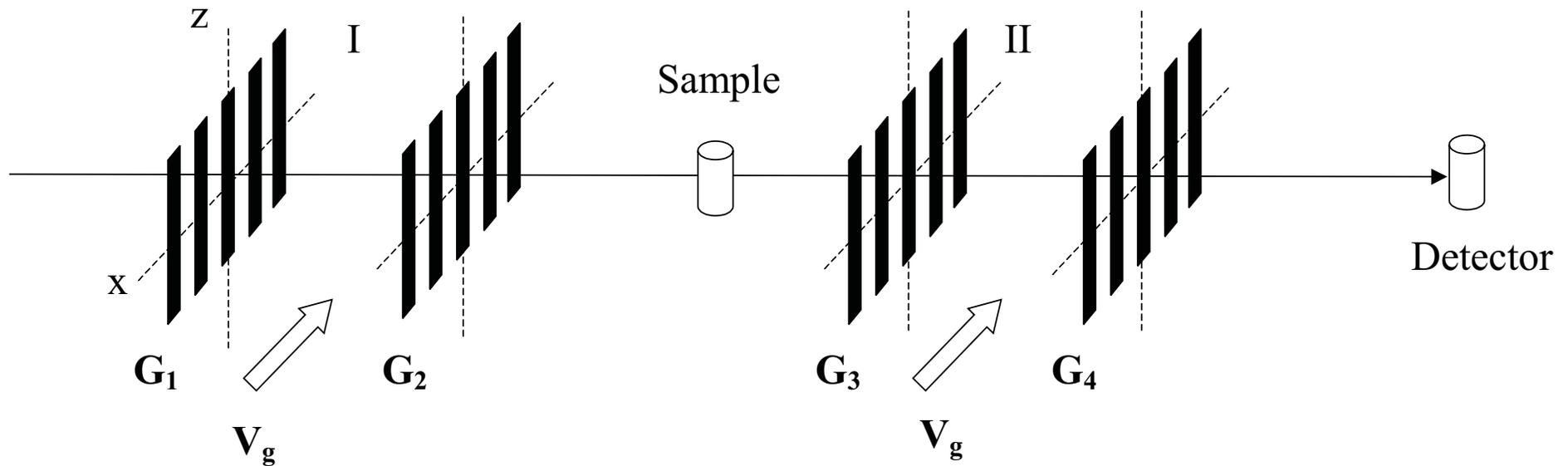


$$\frac{d^2\sigma}{d\Omega dE} =$$

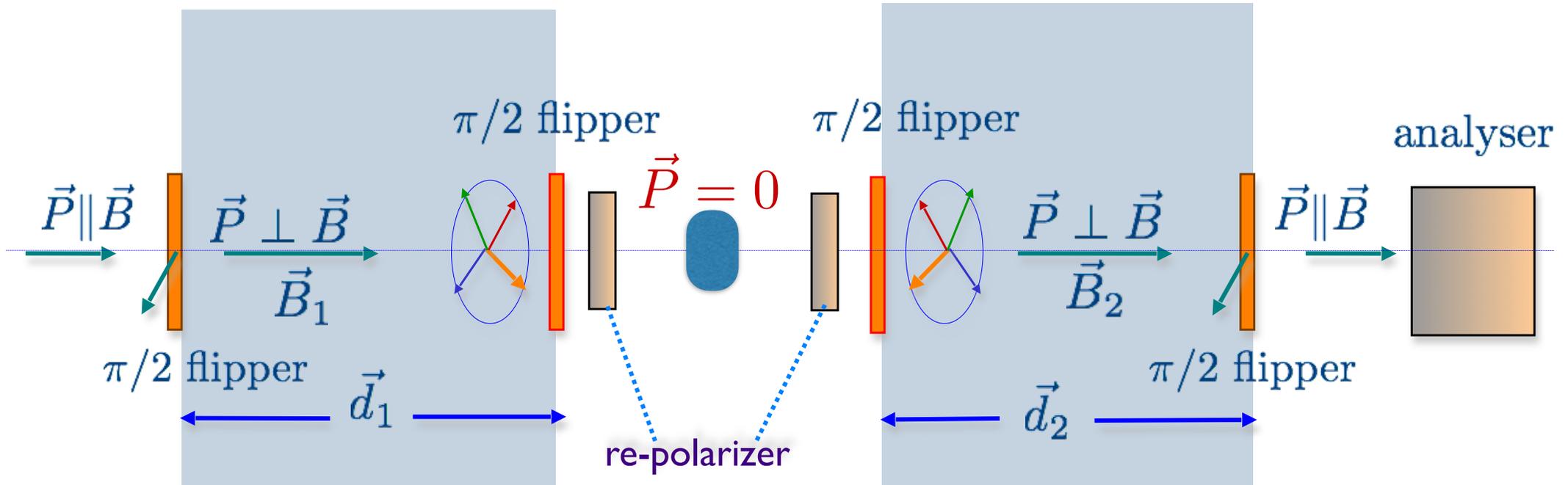
$$\frac{k_f}{k_i} \sum_{\lambda_i, \lambda_f} p_{\lambda_i} |\langle \vec{k}_f \sigma_f; \lambda_f | V | \vec{k}_i \sigma_i; \lambda_i \rangle|^2 \delta(\hbar\omega + E_{\lambda_i} - E_{\lambda_f})$$

# Neutron Speed Echo (A. Ioffe 2003)

$\sim$  NSE



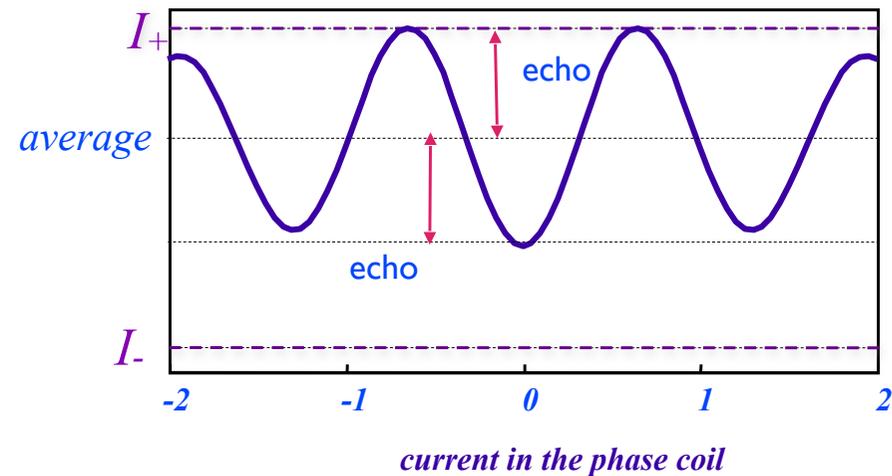
# intensity modulated neutron spin echo



ideally

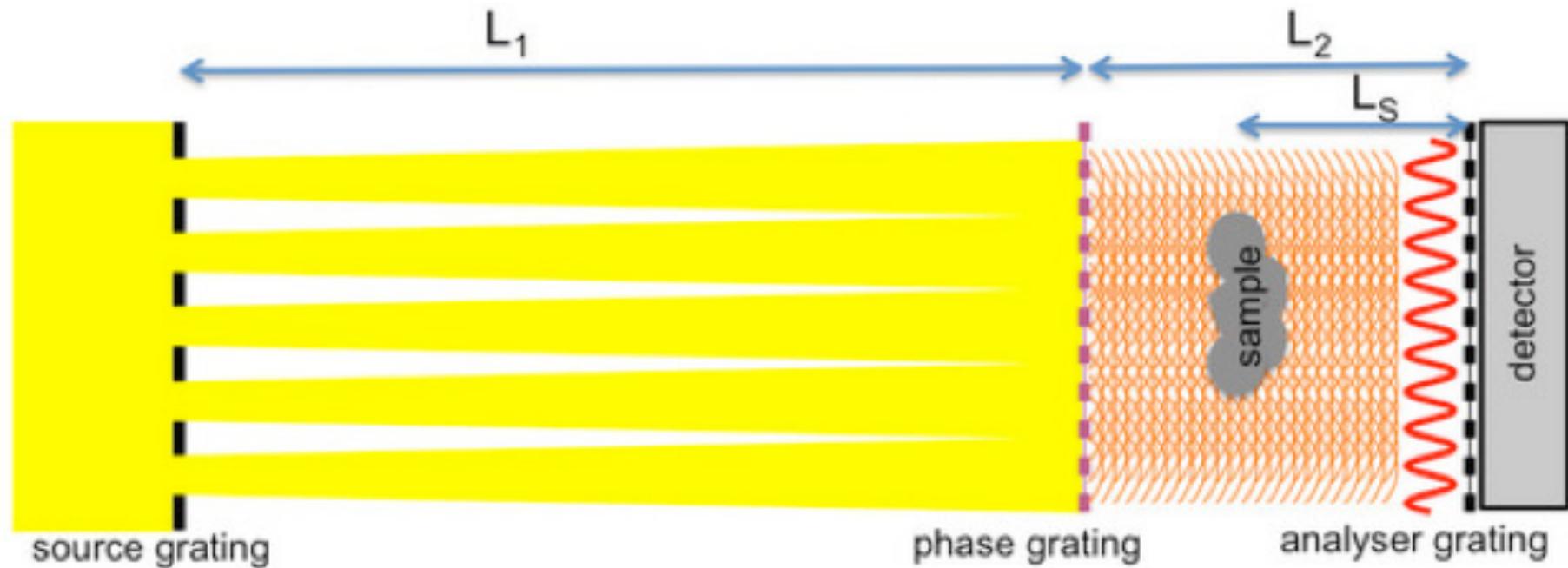
$$\text{echo modulation} = (I_+ - I_-) / 3$$

$$\text{for } |\vec{P}| = 1$$

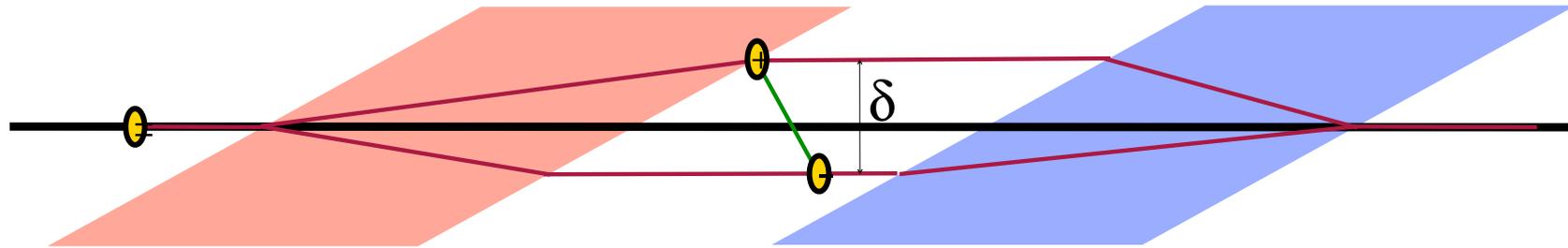


# Talbot Lau grating interferometer for dark-field contrast imaging (M. Scrobl 2014)

~ SESANS

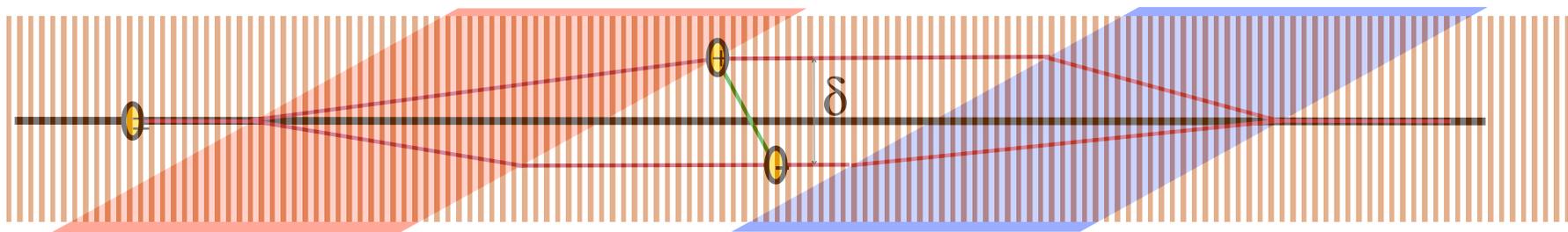


# semi-classical illustration of the phase difference of the components of the wave function in SESANS



IT IS WRONG TO ASSOCIATE THIS PHASE SHIFT TO THE WAVEFUNCTION OF A SINGLE NEUTRON !

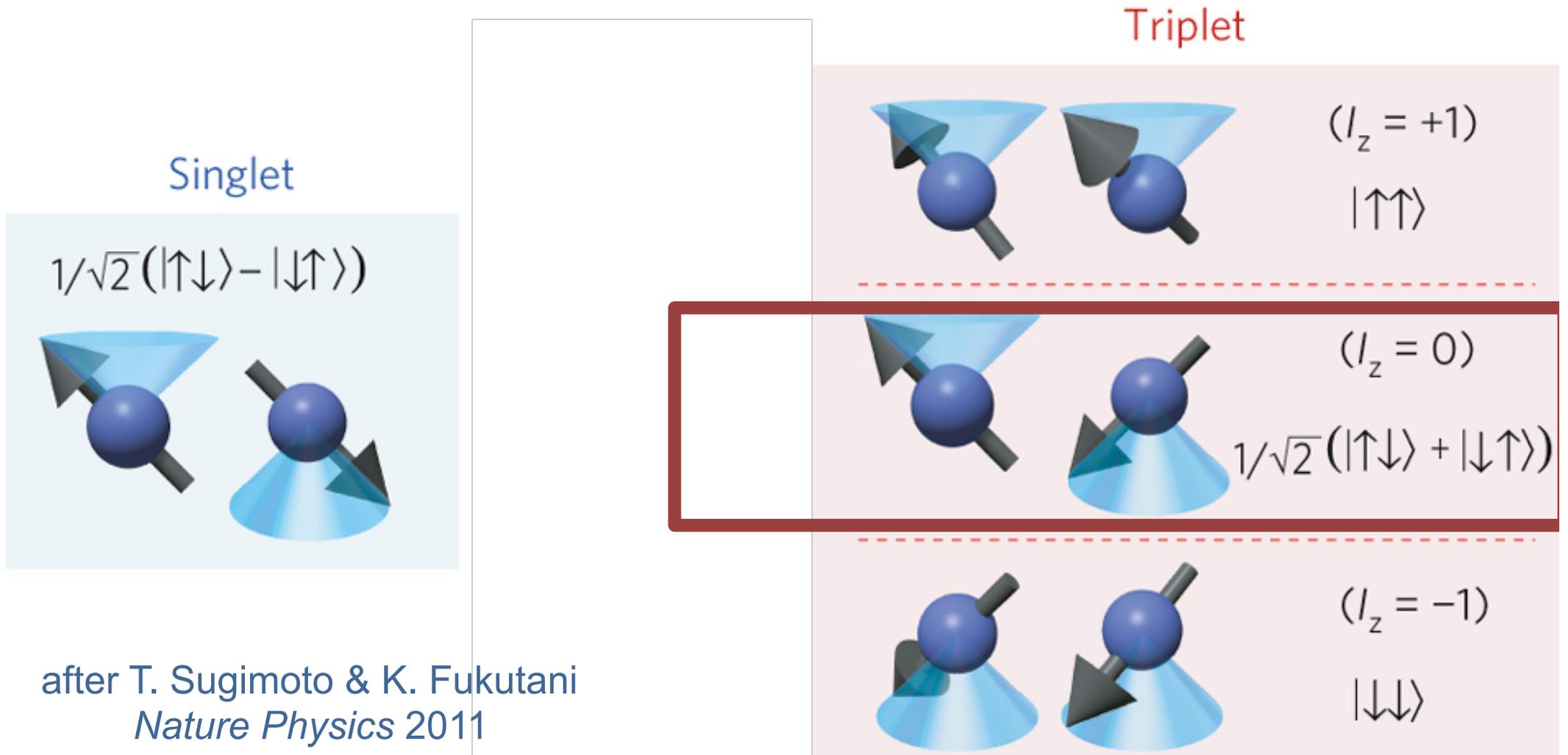
**The correct QM Approach must respect quantum nonlocality within the neutron beam**



**beam dimensions/splitting  $\sim 10^{-4}$  mm  $\Rightarrow$  effect negligible**

how can we understand the coherent superposition of eigenstates for a spin 1/2 ?

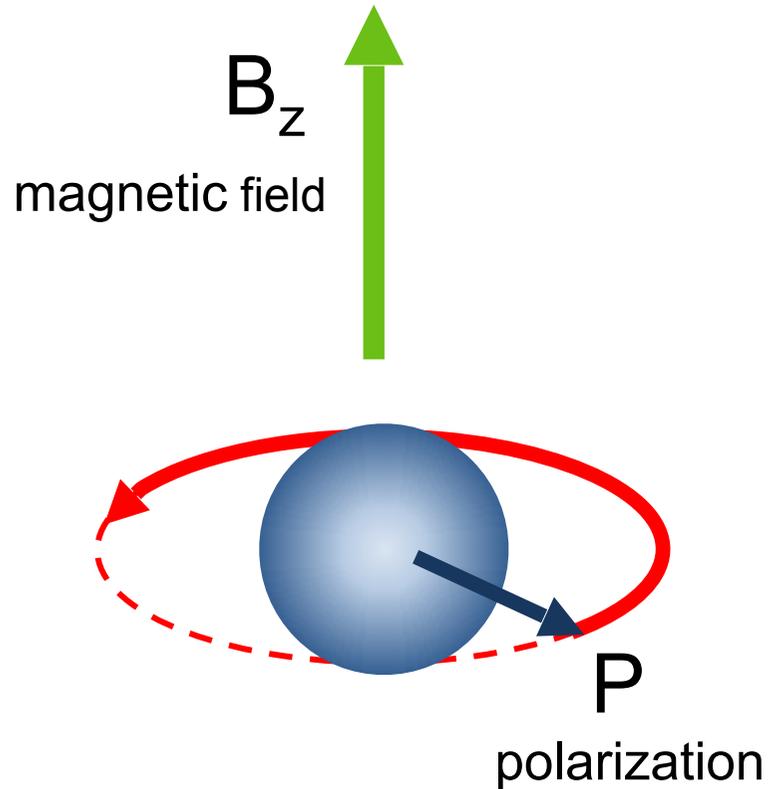
we consider the situation of spin 1



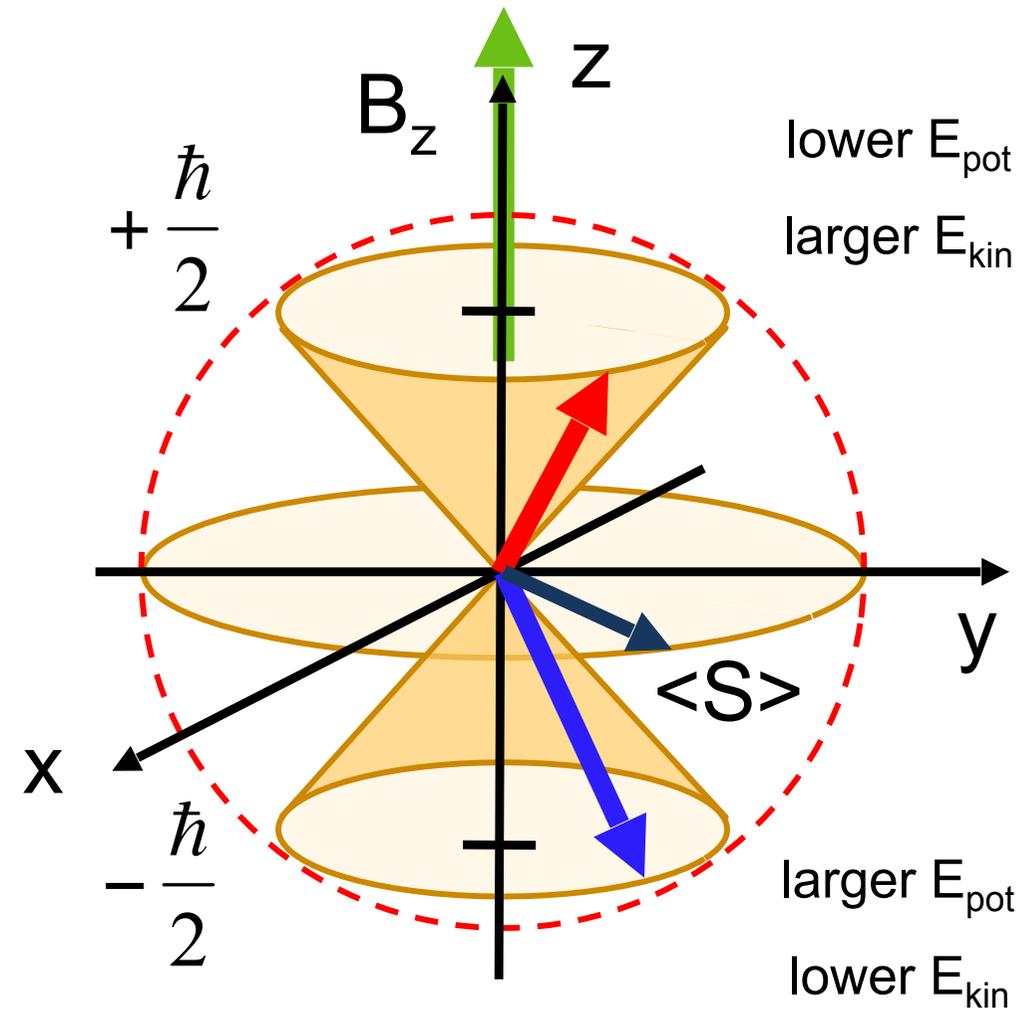
after T. Sugimoto & K. Fukutani  
*Nature Physics* 2011

# Spin Precession of Neutrons

## classical mechanics



## quantum mechanics

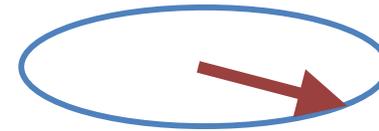


In B-field: spin up state speeds up; spin down state slows down

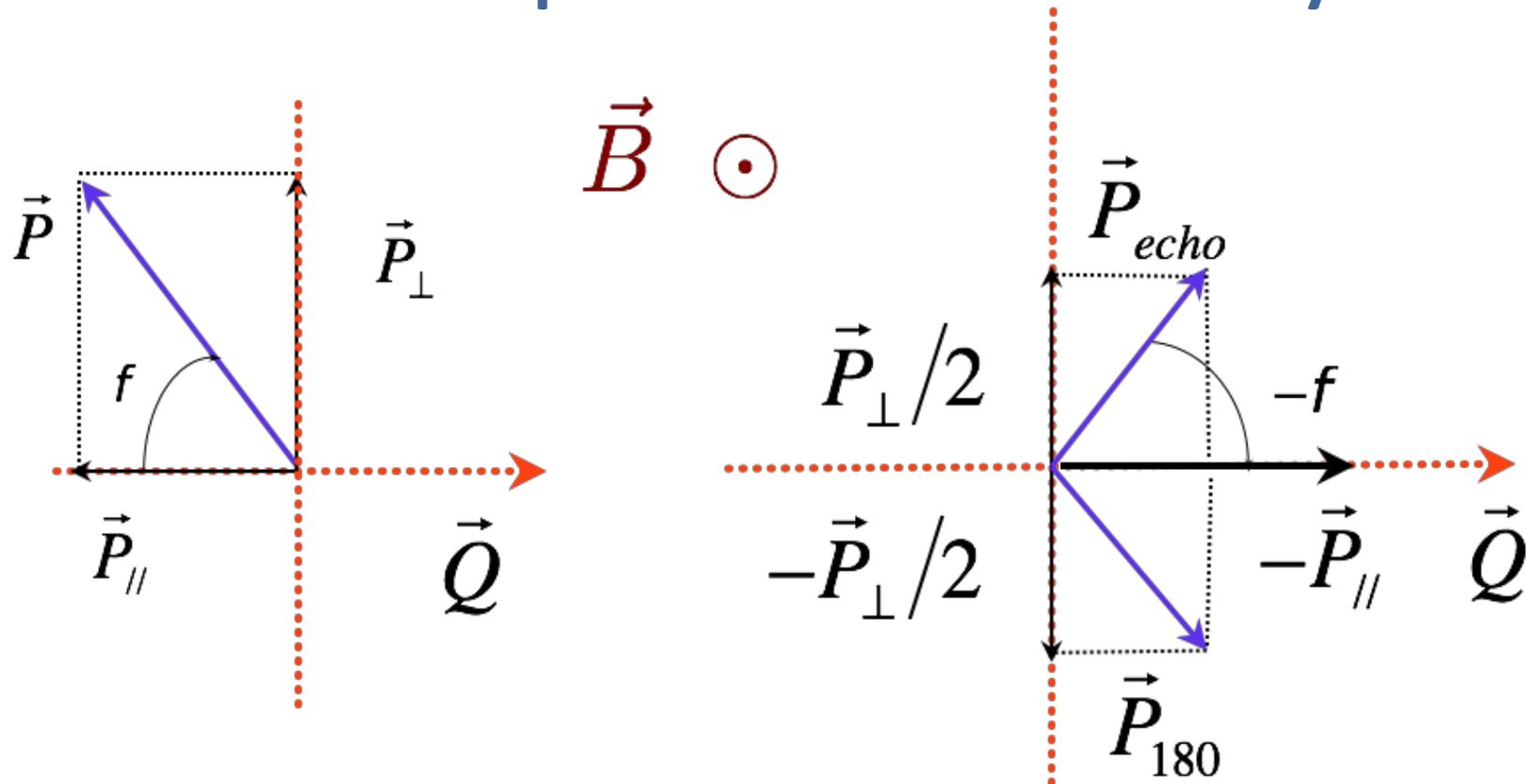
# Anton Zeilinger plenary talk at ECNS 2013, Prague :



QM



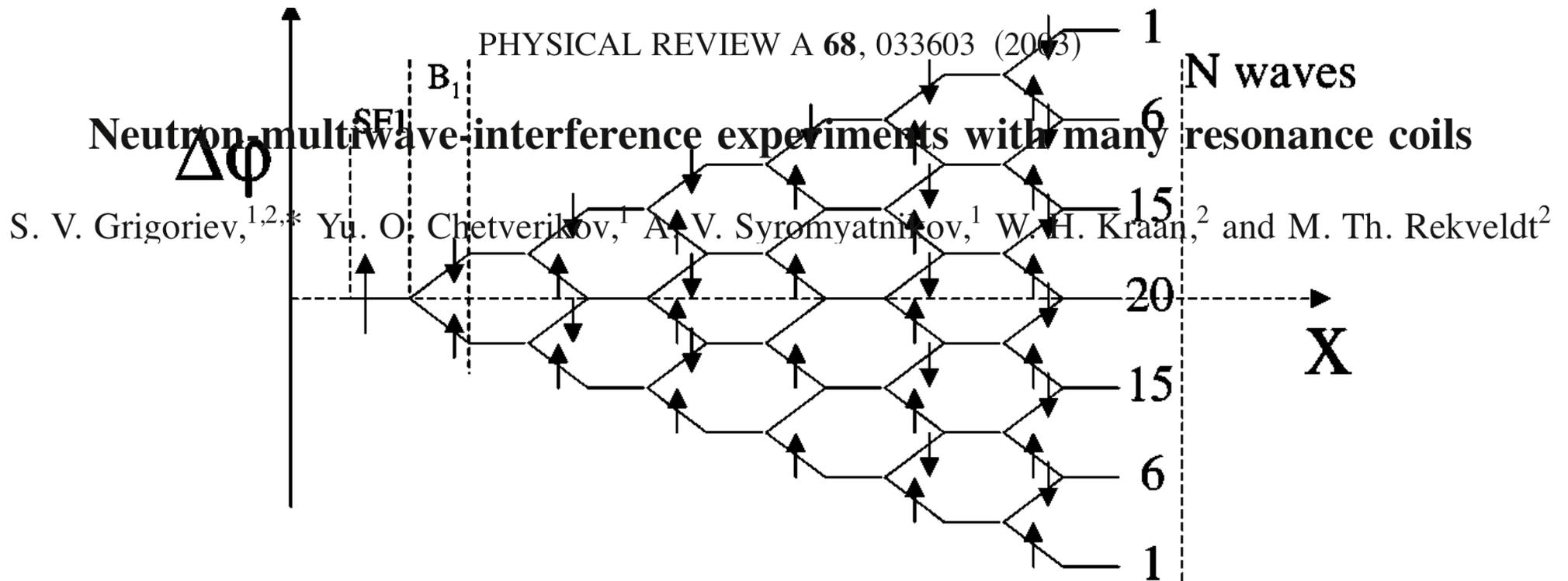
confirmed by the selection rules for magnetic scattering  
at the sample discussed on Monday



# BE AWARE !

Mixing up CM and QM can lead to wrong conclusions

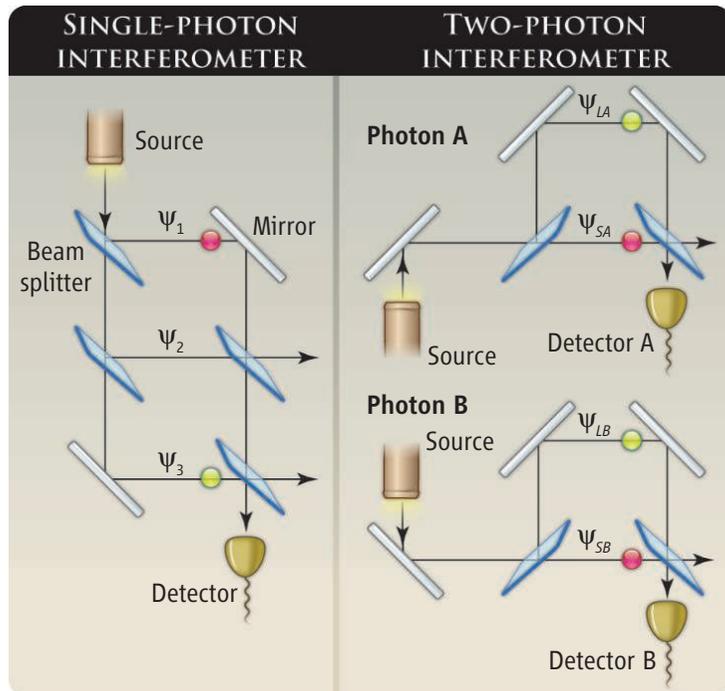
It has been suggested that it is possible to change the scattering process by adding an RF flipper in the beam



**BE AWARE !**

**Mixing up CM and QM can lead to wrong conclusions**

**scattering probes pair correlation functions because  
quantum interference is ruled by pair correlation functions**



**Quantum interference between many different pathways is simply the sum of the effects from all pairs of pathways.**

**Sinha et al. Science 329, 418 (2010)**

**any other assumption would violate  
Bell's theorem**

**J. D. Franson Science 2010**

**10.1126/science.1192624**

# be suspicious of deterministic approaches to Quantum Mechanics

it is a strange theory of light and matter (Feynman)