

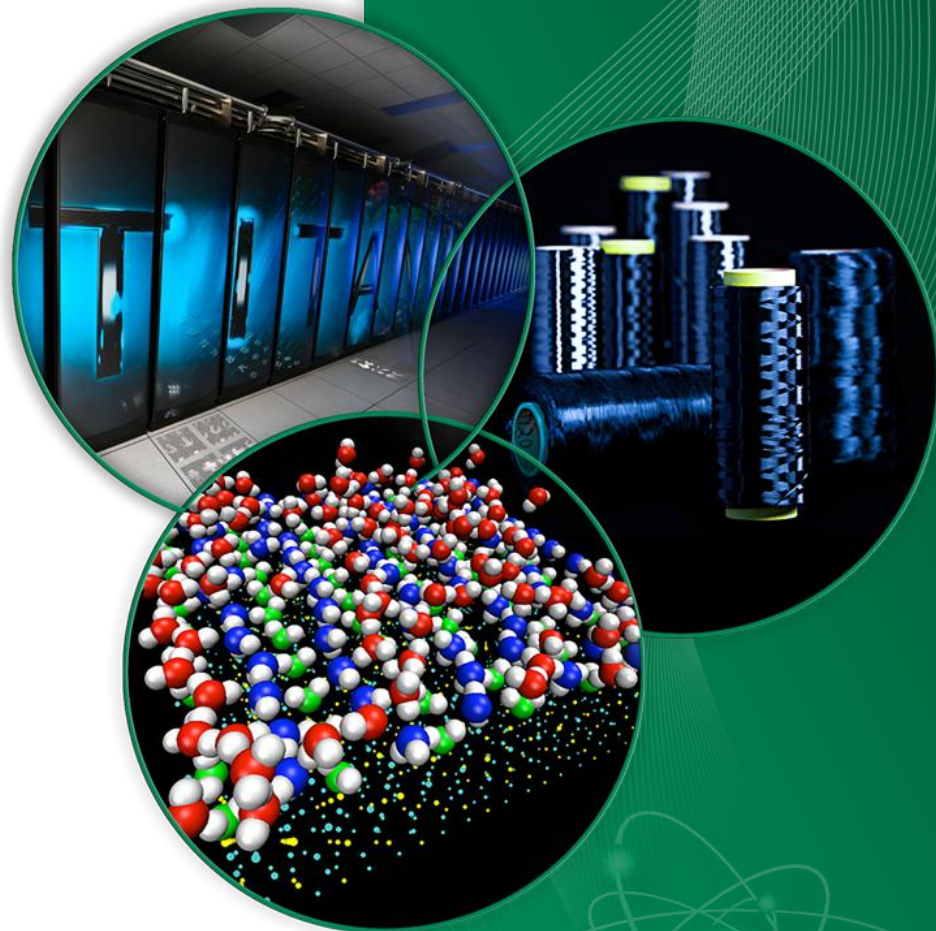
# Quasielastic neutron scattering, neutron backscattering technique, BASIS and beyond

## Part I: quasielastic neutron scattering

Eugene Mamontov

Neutron Sciences Directorate  
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Erice School “Neutron Science and Instrumentation”  
July 4 – July 13, 2018



# Inelastic neutron scattering in just one slide

Measure scattering intensity as a function of  $Q$  and  $\omega$

$\omega = 0 \rightarrow$  elastic

$\omega \neq 0 \rightarrow$  inelastic

$\omega$  near 0  $\rightarrow$  quasielastic

scattered neutron  detector

Neutron momentum:  $k = \frac{2\pi}{\lambda}$

Neutron energy:  $E = \frac{(\hbar k)^2}{2m_n}$

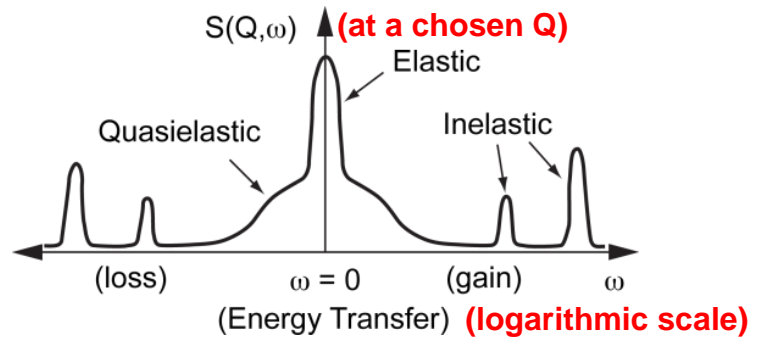
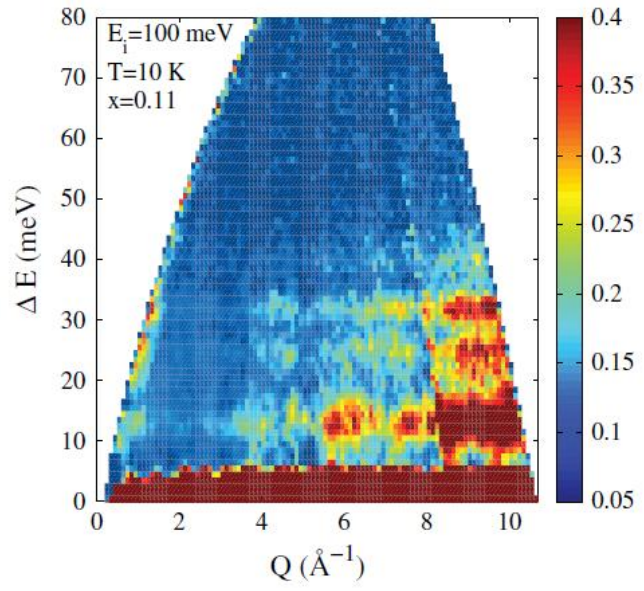
$\vec{k}_f$

$\vec{k}_i$

incident neutron

Momentum transfer:  $\vec{Q} = \vec{k}_i - \vec{k}_f$

Energy transfer:  $\hbar\omega = E_i - E_f$



**Quasielastic neutron scattering (QENS) is a special case of inelastic neutron scattering with small energy transfers, usually probing diffusion and relaxation phenomena**

PRL 101, 157004 (2008) PHYSICAL REVIEW LETTERS week ending 10 OCTOBER 2008

Phonon Density of States of LaFeAsO<sub>1-x</sub>F<sub>x</sub>

A. D. Christianson,<sup>1</sup> M. D. Lumsden,<sup>1</sup> O. Delaire,<sup>2</sup> M. B. Stone,<sup>1</sup> D. L. Abernathy,<sup>1</sup> M. A. McGuire,<sup>1</sup> A. S. Sefat,<sup>1</sup> R. Jin,<sup>1</sup> B. C. Sales,<sup>1</sup> D. Mandrus,<sup>1</sup> E. D. Mun,<sup>3</sup> P. C. Canfield,<sup>3</sup> J. Y. Lin,<sup>2</sup> M. Lucas,<sup>2</sup> M. Kresch,<sup>2</sup> J. B. Keith,<sup>2</sup> B. Fultz,<sup>2</sup> E. A. Goremychkin,<sup>4,5</sup> and R. J. McQueeney<sup>3</sup>

July 7, 2018

# There are few QENS-capable spectrometers in the US...

Scattering technique is not the same as neutron instrumentation technique

Quasielastic neutron scattering concerns small energy transfers between neutrons and the sample

Backscattering is a special high energy-resolution technique often used for QENS...not the only one

In principle, QENS data can be collected on any inelastic spectrometer... even a triple-axis!

**Backscattering** spectrometers – specifically designed for QENS, **disk chopper** spectrometers – often can be used for QENS too

Disk Chopper Spectrometer (**DCS**), NIST Center for Neutron Research

High Flux Backscattering Spectrometer (**HFBS**), NIST Center for Neutron Research

Cold Neutron Chopper Spectrometer (**CNCS**), SNS, ORNL

Backscattering Spectrometer (**BASIS**), SNS, ORNL

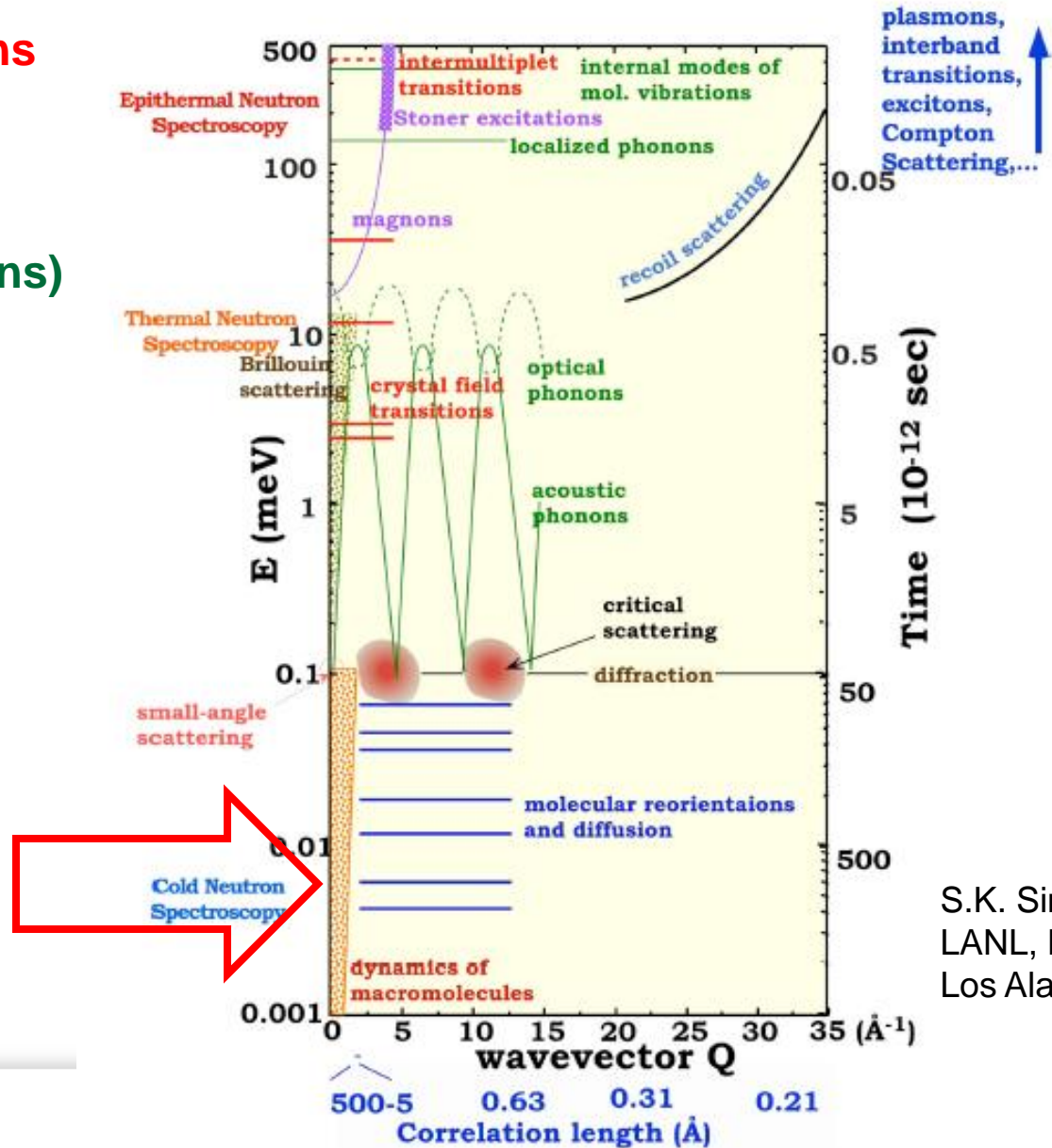
# ...because of the stringent energy resolution requirements

1 meV ~ 8 cm<sup>-1</sup> ~ 1 ps  
 1 μeV ~ 0.008 cm<sup>-1</sup> ~ 1 ns

sub-ps (vibrations)

$$\tau = \tau_0 \exp(E_a/T)$$

ns (diffusion jumps)



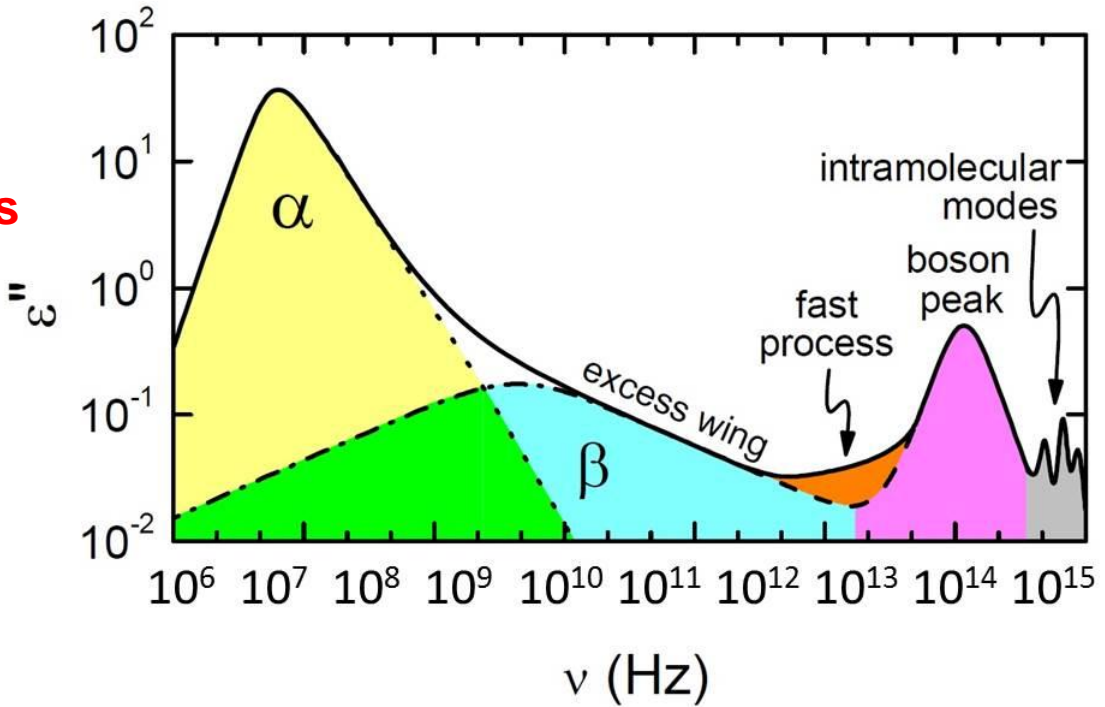
**YOU ARE HERE**

S.K. Sinha, 1985, LANL, LA-10227-C, Los Alamos, p.346

# Hard vs. soft matter dynamics (a slide for spectroscopists)

Think of inelastic neutron scattering as a typical spectroscopic technique, but with a sensitivity to H and spatial information accessible through Q-resolution capabilities

1 meV ~ 8 cm<sup>-1</sup> ~ 1 ps  
 1 μeV ~ 0.008 cm<sup>-1</sup> ~ 1 ns



←————→
←——→
↔

**Relaxations: usually specific to soft matter (but could be, e.g., due to diffusion in solid)**

**Temperature dependence: strong**

**QENS needs both a high energy resolution and a wide dynamic range**

**Vibrations are always present**

**Mostly thermal population changes**

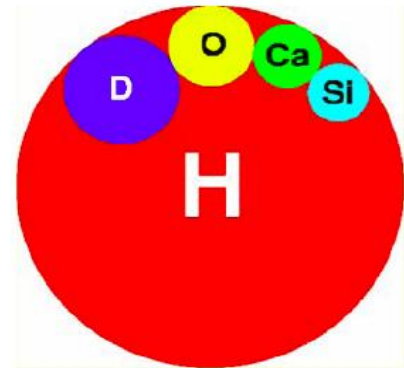
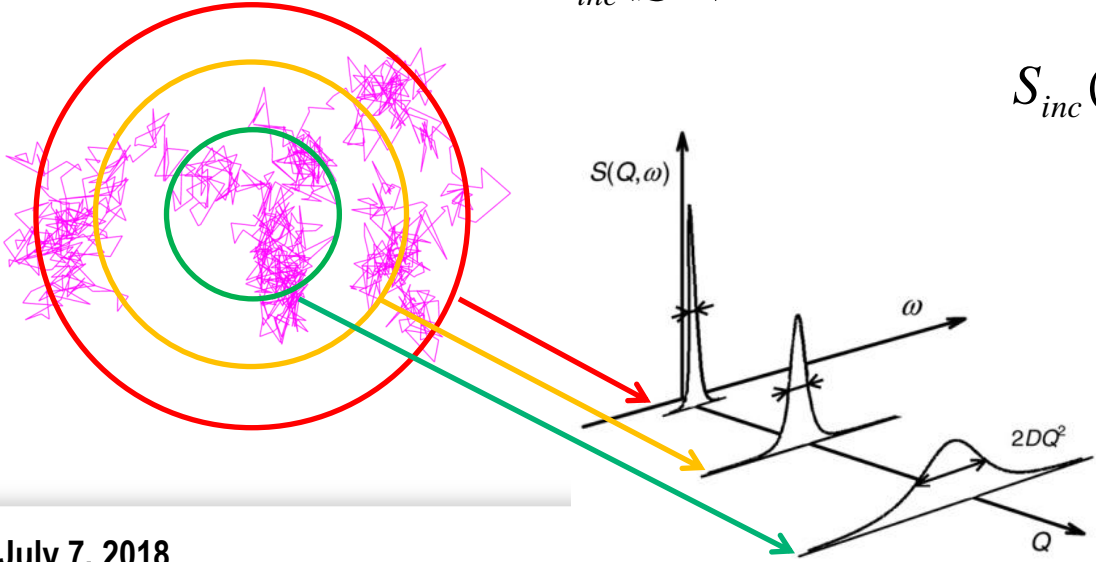
# Quasielastic scattering: simplest example to explain the signal Q-dependence - diffusion

$$S_{inc}(Q, E) = \int I_{inc}(Q, t) e^{i\frac{E}{\hbar}t} dt = \iint (G_{self}(r, t) e^{-iQr} dr) e^{i\frac{E}{\hbar}t} dt$$

Simplest case: Fickian diffusion with a diffusion coefficient  $D$

$$G_{self}(r, t) = \frac{e^{-\left(\frac{r^2}{4Dt}\right)}}{(4\pi Dt)^{3/2}}$$

$$I_{inc}(Q, t) = e^{-tDQ^2}$$



Total neutron scattering cross-section  
 Hydrogen dwarfs all the other elements due to its huge **incoherent** scattering cross-section:  
 $\sigma_{coh} = 1.76$  barn,  $\sigma_{inc} = 80.26$  barn

$$S_{inc}(Q, E) = \frac{1}{\pi} \frac{\eta D Q^2}{(\eta D Q^2) + E^2}$$

In an experiment, we'll see a Lorentzian QENS signal with Q-dependent HWHM

# More realistic “jump” diffusion description (usually for “associated” fluids)

Atom/molecule occupies a position for a period of time  $\tau$ , then quickly jumps to a new position

The HWHM,  $\Gamma(Q)$ , is no longer  $\eta D Q^2$

$$\Gamma(Q) = \frac{\eta}{\tau_T} \left( 1 - \frac{\sin(Qr)}{Qr} \right)$$

Well defined jump length  $r$  (where  $D = \langle r^2 \rangle / 6\tau$ ) (powder-averaged)

Often describes hydrogen behavior in solids very well

$$\Gamma(Q) = \frac{\eta \int_0^\infty \left( 1 - \frac{\sin Qr}{Qr} \right) P(r) dr}{\int_0^\infty P(r) dr}$$

If there is a distribution of jump length...

Often describes liquids such as water

$$\Gamma(Q \rightarrow 0) = \eta D Q^2$$

$$\Gamma(Q \rightarrow \infty) = \eta / \tau_T$$

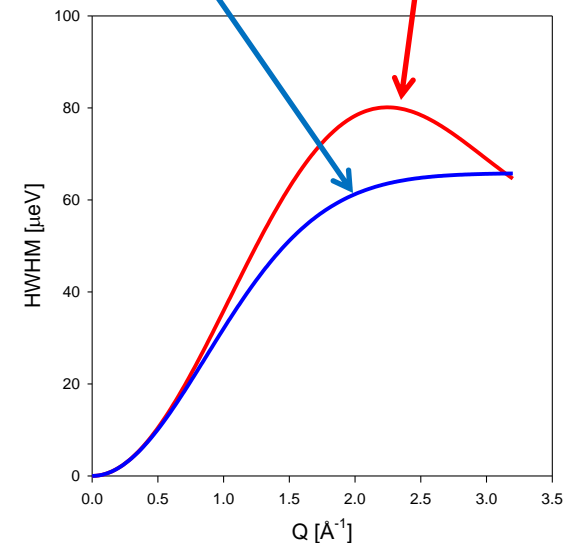
$$\Gamma(Q) = \frac{\eta}{\tau_T} \left[ 1 - \frac{1}{1 + D Q^2 \tau_T} \right]$$

$$\Gamma(Q) = \frac{\eta}{\tau_T} \left[ 1 - \exp(-D Q^2 \tau_T) \right]$$

For exponential distribution

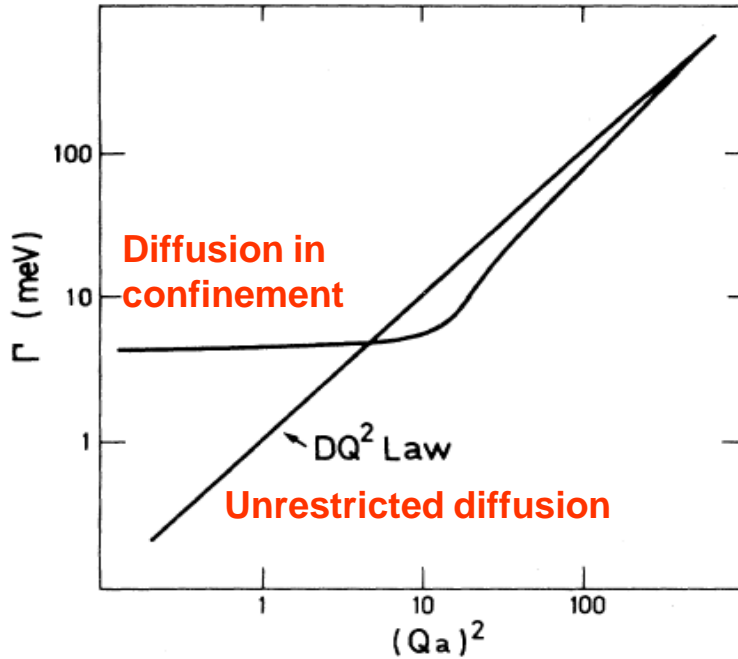
For Gaussian distribution

From the data fits, we get  $D, \tau, \langle r^2 \rangle$

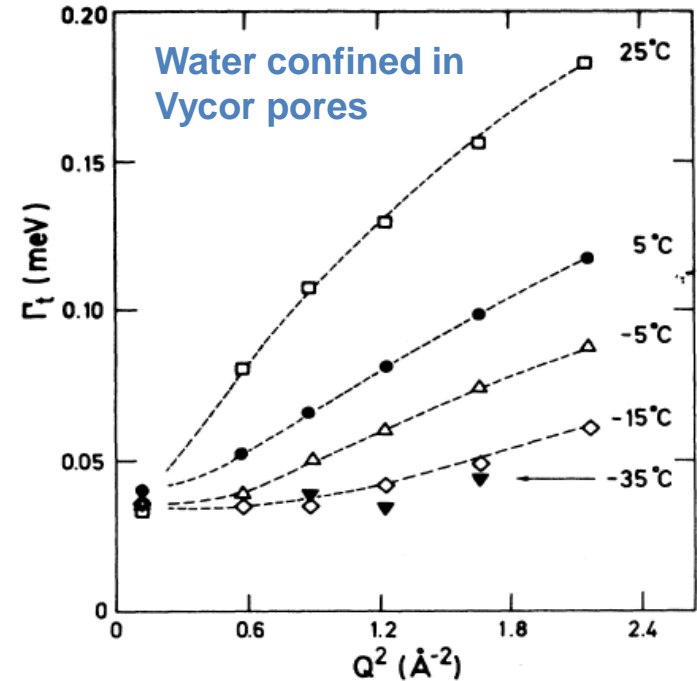


# What if the diffusion process is localized in space: The effect on the QENS signal broadening

- Examples: liquids in nano-cavities, hydrogen hopping back and forth between the interstitial sites



Volino and Dianoux, Mol. Phys. 41, 271 (1980)



Bellissent-Funel et al., Phys. Rev. E **51**, 4558 (1995)

Common feature: diffusing molecules cannot penetrate the borders of the pore. This effect is evident at low  $Q$  that corresponds to large distances: no more  $DQ^2$  law!

For example, for diffusion in a sphere of radius  $a$ ,  $\text{HWHM} = 4.33D/a^2$  for  $0 < Qa < 3.3$



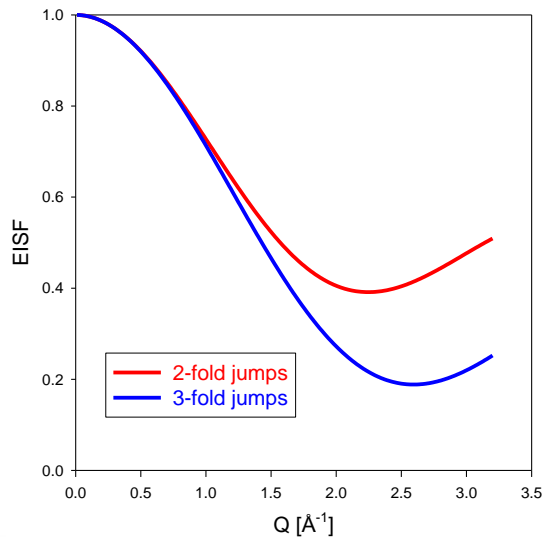
# What if the diffusion process is localized in space: Some of the scattering signal becomes elastic

- Examples: liquids in nano-cavities, hydrogen hopping back and forth between the interstitial sites

Then there is an elastic scattering due to “spatial restriction”

Practical definition of **EISF**: Elastic Incoherent Structure Factor = Elastic/(Elastic+Quasielastic)

Physical meaning: **EISF**(Q) measured in an experiment with an energy resolution  $\Delta E$  is a probability that, after a time  $\sim(\eta/\Delta E)$ , the moving particles still resides inside a box of  $\sim 1/Q$  size

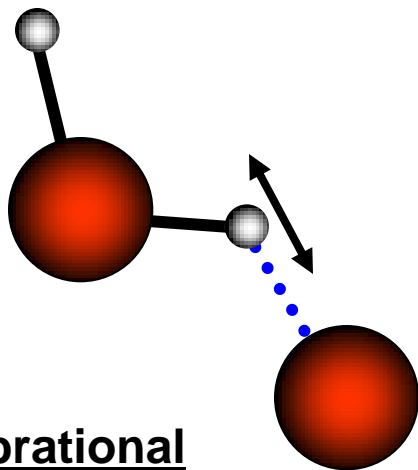


Measuring **EISF**(Q) is a great way to deduce the geometry of the corresponding restricted motion!

But **EISF**(Q) may depend on the energy resolution of the experiment – beware!

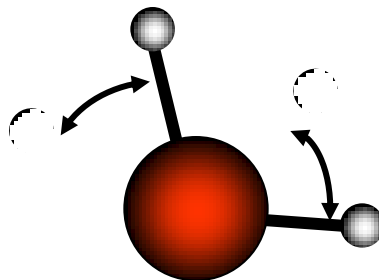
From the data fits, we get the characteristic size and (sometimes) geometry of the confinement

# A textbook example: molecular motions in water



**Vibrational**  
(harmonic oscillation)

$\langle u^2 \rangle^{1/2}$   
Debye-Waller

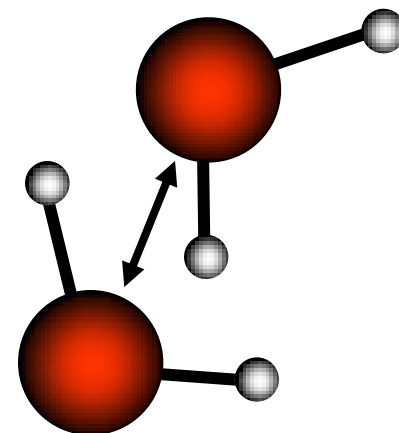


**Reorientational**  
(isotropic rotation)

Localized motion:  $EISF = j_0^2(Qa)$

$\tau_r$   
Rotational Correlation Time

$r_g$   
Radius of Gyration



**Jump Translational**

Non-localized motion: no EISF

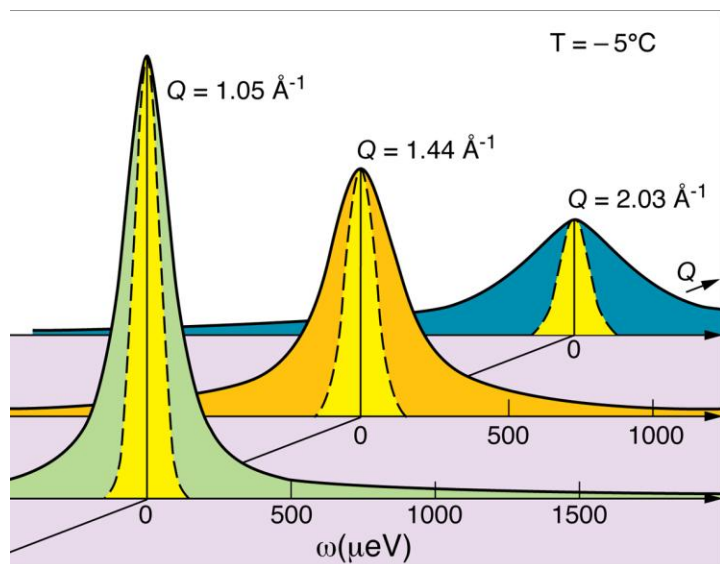
$D_t$   
Translational Diffusion Constant

$\tau_t$   
Residence Time

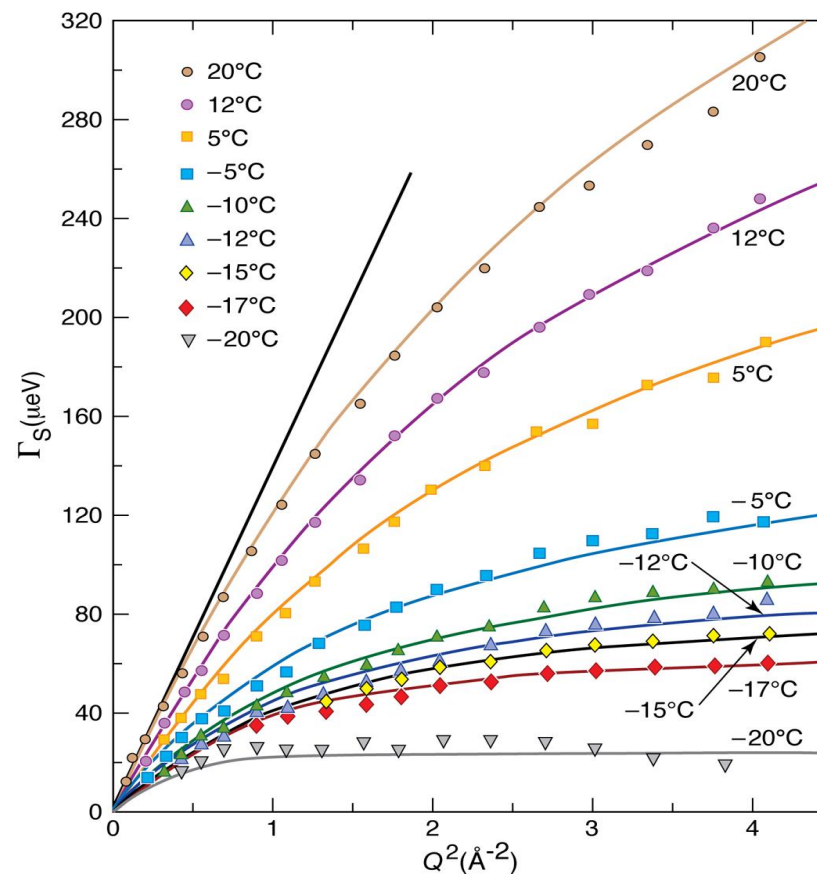
$l$   
Mean Jump Distance

$$S(Q, \omega) = e^{-\langle u^2 \rangle Q^2 / 3} T(Q, \omega) \otimes R(Q, \omega)$$

# Supercooled bulk water



Data from Teixeira et al. (1985)



Good example of translational jump diffusion

$\Gamma$  (HWHM) is Q-dependent

Low Q:  $\Gamma = \hbar D Q^2$ ; High Q,  $\Gamma = \hbar/\tau_0$

- **Translational Motion**

$$T(Q, \omega) = \frac{1}{\pi} \frac{\Gamma(Q)}{\Gamma^2(Q) + \omega^2}$$

- **Jump Diffusion**

$$\Gamma(Q) = \frac{D_t Q^2}{1 + D_t Q^2 \tau_0} \text{ and } D_t = \frac{L^2}{6\tau_0}$$

# A practical example: a room-temperature ionic liquid

*J. Phys. Chem. B* 2009, 113, 159–169

## Proton Dynamics in *N,N,N',N'*-Tetramethylguanidinium Bis(perfluoroethylsulfonyl)imide Protic Ionic Liquid Probed by Quasielastic Neutron Scattering

Eugene Mamontov,<sup>\*,†</sup> Huimin Luo,<sup>‡</sup> and Sheng Dai<sup>§</sup>

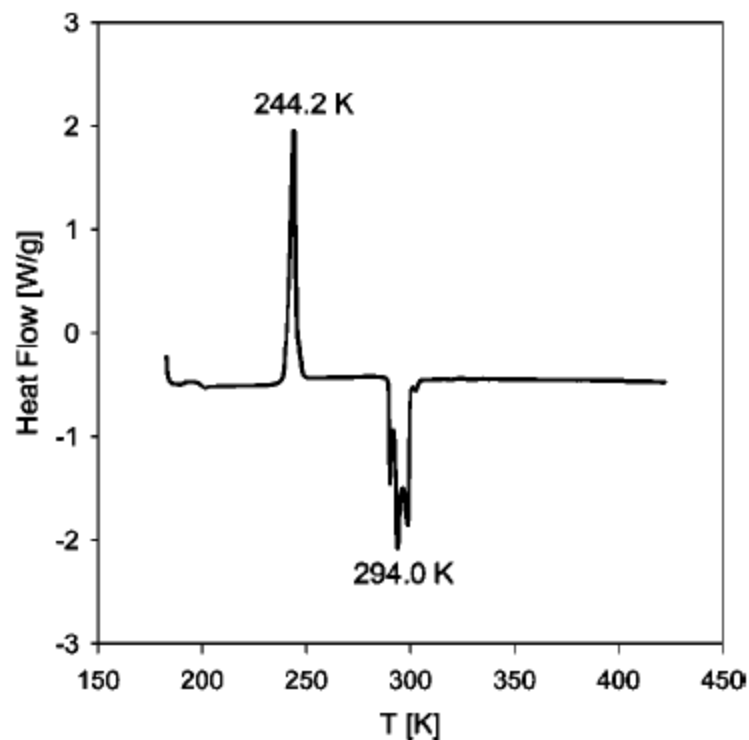
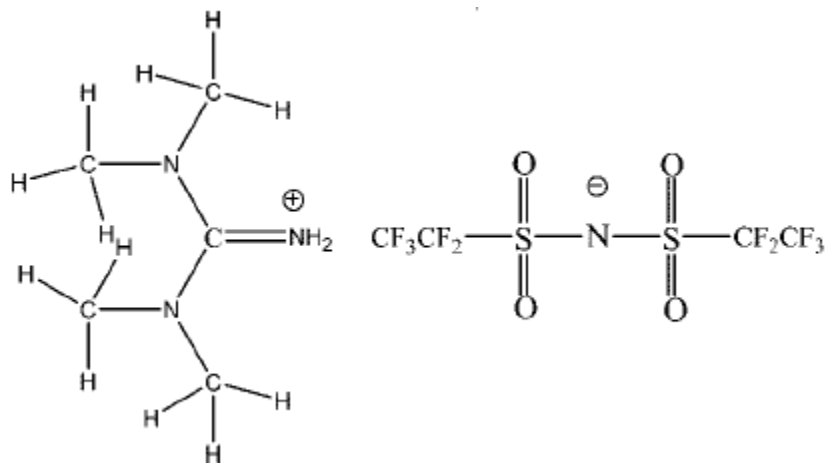
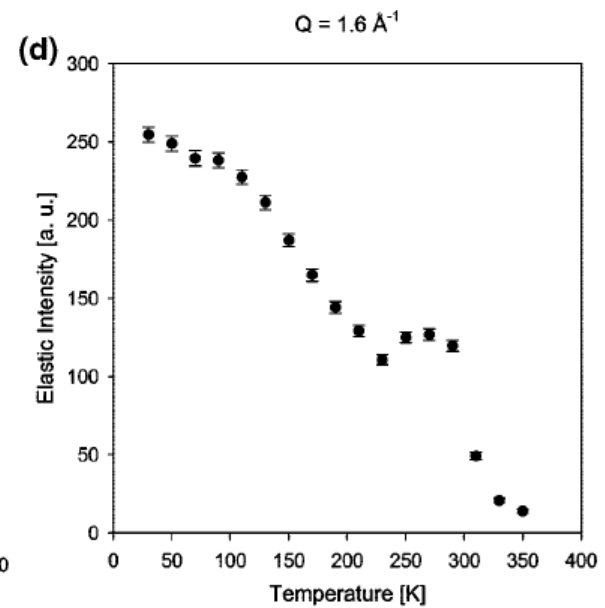
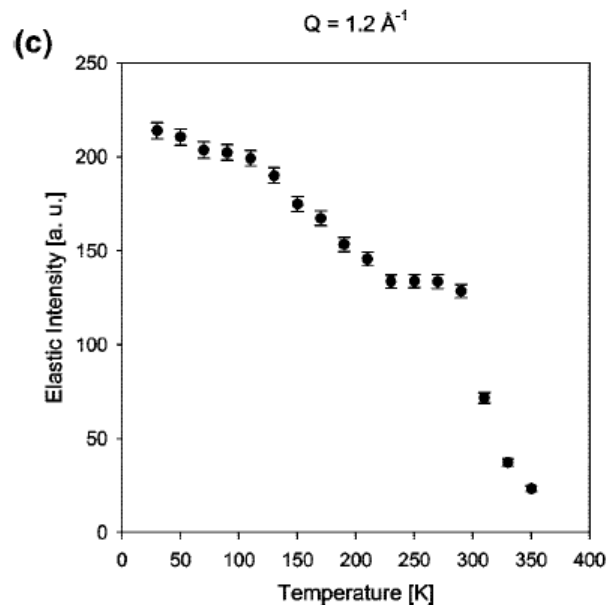
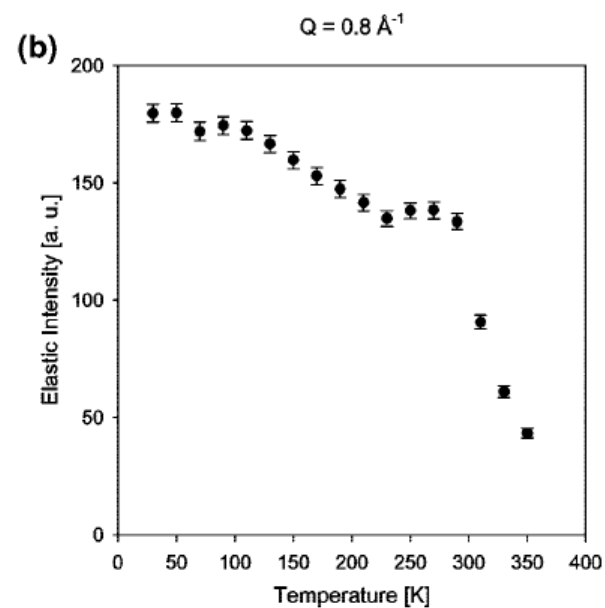
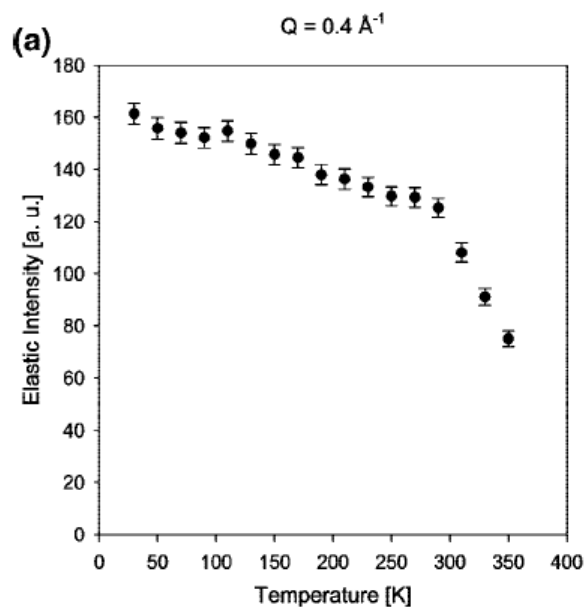
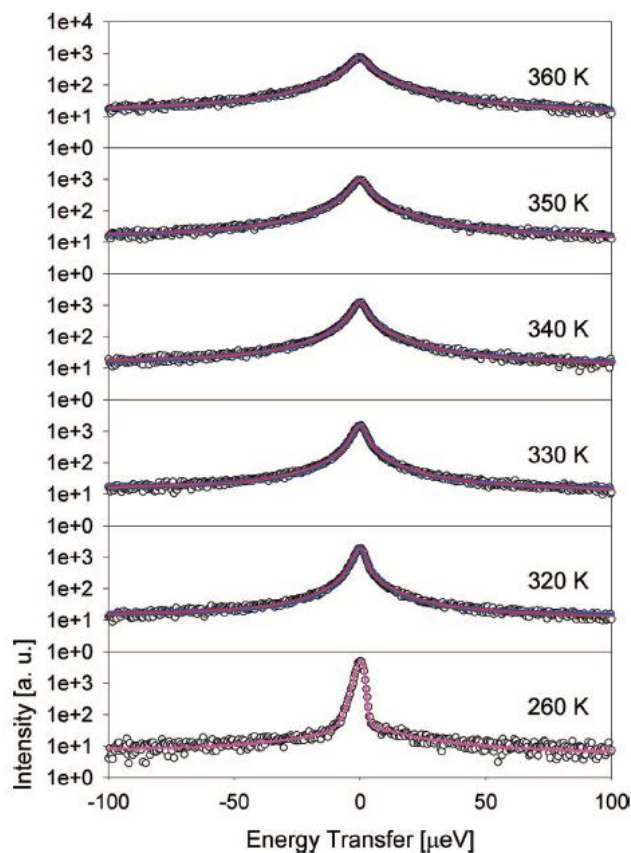
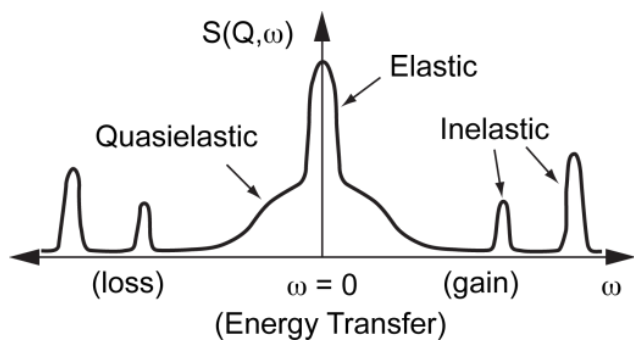


Figure 2. Differential scanning calorimetry measurement of [H<sub>2</sub>NC(dma)<sub>2</sub>][BETI] taken on warming up at 2 K/min.

# A diagnostic tool: elastic intensity scan



# Methyl group rotation in the solid phase, or something else?

$$\text{EISF}_{\text{apparent}} = x_{\text{immobile}} + (1 - x_{\text{immobile}})\text{EISF}$$

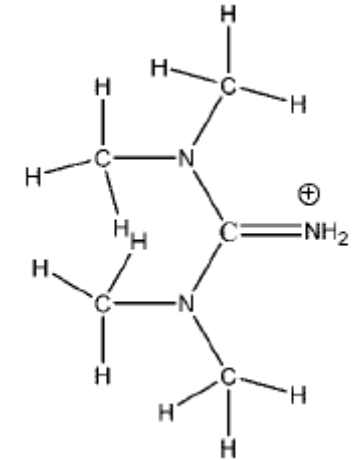
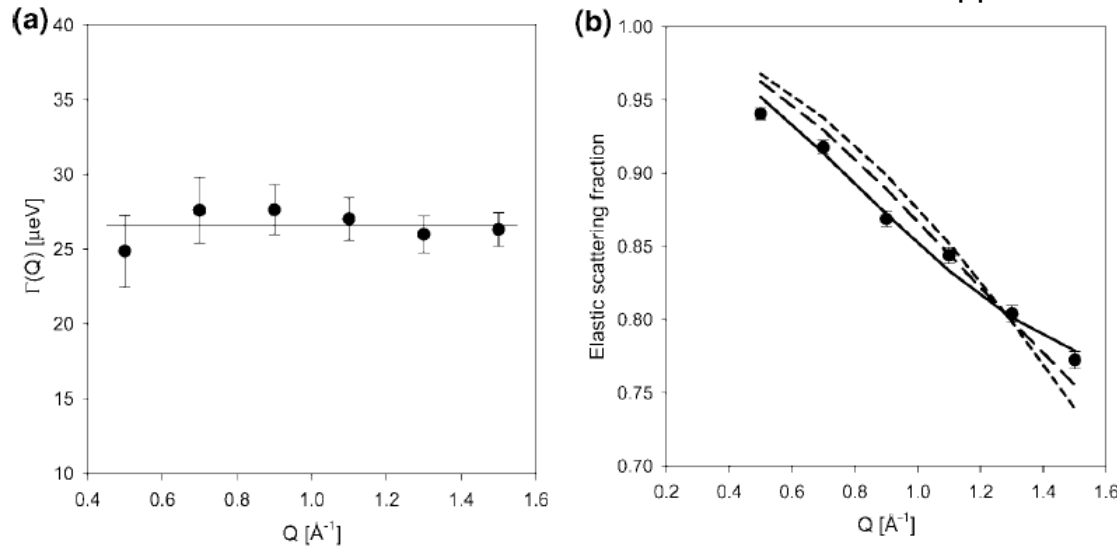


Figure 6. Parameters of the 260 K data fits obtained using eq 2 and 3. (a) Hwhm of the Lorentzian QENS broadening with a  $Q$ -independent fit. (b) Total measured elastic scattering fraction,  $(x + (1 - x)\text{EISF})$ , where  $x$  is a parameter in eq 2, and its best fits obtained using EISF described by eq 4 while  $x$  was fixed to zero (short-dashed line), EISF described by eq 4 while  $x$  was allowed to vary (solid line), and EISF described by eq 5 while  $x$  was allowed to vary (long-dashed line).

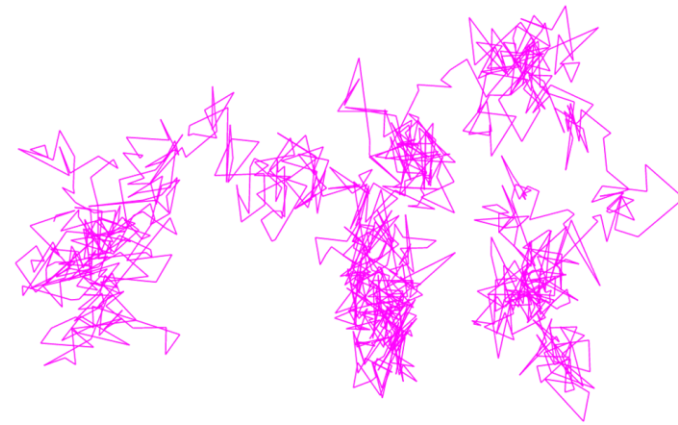
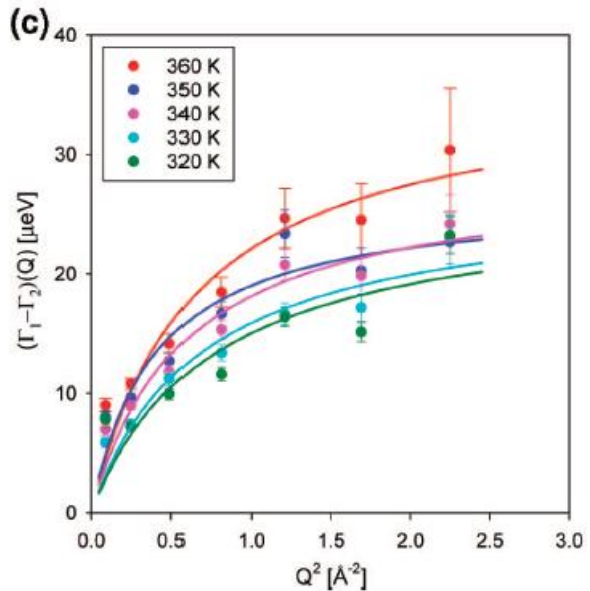
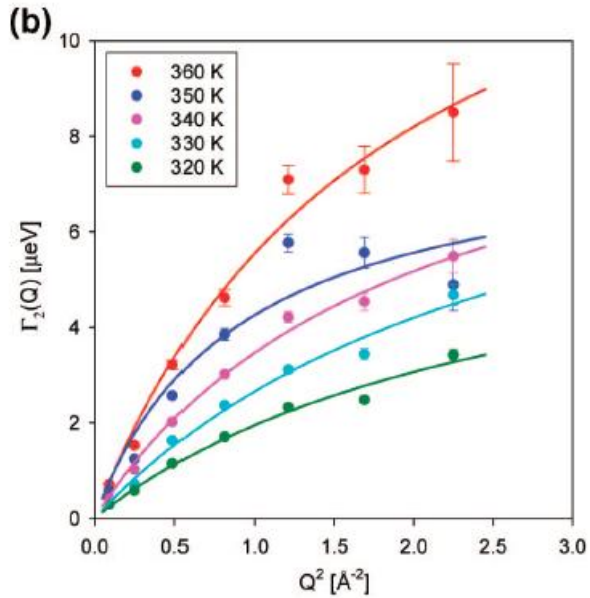
$$\text{EISF}(Q) = (1 + 2j_0(Qr\sqrt{3}))/3$$

- Methyl group rotation model with a known value  $r = 1 \text{ \AA}$  does not work well, even when allowed for adjustable immobile fraction

$$\text{EISF}(Q) = j_0^2(QR_1)$$

- A generic “diffusion on a sphere” model works well when allowed for adjustable immobile fraction, yielding  $r = 1.6 \text{ \AA}$

# Liquid phase: two-component fits and what they mean



At short times, a particle moves inside a transient cage made of the nearest neighbours...

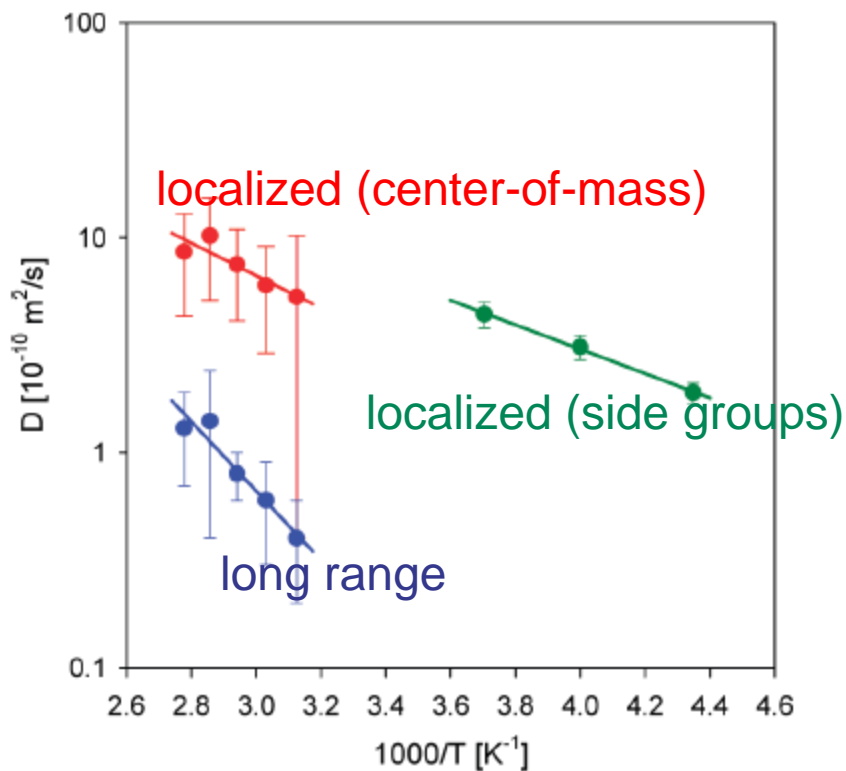
...then eventually breaks the cage to perform a translational diffusion jump

$$S(E) = T_1(E) \otimes T_2(E)$$

$$S(E) = (1 - p) \frac{1}{\pi} \frac{((\hbar/\tau_1) + (\hbar/\tau_2))}{E^2 + ((\hbar/\tau_1) + (\hbar/\tau_2))^2} +$$

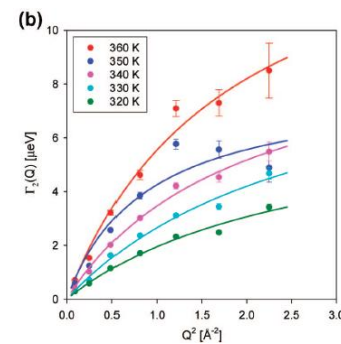
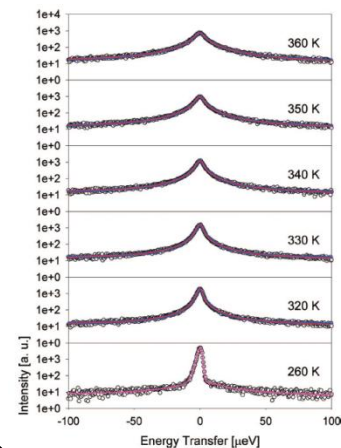
This parameter,  $p$ , is actually EISF(Q) for those "caged" motions, yielding the cage size  $\rightarrow p \frac{1}{\pi} \frac{(\hbar/\tau_2)}{E^2 + (\hbar/\tau_2)^2}$

# Then we can summarize all the processes we have seen



**Figure 10.** Temperature dependence of the diffusion coefficients describing a long-range translational diffusion process in the liquid phase (blue), a localized translational diffusion process in the liquid phase (red), and a localized process which is present in solid and liquid phases (green).

- At each temperature, collect the  $I(E)$  spectra at several  $Q$  values (simultaneously) and fit each spectrum with an appropriate model scattering function (a very important decision to make at this point)
- The so obtained  $\text{HWHM}(Q)$ ,  $\text{EISF}(Q)$ , etc., are in turn fit with an appropriate model to obtain, e.g., the jump time (or similar parameters) at each temperature
- Make an Arrhenius plot of this parameter; analyze the temperature dependence





# Quasielastic neutron scattering: Conclusion

- **QENS can elucidate microscopic diffusion dynamics through analysis of Q-dependence of signal broadening and the fraction of elastic vs. quasielastic scattering signal; this information is unobtainable by any technique other than MD**
- **If your system exhibits diffusion/relaxation dynamics on pico- to nano-second time scale, QENS can likely help in you research efforts**
- **The power of QENS to elucidate microscopic diffusion dynamics is demonstrated best by a new generation spectrometer such as BASIS at SNS, ORNL because of its ability to probe several processes at once; see Part II for explanation of what it takes**

## Acknowledgement

Scientific User Facilities Division, Office of Basic Energy Sciences, US Department of Energy

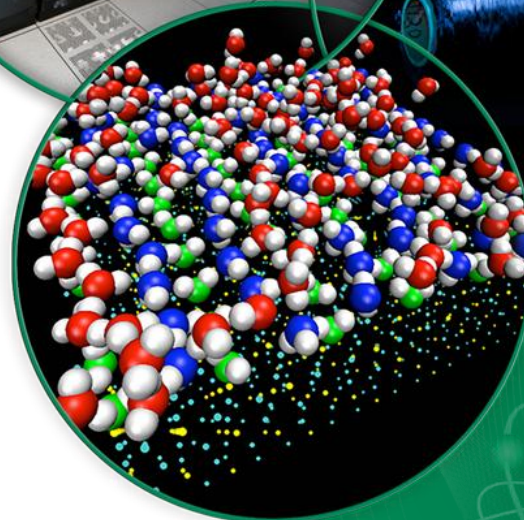
# Quasielastic neutron scattering, neutron backscattering technique, BASIS and beyond

## Part II: neutron backscattering technique, BASIS and beyond

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Oak Ridge National Laboratory

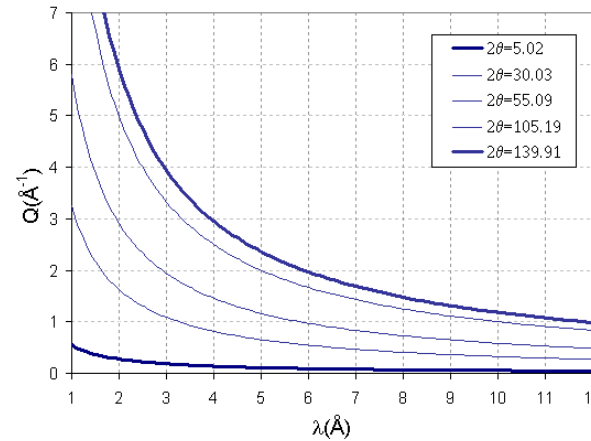
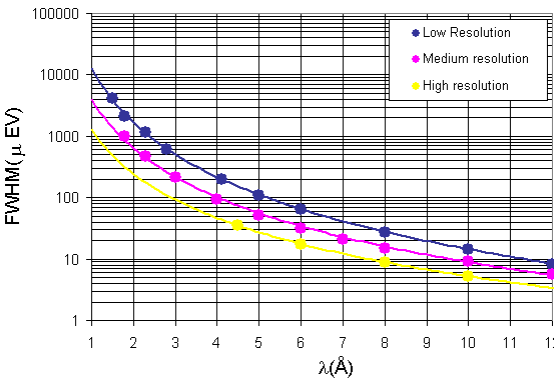
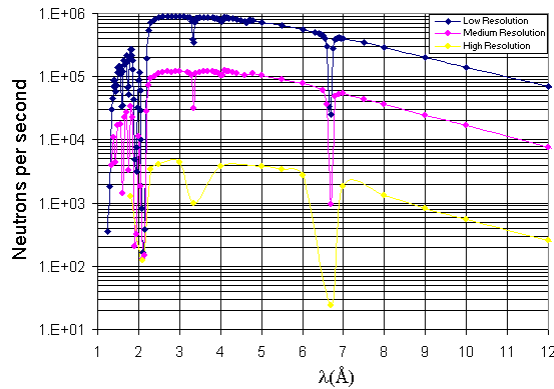
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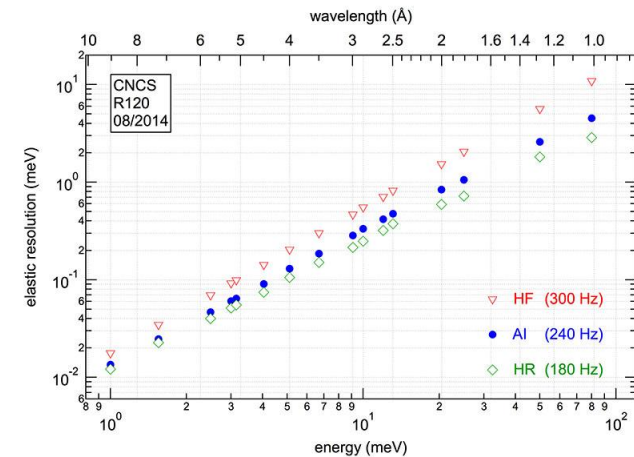
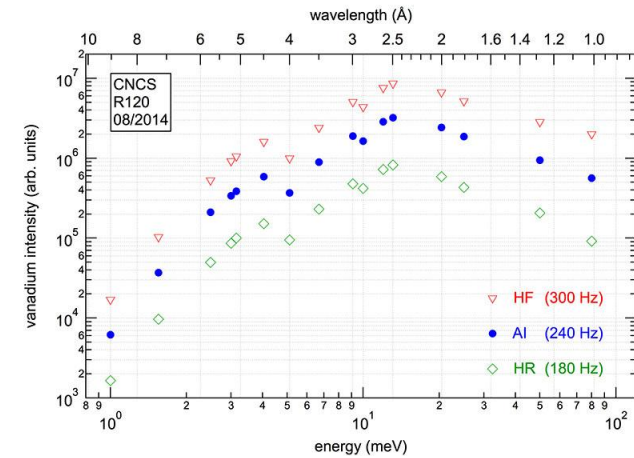
# Quasielastic neutron scattering measurements do not absolutely require a backscattering spectrometer, but...

Some prominent quasielastic studies were even performed in the past on triple-axis spectrometers!

Direct-geometry TOF spectrometers are widely used for medium-resolution QENS measurements today, but they come with serious limitations



**Very long incident wavelengths required for high resolution QENS come with intensity and Q-range problems**



Disk Chopper Spectrometer, NCNR

Cold Neutron Chopper Spectrometer, SNS

# Neutron backscattering: the limiting case of the [inverse geometry] crystal analyzer spectrometer for the best possible energy resolution

Whether a crystal analyzer spectrometer is TOF-based or on a steady source, the energy resolution of the analyzer crystals:

$$\delta E_f = 2E_f \left( \frac{\delta d}{d} + \cot \theta \delta \theta \right)$$

If a crystal analyzer spectrometer is TOF-based, then  $E = E_i - E_f$ , where  $E_f$  is fixed by analyzer Bragg reflection,  $E_i$  is determined from the TOF

The overall energy resolution then becomes:

$$\delta E = 2E \sqrt{\left( \frac{\delta d}{d} + \cot \theta \delta \theta \right)^2 + \left( \frac{\delta TOF}{TOF} \right)^2}$$

Long-wavelength  
neutrons

Small lattice  
constant spread

Backscattering  
conditions

Sharp neutron  
pulse, or long  
flight path

# Building a TOF backscattering spectrometer: what's not negotiable?

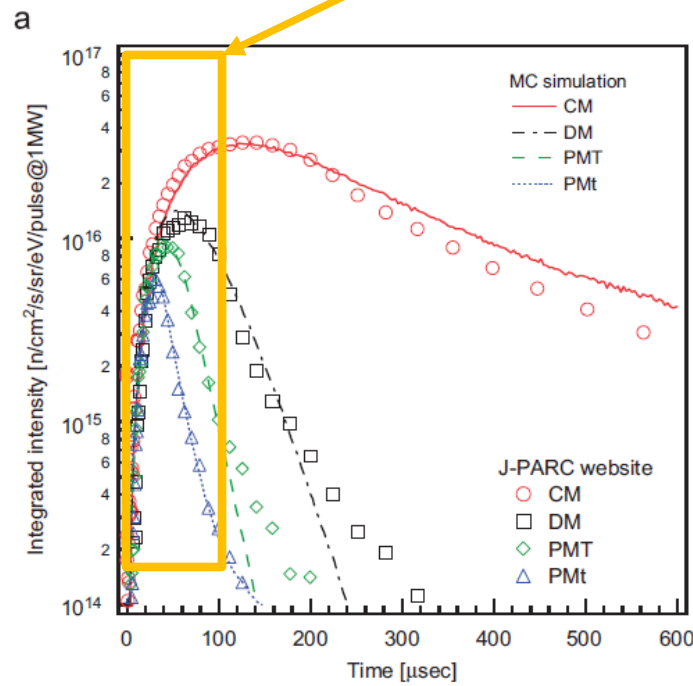
$$\delta E = 2E \sqrt{\left( \frac{\delta d}{d} + \cot \theta \delta \theta \right)^2 + \left( \frac{\delta TOF}{TOF} \right)^2}$$

Analyzer crystals with small ( $\delta d/d$ ) in the backscattering position

Crystal plane	$\frac{\Delta \tau}{\tau}$	$\Delta E_{ext}$ ( $\mu eV$ )	$\lambda$ ( $\text{\AA}$ ) for $\Theta = 90^\circ$
Si (111)	$1.86 \cdot 10^{-5}$	0.077	6.2708
Si (311)	$0.51 \cdot 10^{-5}$	0.077	3.2748
Ca F <sub>2</sub> (111)	$1.52 \cdot 10^{-5}$	0.063	6.307
Ca F <sub>2</sub> (422)	$0.54 \cdot 10^{-5}$	0.177	2.23
Ga As (400)	$0.75 \cdot 10^{-5}$	0.153	2.8269
Ga As (200)	$0.157 \cdot 10^{-5}$	0.008	5.6537
Graphite (002)	$12 \cdot 10 \cdot 10^{-5}$	0.44	6.70

[https://www.ill.eu/other\\_sites/BS-review/index.htm](https://www.ill.eu/other_sites/BS-review/index.htm)

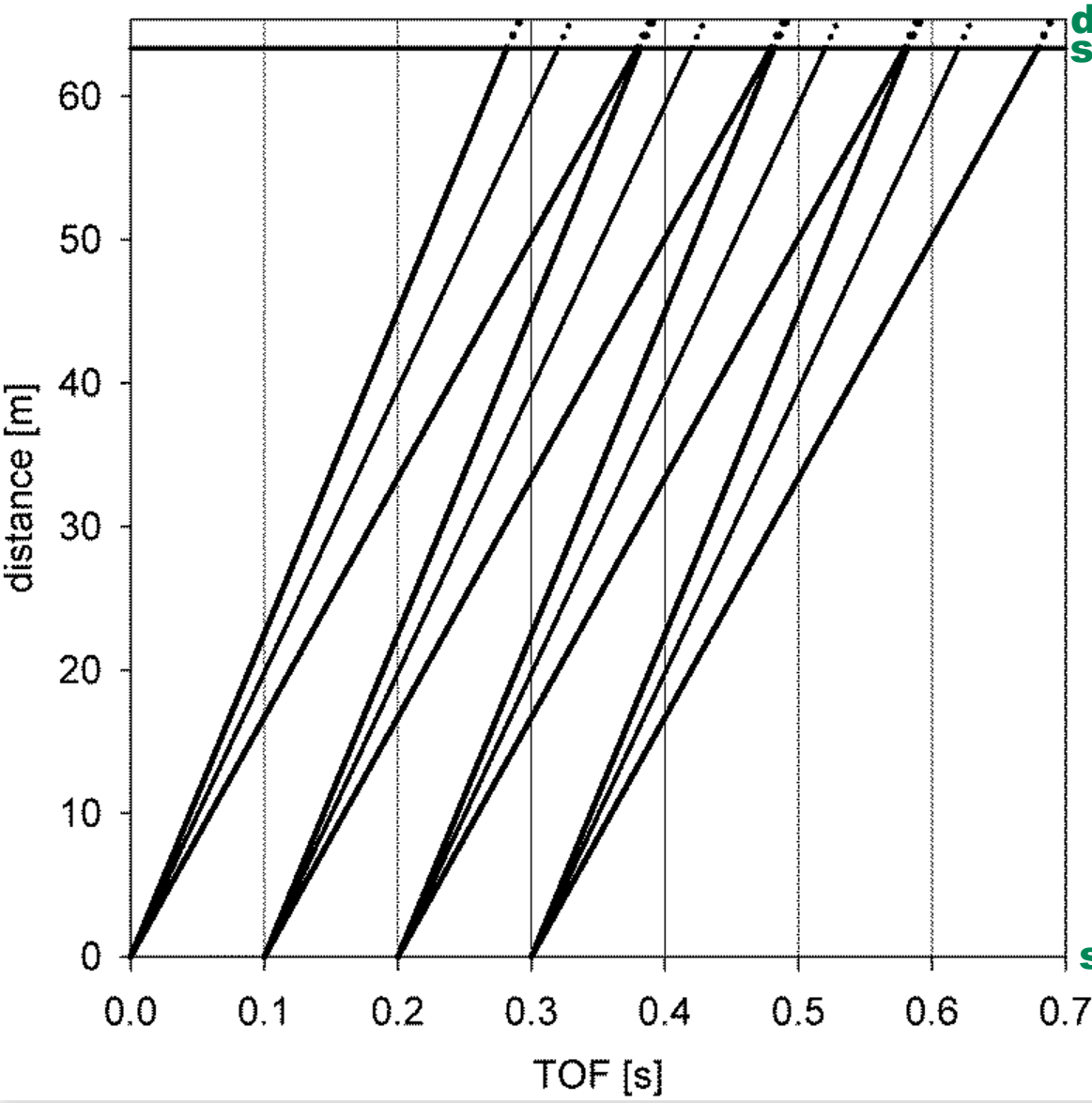
Relatively long flight path with a sharp pulse, either from a decoupled moderator, or a pulse-shaping chopper



**The art of the possible:** Because improving energy resolution kills counting statistics, why kill statistics for only a marginal resolution improvement? Hence one usually wants to **match the resolution terms**

Attainable energy resolution: Perfect crystals < Elastically bent perfect crystals < Mosaic crystals

# Once the resolution has been worked out, what's negotiable?



Accessible range of energy transfers vs. flight path (needed for the desired resolution!) vs. source repetition rate

# BASIS at SNS, ORNL, 11th year in the user program

REVIEW OF SCIENTIFIC INSTRUMENTS **82**, 085109 (2011)

## A time-of-flight backscattering spectrometer at the Spallation Neutron Source, BASIS

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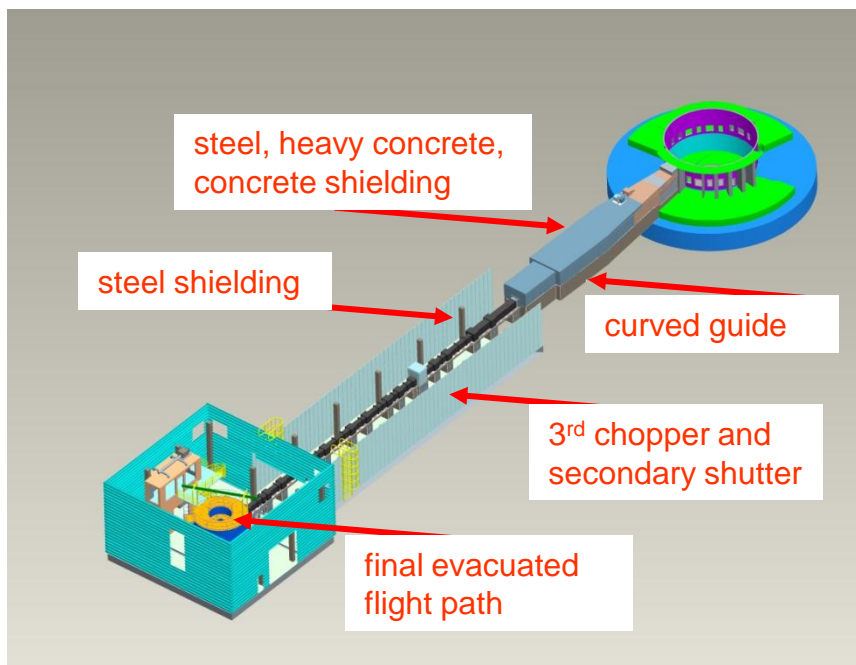
(Received 1 June 2011; accepted 28 July 2011; published online 25 August 2011)

<b>2008 7 Publications</b>	<b>2009 10 Publications</b>	<b>2010 16 Publications</b>
<b>2011 13 Publications</b>	<b>2012 30 Publications</b>	<b>2013 24 Publications</b>
<b>2014 23 Publications</b>	<b>2015 30 Publications</b>	<b>2016 37 Publications</b>
<b>2017 34 Publications</b>		

**We must have done it about right!**

# TOF backscattering implementation, BASIS at SNS

- **BA**ckscattering **SI**licon **S**pectrometer is a high-energy resolution, wide-dynamic range inverted geometry neutron spectrometer built on BL2 and facing a decoupled supercritical hydrogen, centerline-poisoned moderator

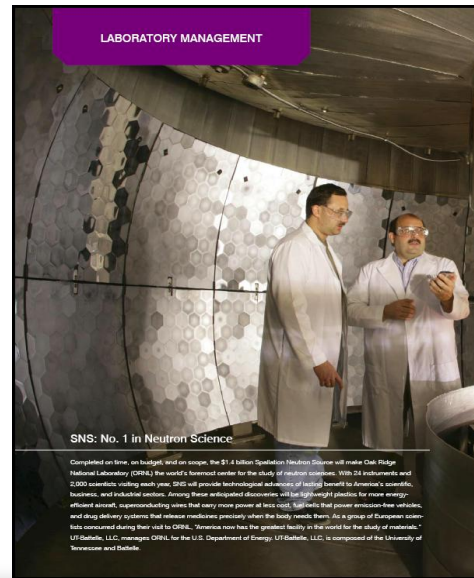
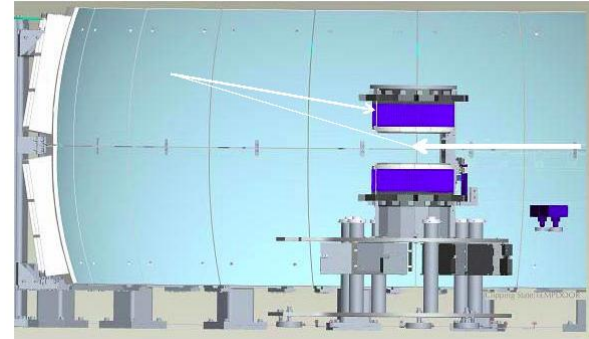


- Incident Flight Path - 84 m moderator-sample position
  - Curved Guide: 10 cm wide x 12 cm tall, 1000 m radius of curvature, line-of-sight at 31 m
  - Straight Guide: 10 cm wide x 12 cm tall
  - Converging Funnel: last 7.7 m; exit 3.25 cm x 3.25 cm, stops 27.5 cm from sample
- Chopper System
  - 3 bandwidth/frame overlap choppers at 7, 9.25 and 50 m
  - Operation at 60 (standard), 30, 20, 15, 12, or 10 Hz
  - Bandwidth (full choppers transmission) of about 0.5 Å at 60 Hz

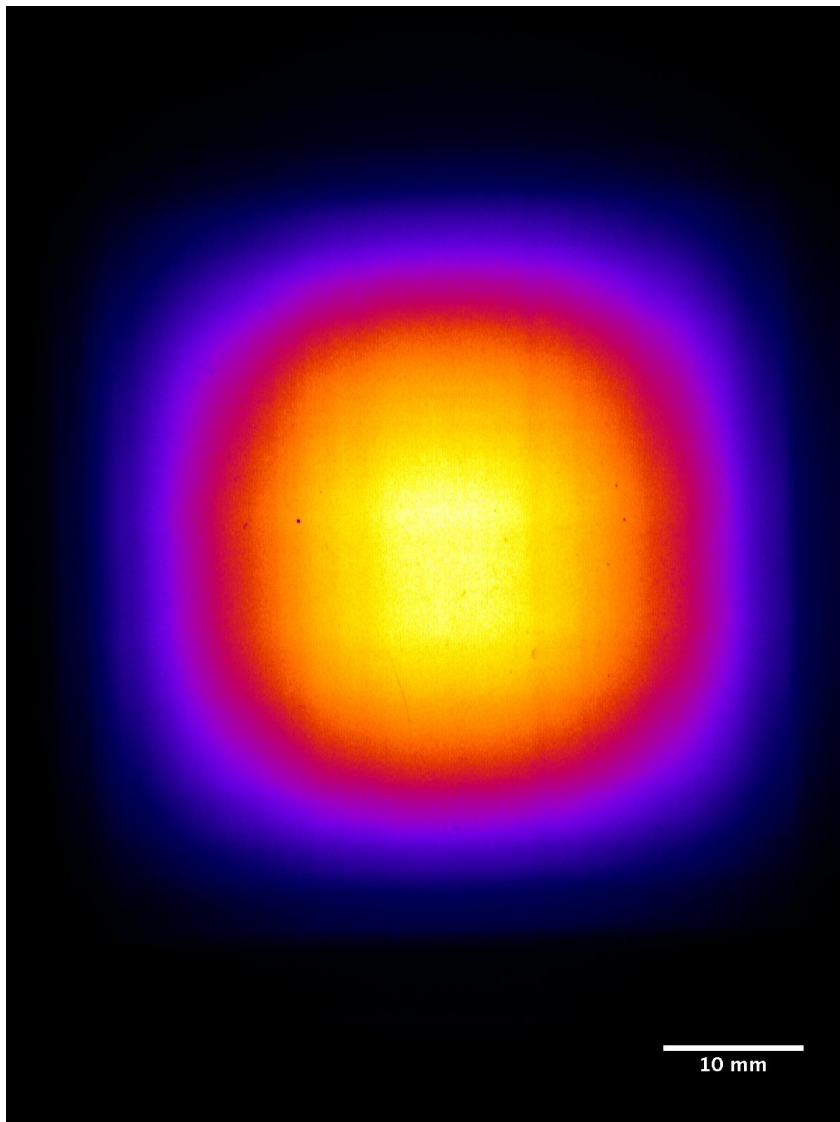


# Evacuated Final Flight Path (aka tank)

- Sample – nominal dimensions 3 x 3 cm<sup>2</sup>
- Analyzer Crystals - Si (111):  $\lambda_f = 6.267 \text{ \AA}$ ,  $\delta d/d \sim 3.5 \times 10^{-4}$ , 2.0 ster coverage (16 % of  $4\pi$ ).
- Radial Collimator – restricts analyzer view of the sample
- Final Evacuated Flight Path - 2.5 m sample - analyzer,  $\sim 2.23 \text{ m}$  analyzer – detector
- Detector Choice – LPSD <sup>3</sup>He tubes

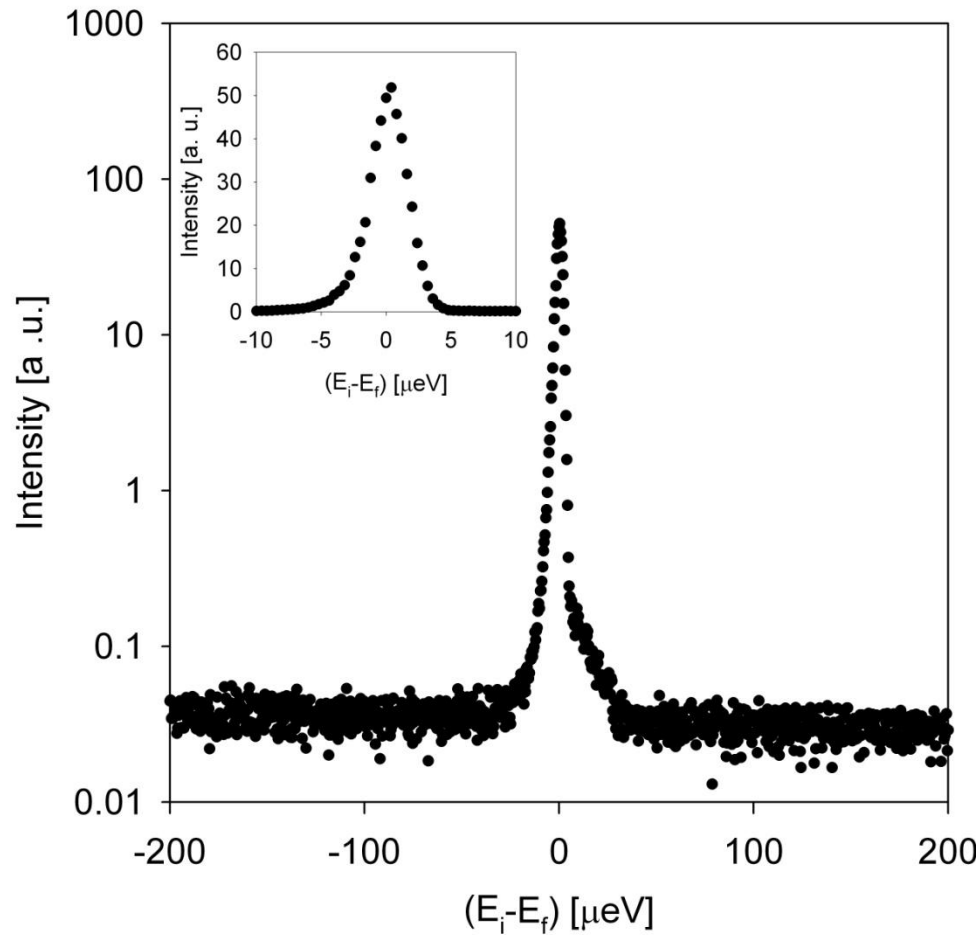


# Beam at the sample position (6.3 Å)



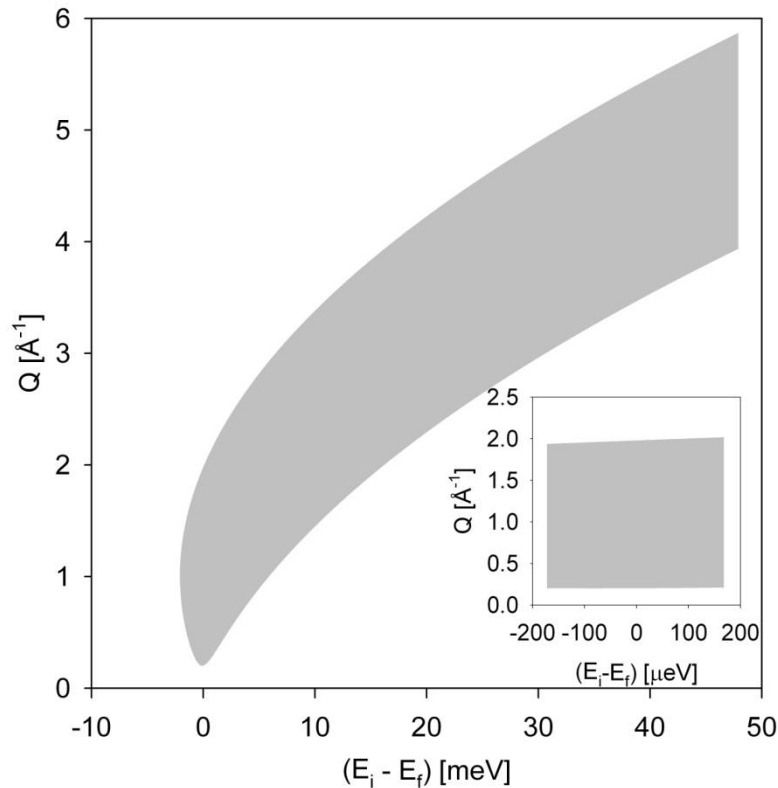
- Sample holders ID: 29.0 mm; cylindrical inserts can provide a gap as narrow as 0.05 mm

# Annular vanadium, 94 % transmission

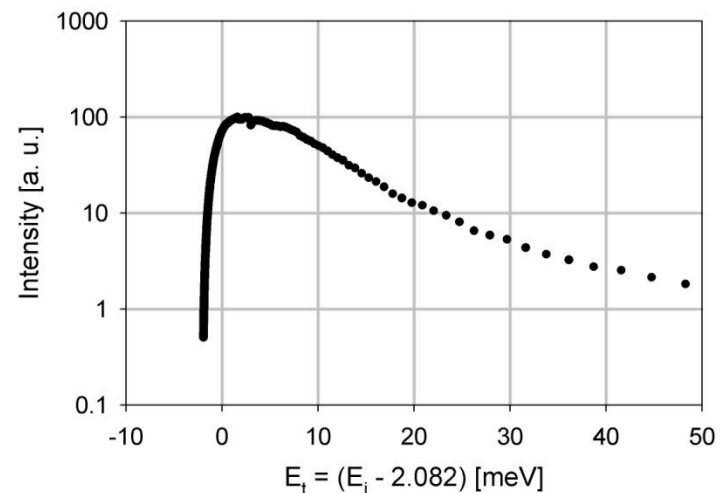
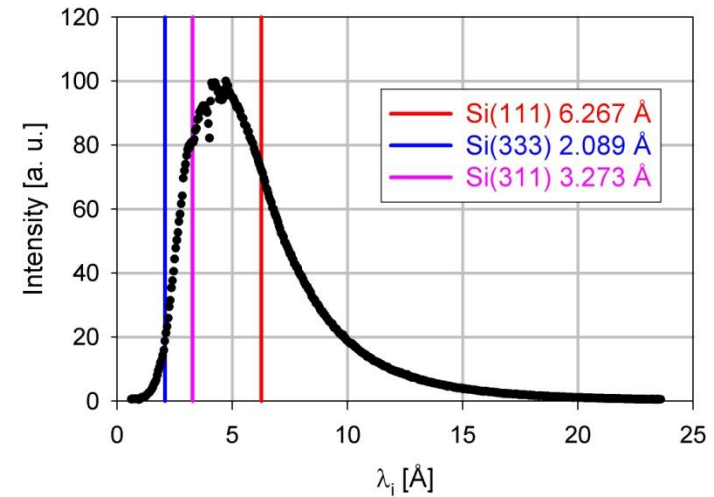


- Energy resolution (Q-averaged): 3.5  $\mu\text{eV}$  (FWHM)
- Signal-to-background ratio (at the elastic line): better than 1000:1
- Dynamic range: variable (affects counting statistics, but not the energy resolution)

# Incident spectrum and $(Q, \omega)$ coverage

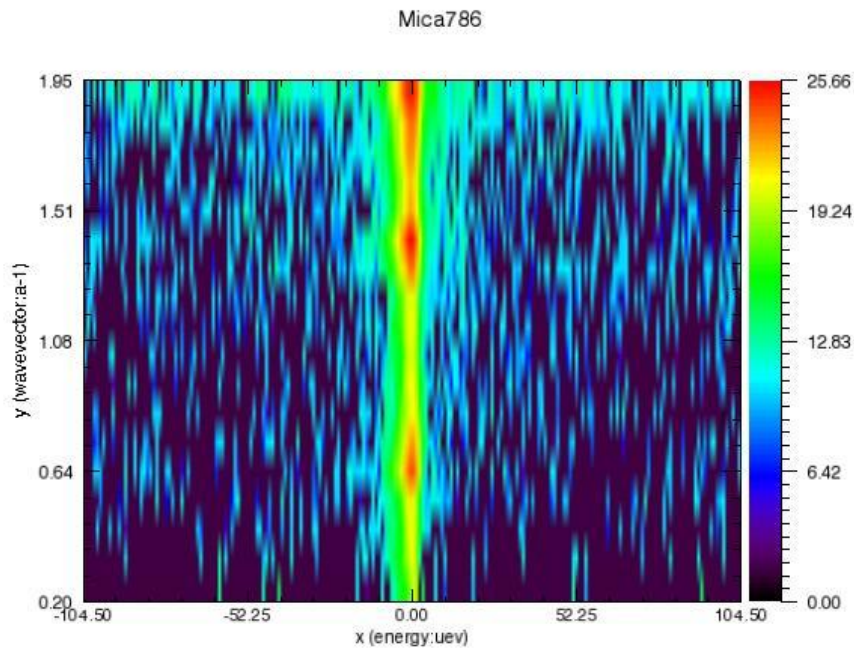
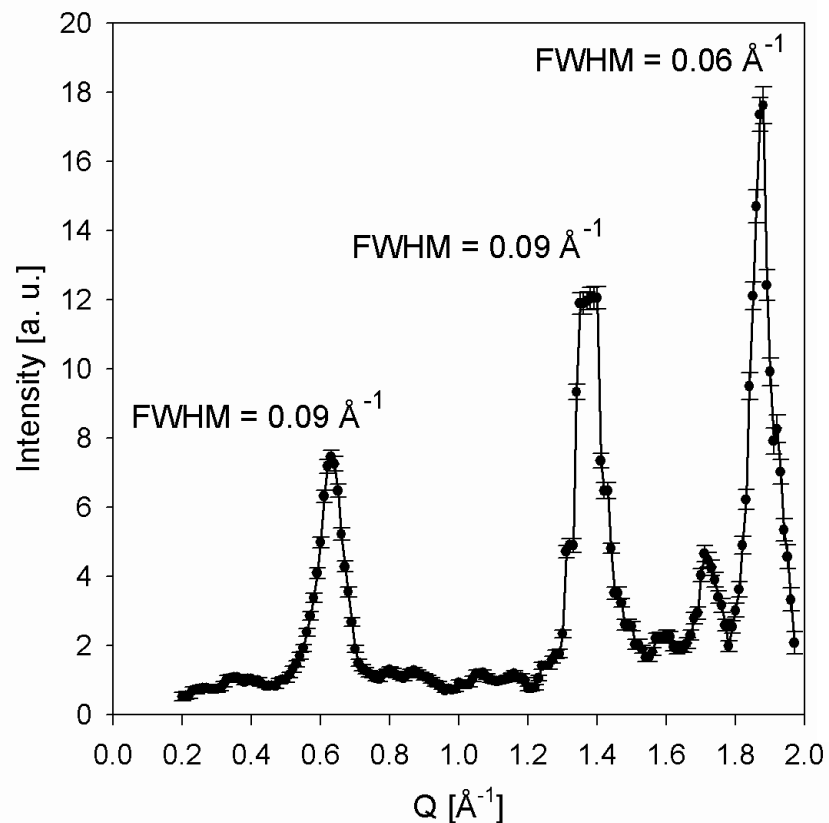


- Incident band (full chopper opening):  $(60/\nu) \cdot [0.5 \text{ \AA}]$ , where  $\nu = 60, 30, 20, 15, 12, 10 \text{ Hz}$
- Inelastic resolution:  $\delta E \approx 0.001 \cdot E_i$  at high energy transfers



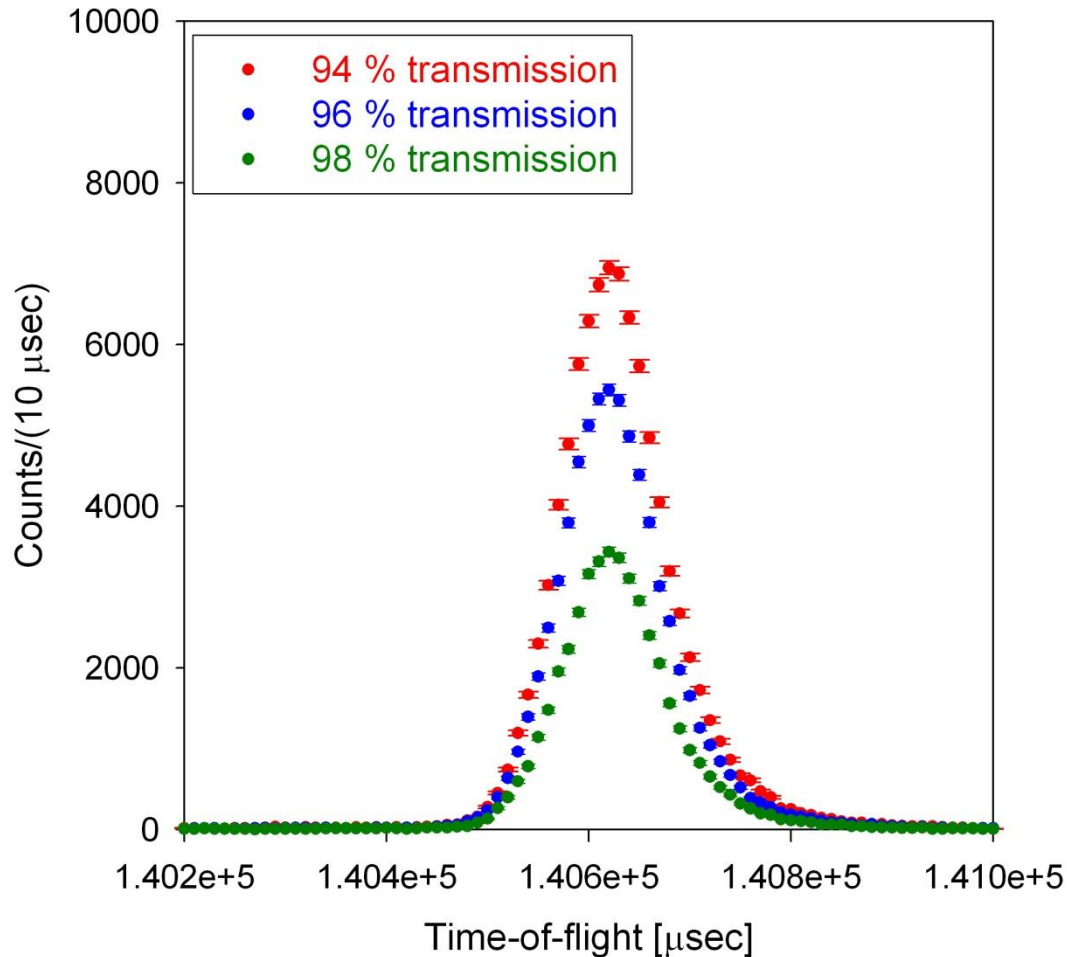
- 1 Hz signal (no frame overlap),  $1/\nu$  efficiency corrections applied

# Q-resolution at the elastic line



# Data collection rates

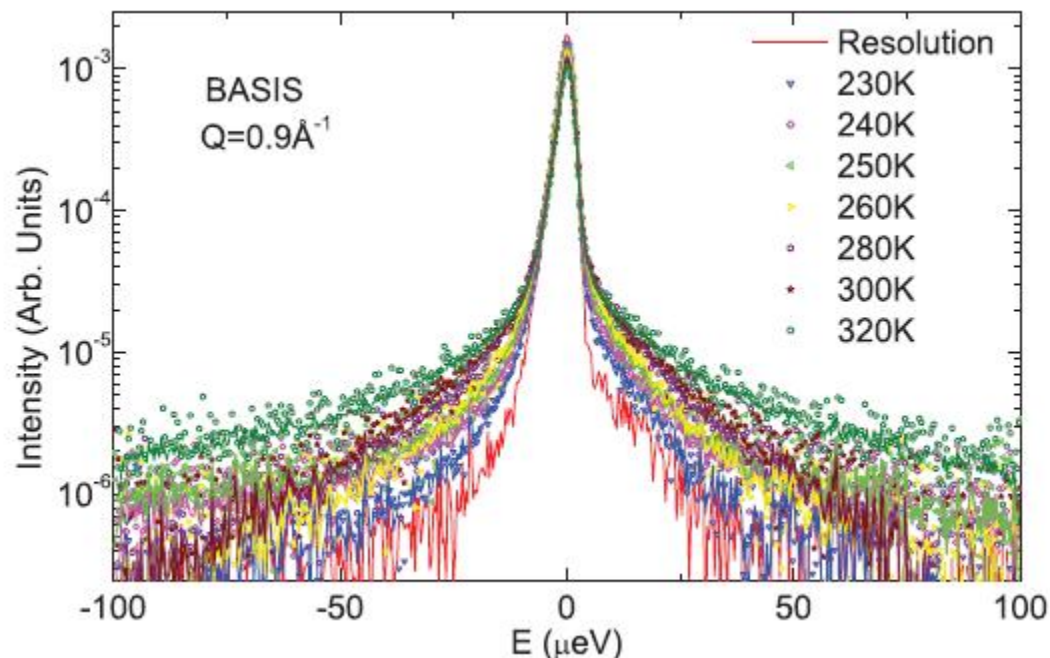
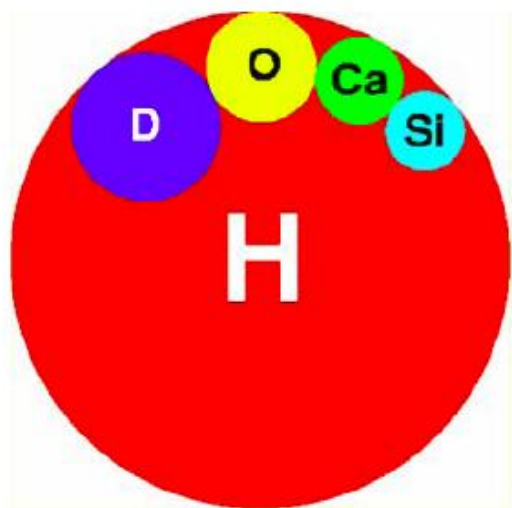
Annular vanadium standards  
5 min at 500 kW (all detectors)



60 Hz, center of the  
chopper transmission  
band on the elastic line

Incident flux on the  
sample: about  $1.3 \times 10^7$   
 $\text{n/cm}^2\text{s}$

# We measure single-particle dynamics in H-bearing samples in 90 % of our experiments



PHYSICAL REVIEW E 84, 031505 (2011)

Diffusion processes in water on oxide surfaces: Quasielastic neutron scattering study of hydration water in rutile nanopowder

Xiang-qiang Chu,<sup>1</sup> Georg Ehlers,<sup>1</sup> Eugene Mamontov,<sup>1\*</sup> Andrey Podlesnyak,<sup>1</sup> Wei Wang,<sup>2</sup> and David J. Wesolowski<sup>3</sup>

Total neutron scattering cross-section

Hydrogen dwarfs all the other elements due to its huge **incoherent** scattering cross-section:

$$\sigma_{\text{coh}} = 1.76 \text{ barn}, \quad \sigma_{\text{inc}} = 80.26 \text{ barn}$$

# Watch the following development in the near future

## IN16B: commissioning of the two projects BATS and GaAs

<https://www.ill.eu/news-press-events/news/scientific-news/in16b-commissioning-of-the-two-projects-bats-and-gaas/>

## MIRACLES

### Backscattering Spectrometer

MIRACLES will be the time-of-flight backscattering instrument of the European Spallation Source.

<https://europeanspallationsource.se/instruments/miracles>



# Neutron backscattering technique, BASIS and beyond: Conclusion

- Backscattering spectrometers are built for high energy resolution; this is a must!
- The feature of BASIS most appreciated by users (besides the high count rate) is a combination of a high energy resolution and a broad accessible range of energy transfers; this is the only way to probe multiple dynamic processes at once
- Exciting developments are underway in Europe in elsewhere

## Acknowledgement

Scientific User Facilities Division, Office of Basic Energy Sciences, US Department of Energy

**Question 1 (easy): Would a liquid sample give rise to any elastic scattering, irrespective of the temperature? How about supercooled liquids?**

**Question 2 (medium): The resolution function is measured best when the sample is cooled down to cryogenic temperatures. Why? Can you think of systems where this approach fails (even at helium temperatures)? Hint: can you think of systems where 100 K is not low enough for the resolution measurement – there are many of them?**

**Question 3 (difficult): A typical sample-analyzer-detector arrangement is usually perfectly cylindrical with respect to the vertical axis passing through the sample center. Yet the shape of the resolution functions is often Q-dependent (that is, dependent on the scattering angle in the horizontal plane). Why? When is this effect negligible, and when not? Hint: consider the incident beam propagation.**