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National Neutron Scattering Facility

# Outline QuasiElastic Neutron Scattering from an user point of view

## Part I : why neutrons ?

context and experimental probes

Role of the experimentalist :user, facility scientist

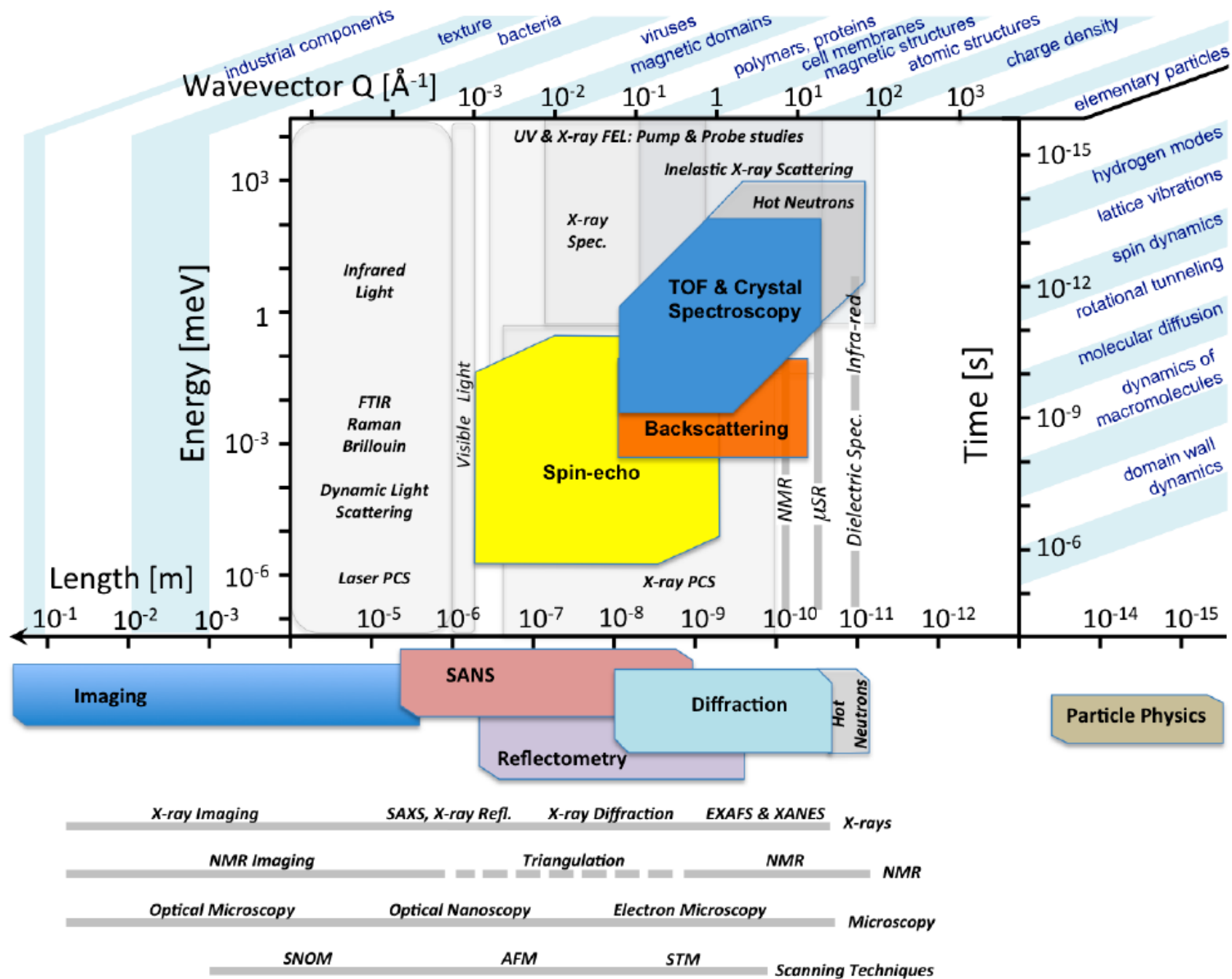
QENS spectrometers

## Part II : what are the observables?

constraints on measurements, limitations

Models and theories

Sample environment : next challenges



## good reasons to use neutrons

- Cover large scales of time and space simultaneously
- A unique probe for the magnetism
- Complementary to the other techniques; give access directly in observable relevant and defined well ( $S(Q)$ ,  $S(Q, \omega)$ ,  $\chi(Q, \omega)$ , dispersion curves)

• Neutron

- Neutron scattering methods are pluridisciplinary
- it provides final answers to fundamental questions and
- a solid background to support any other techniques ( X rays, NMR, Numerical Simulations..)

Their wavele

The interacti

The neutrons

The neutrons

The use of va

**thanks to well controlled and well known observables providing absolute quantities.**

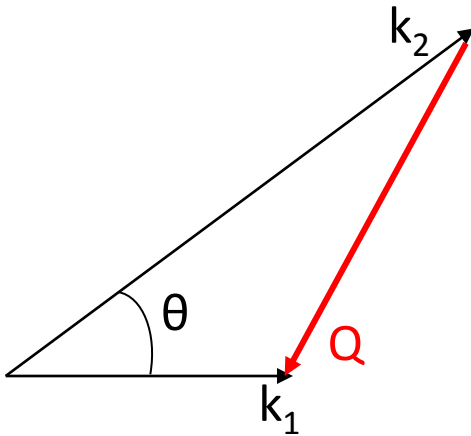
# Comparison with x rays and light

$$\mathbf{Q} \equiv \mathbf{k}_1 - \mathbf{k}_2$$

$$Q^2 = k_1^2 + k_2^2 - 2|\mathbf{k}_1||\mathbf{k}_2| \cos \theta$$

$$\hbar\omega \equiv E_1 - E_2$$

$$Q_{el} = 2|\mathbf{k}_1| \sin(\theta/2) \\ = (4\pi/\lambda) \sin(\theta/2)$$



**Neutrons:**

$$E = \frac{h^2}{2m_n} \left( \frac{1}{\lambda} \right)^2$$

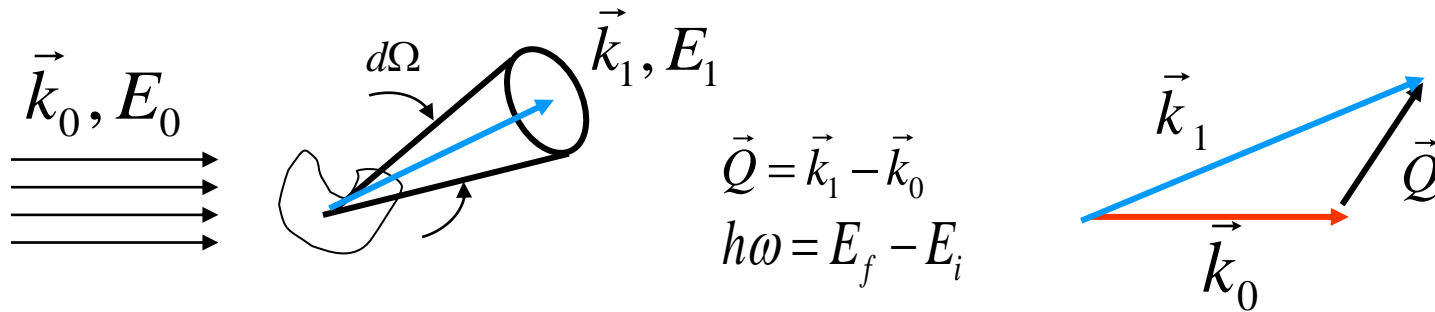
$$E \text{ (meV)} = 81.81 / \lambda^2$$

**X Rays and Light scattering:**

$$E = hc \left( \frac{1}{\lambda} \right)$$

$$E \text{ (keV)} = 12.4 / \lambda$$

( $\lambda$  in Å)

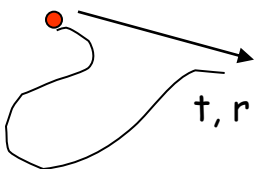


Measured Intensity  $\rightarrow \frac{\partial^2 \sigma}{\partial \Omega \partial \omega} \approx N^* \sigma_{Scat} * S(\vec{Q}, \omega) \leftarrow$

Scattering cross-section  $\nearrow$  **Dynamical Structure Factor**  
The "Physics" is here

$S(\vec{Q}, \omega)$  Is the FT  $G(r, t)$  (van Hove correlation function)

$t=0, r=0$



$$S(\vec{Q}, \omega) = \frac{1}{2\pi} \int G(\vec{r}, t) e^{i(\vec{Q}\vec{r} - \omega t)} d\vec{r} dt$$

van Hove correlation function:  $G(r, t)$  is the probability to find a particle at a distance  $r$ , at time  $t$ , provided it was at  $r=0$ , at  $t=0$ .

# QUASI ELASTIC NEUTRON SCATTERING : QENS

Measure of scattering processes involving small amounts of energy exchange, classical approximation (  $|\hbar\omega| \ll \frac{1}{2}k_B T$  )  
*i.e.* in the low energy region of inelastic spectra close to 0

**Dynamical phenomena at  $10^{-13}$  to  $10^{-7}$  s**

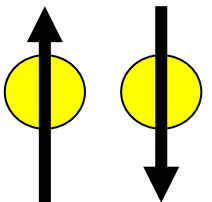
**Motions explored in space on lengthscales comparable with  $\lambda$  of the neutrons**

Vibrational displacements, librations, jump distances, diffusion paths, correlation lengths ( **nano to micro** )

**Observables : Dynamical structure factor,  $S(Q,w)$  or intermediate scattering function, mean square-displacements, self diffusion coefficient, relaxation time, Reptation Rouse modes, friction coefficient, Rotational diffusion, EISF, VDOS,  $C_p$**

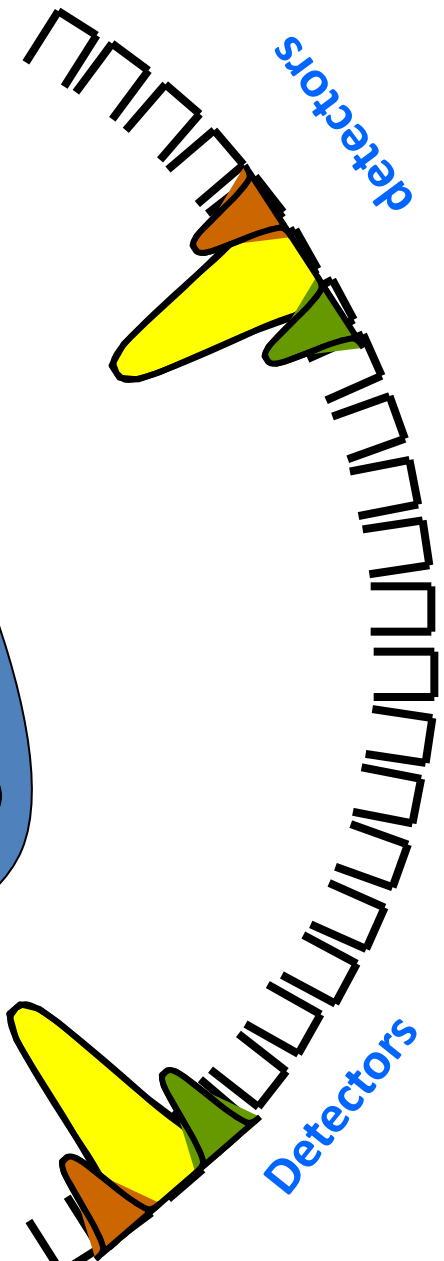
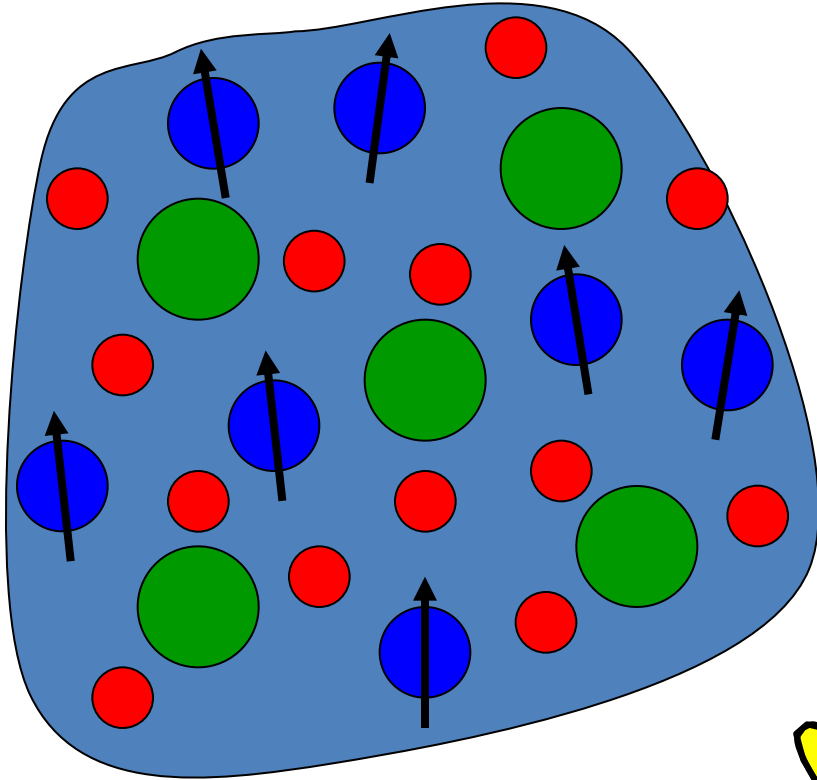
# Sample where atoms are moving

Neutron Source  
The probe



Neutrons have a spin

Scattering with or without spin flipping



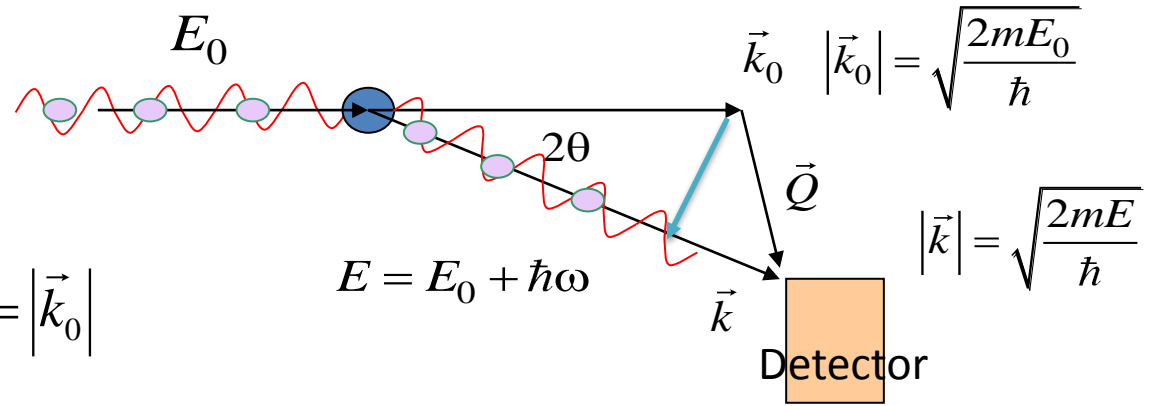


# Elastic quasielastic and inelastic scattering of neutrons

Incoming Neutron

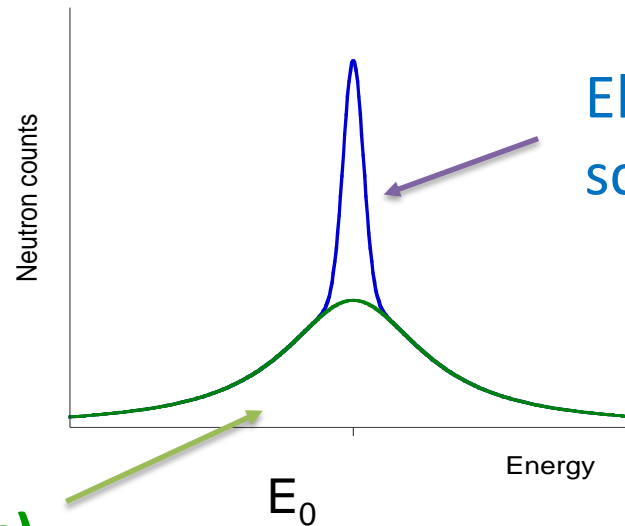
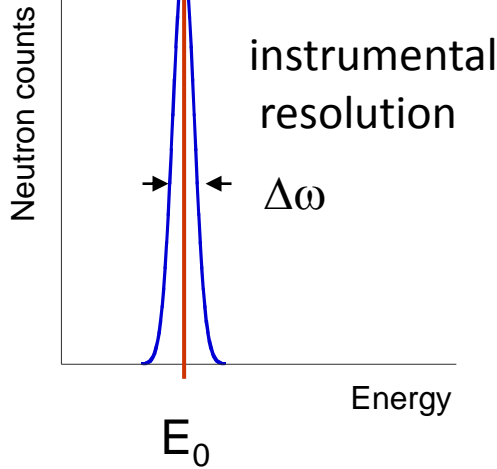
$\lambda$ : 2 to 10 Å

$E_0$ : 1 to 10 meV

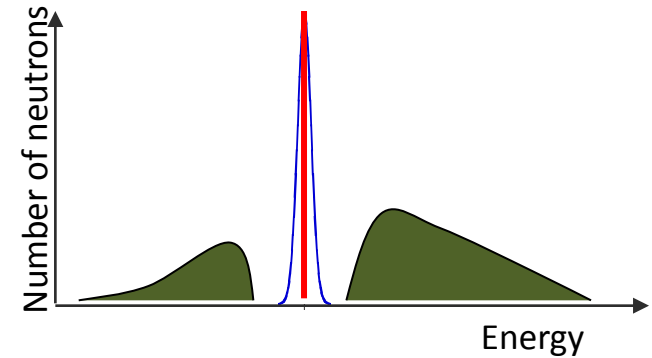


Technically a TOF spectrum is accumulated at a fixed scattering angle for each detector

$$Q_{elastic} = \frac{4\pi}{\lambda_0} \sin \theta \quad \text{and} \quad |\vec{k}| = |\vec{k}_0|$$



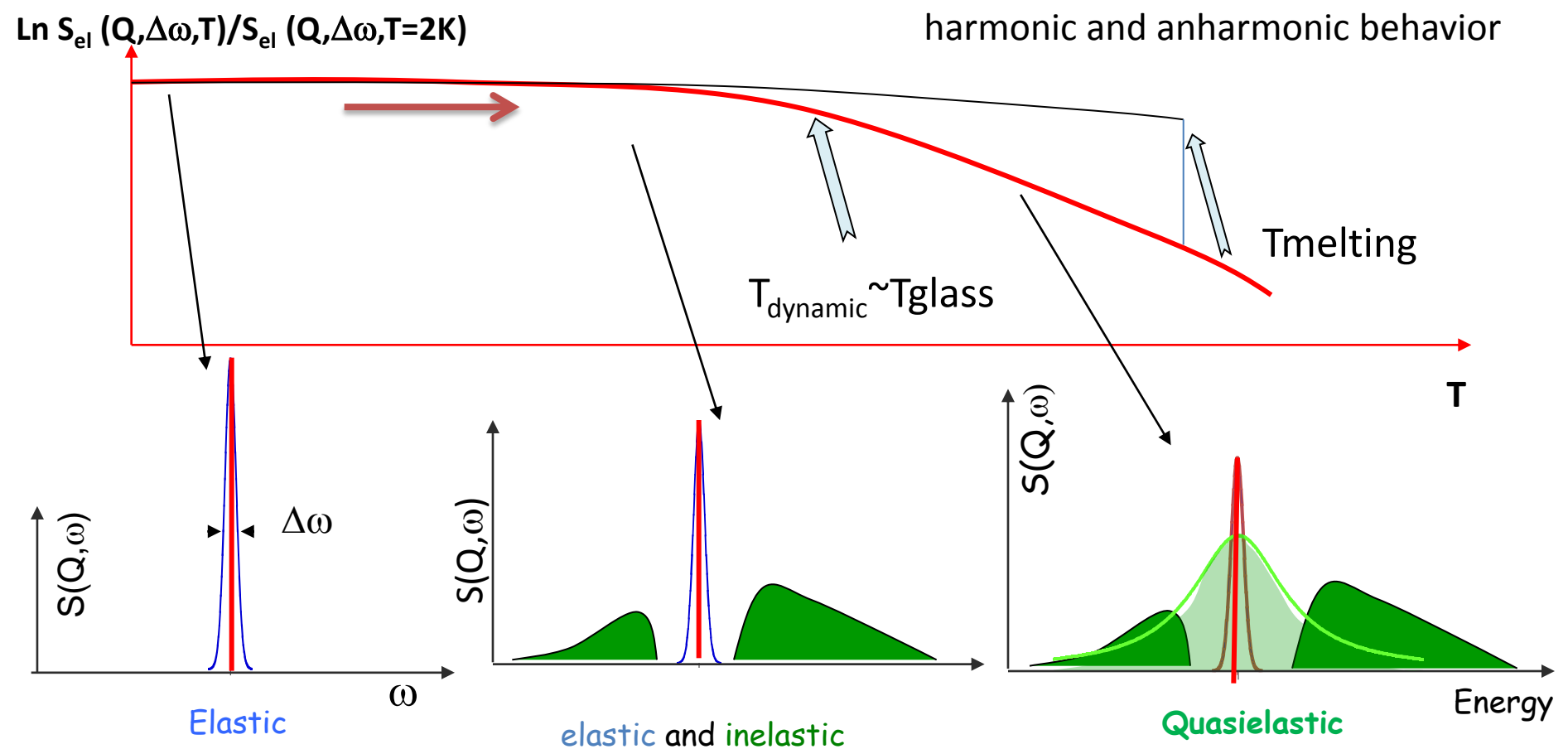
Elastic and inelastic



diffusif ( $10^{-9} - 10^{-12}$  s)  
quasi elastic broadening

# scenario of quasielastic scattering as T increases

## Molecular liquids and polymers



→ To cover a wide w range requires the combination of several instruments

# Speed and wave length of the neutron

$\lambda$ (Å)	$v$ (m/s)	$k$ (Å <sup>-1</sup> )
<b>0,5</b>	<b>7 912</b>	<b>12,6</b>
<b>1,0</b>	<b>3 956</b>	<b>6,3</b>
<b>1,5</b>	<b>2 637</b>	<b>4,2</b>
<b>2,0</b>	<b>1 978</b>	<b>3,1</b>
<b>2,5</b>	<b>1 582</b>	<b>2,5</b>
<b>5,0</b>	<b>791</b>	<b>1,3</b>
<b>10,0</b>	<b>396</b>	<b>0,6</b>
<b>20,0</b>	<b>198</b>	<b>0,3</b>

# Sequences of steps for an experiment

## Before the measurement

Facility scientists,  
engineers and technicians

- Thermalisation
- Monochromator
- Collimator
- Polarisation
- Detector efficiency

**user** interacting at the facility

- Sample holder and position
- Sample environment ( T, p, B)
- Choice of the E and Q resolution
- Low background , parasites

**Interpretation  
of the data  
Models  
Theories  
applications  
questions**

## after the measurement

- Speed,(particle character)
- Wavelength ( wave character)
- direction,
- polarisation

- Normalisation, Vanadium
- Background soustraction
- Multiple scattering
- Absorption, geometry

**motions**

**{**  
**0.1psec to 500nsec**  
**.5meV à 20meV**  
**1000Å à 1 Å**  
**}**

Several  
instruments

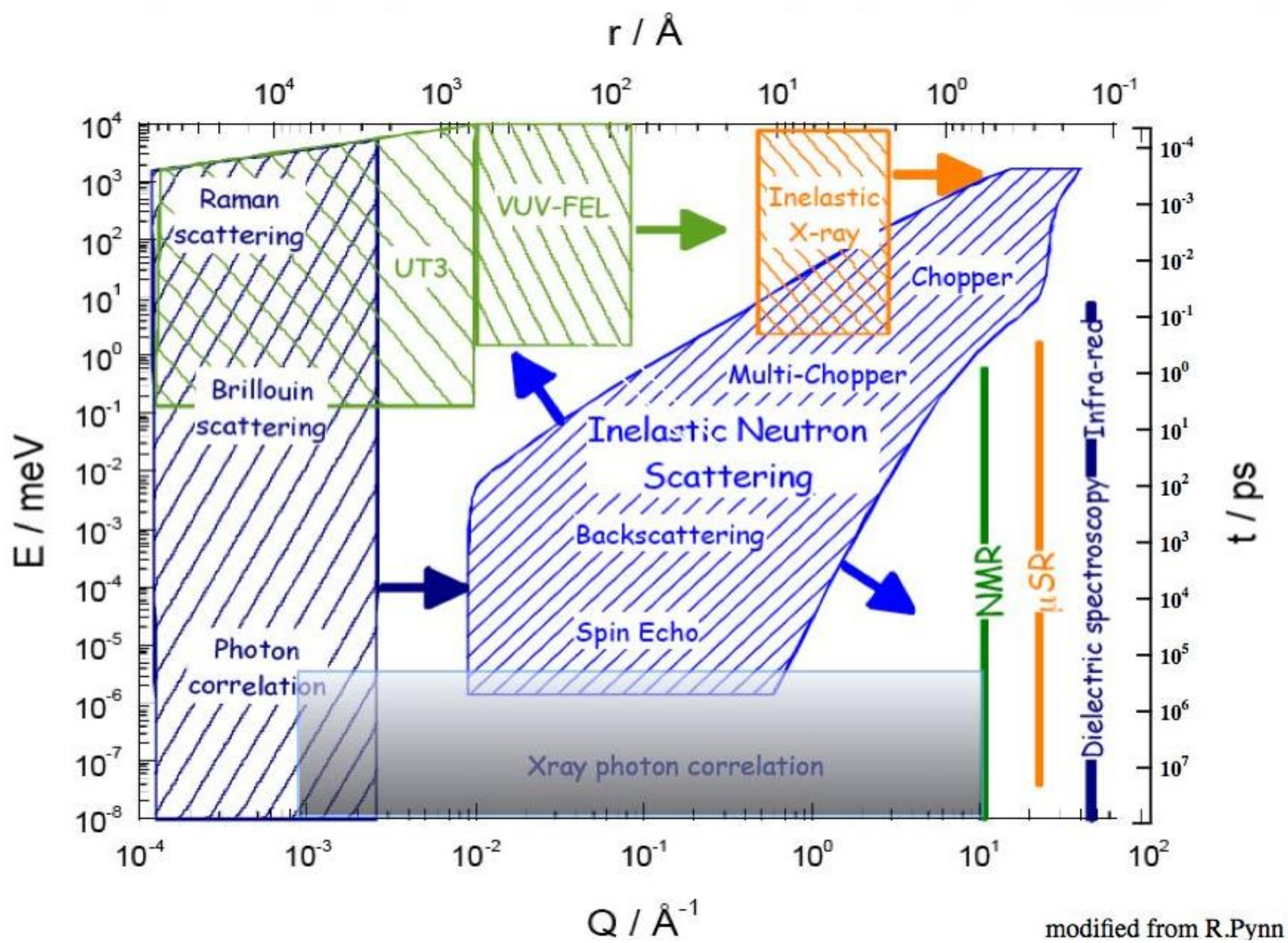
## Triple Spectrometer

**Time of Flight Spectrometer** (*based on energy transfer analysis*)

**Backscattering Spectrometer**

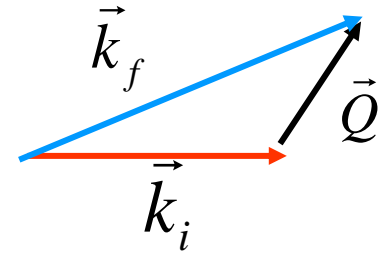
**Neutron spin Echo Spectrometer (NSE and NRSE)**

*Based on the Fourier time analysis of the scattered intensity*



modified from R.Pynn

# Triple axis and Time of flight approaches



Create high continuous flux of monochromatic neutrons ( $k_i$  fixed)  
continuous detection of monochromatic neutrons ( $k_f$  fixed)

**Triple axis  
spectrometer**

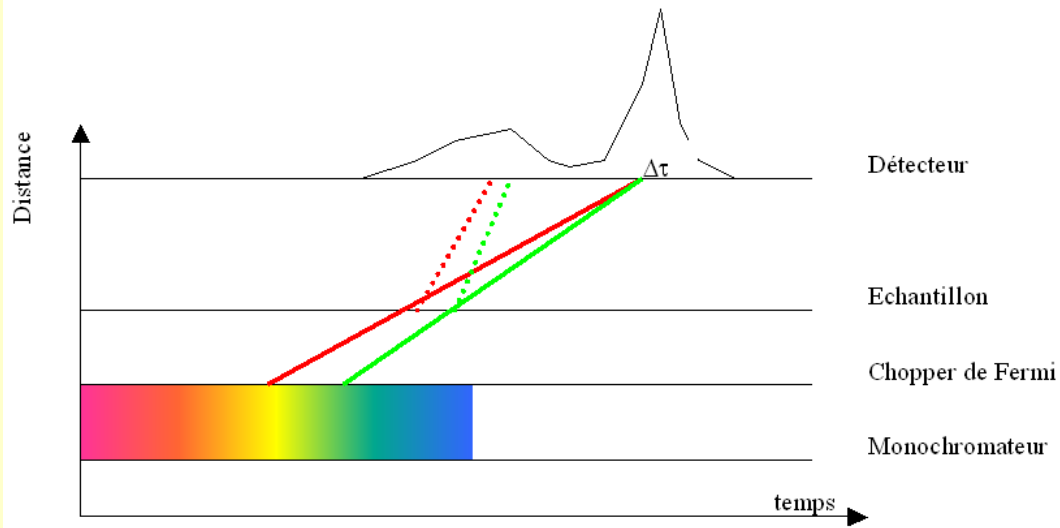
Create a high flux of pulsed monochromatic neutrons ( $k_i$  fixed)  
Detection as a function of time ( $k_f$  variable)

**Direct geometry  
Time of flight**

Create high flux white neutron beam ( $k_i$  variable)  
Detection of monochromatic neutrons as function of time ( $k_f$  fixed)

$$\left( \frac{d^2\sigma}{d\Omega d\omega} \right) = \frac{k_f}{k_i} \frac{\sigma_{sc}}{4\pi} N S(\vec{Q}, \omega)$$

**Indirect geometry  
Time of flight**

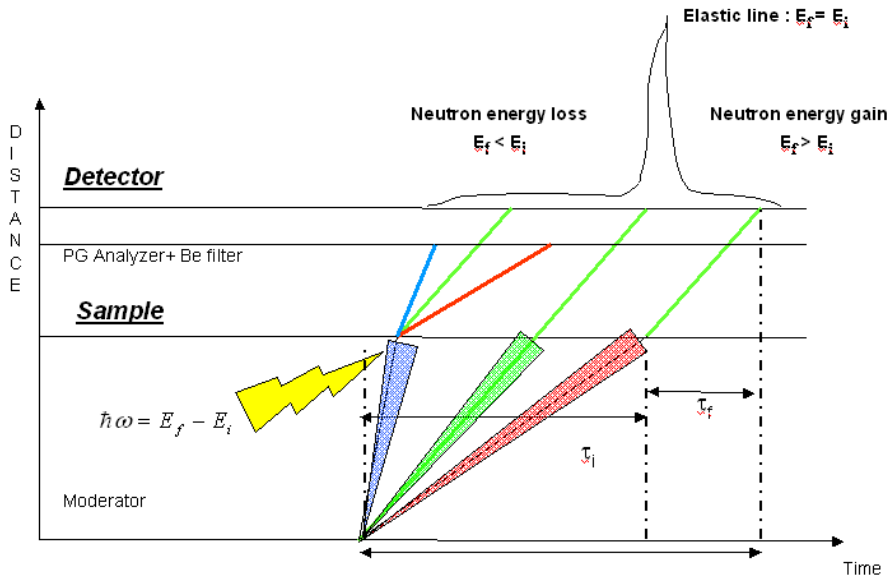


**Time focusing**  
**IN6 (ILL) – Focus (PSI)**

Select a broad incident energy band  
 +  
 The « fastest » neutrons  
 Get to the detector at the same time that  
 the « slowest » ones.

**Large flux** but resolution not triangular

**NB:**  
 Can focus in the inelastic region



**Inverted geometry**  
**QENS (ANL/Intense Pulsed Neutron Source)**  
**IRIS (ISIS)**

Use a white beam  
 + analyzer in front of detectors.

**Concurrent measurement of elastic (S(Q))**  
**AND inelastic (S(Q,w))**

On pulsed sources: measure the  
 neutron energy loss side: Bose factor not a limiting factor

Can probe far in the inelastic even at low temperature  
 Resolution ± fixed  
 High background



# FOCUS @ PSI

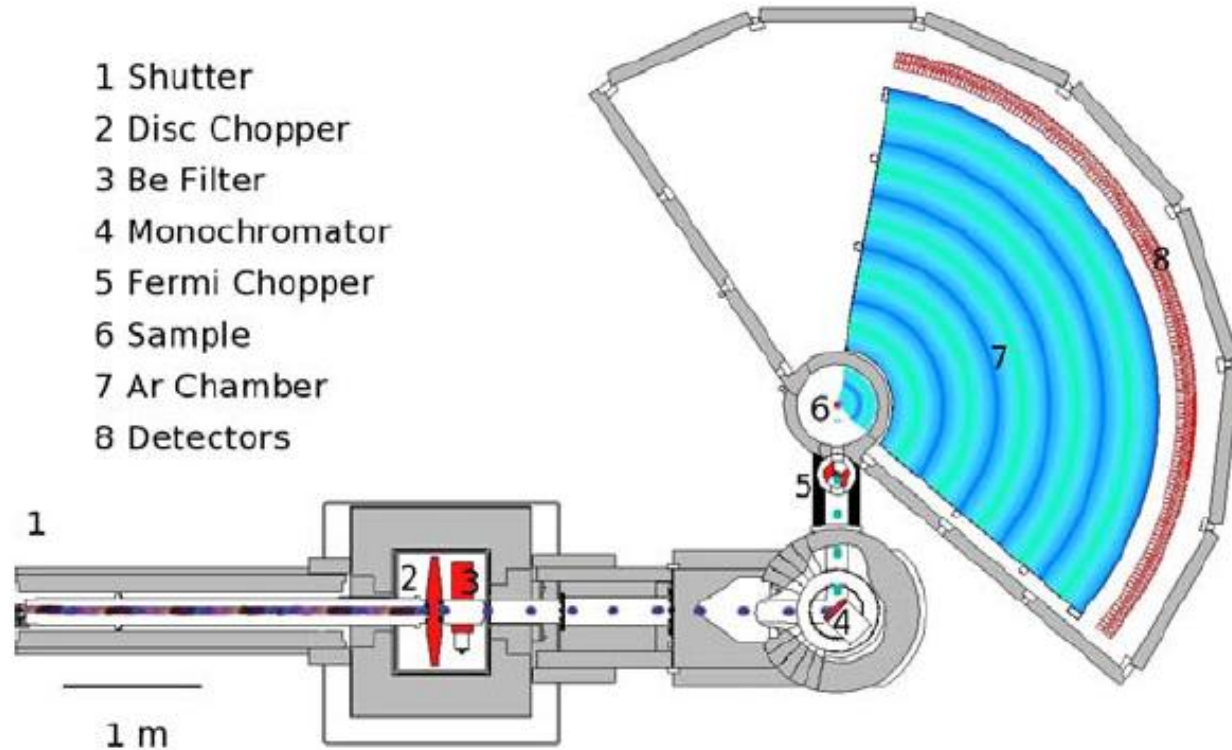


Fig. 3. FOCUS spectrometer at Paul-Scherrer Institut (PSI) [29]; FOCUS is a typical XTL-TOF spectrometer, i.e. a time-of-flight instrument with a Bragg monochromator and a time-of-flight analyzer. While the monochromator selects the incident neutron energy  $E_0$ , the energy of the scattered neutrons  $E$  is determined by measuring the neutron flight time.

# The Fa# Project @ LLB

J-M Zanotti, S Rodriguez

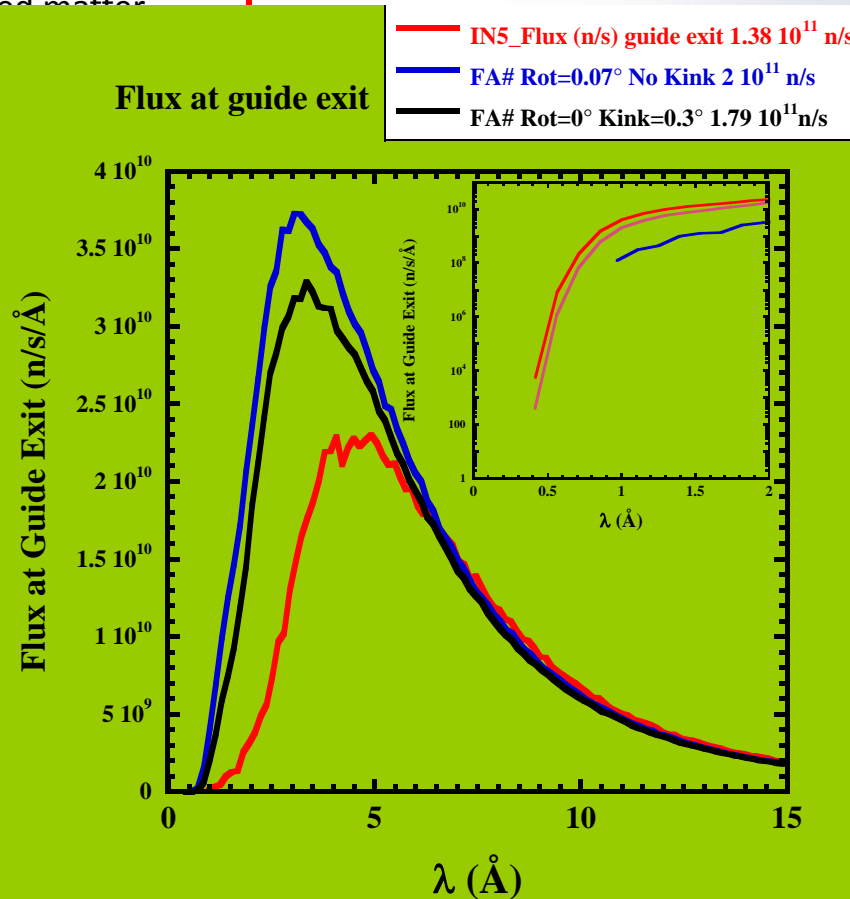
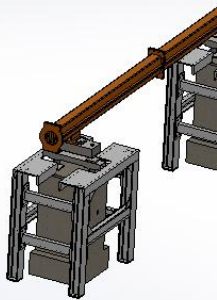
« Hybrid » Instrument :

- Time focusing ( Soft matter / Biology)
- Energy focusing (Solid state physics)

## Scientific fields

- Soft condensed matter
- Materials
- Magnetism
- Soft Matter
- Biology
- Electrolytes
- ...

Elliptic gu

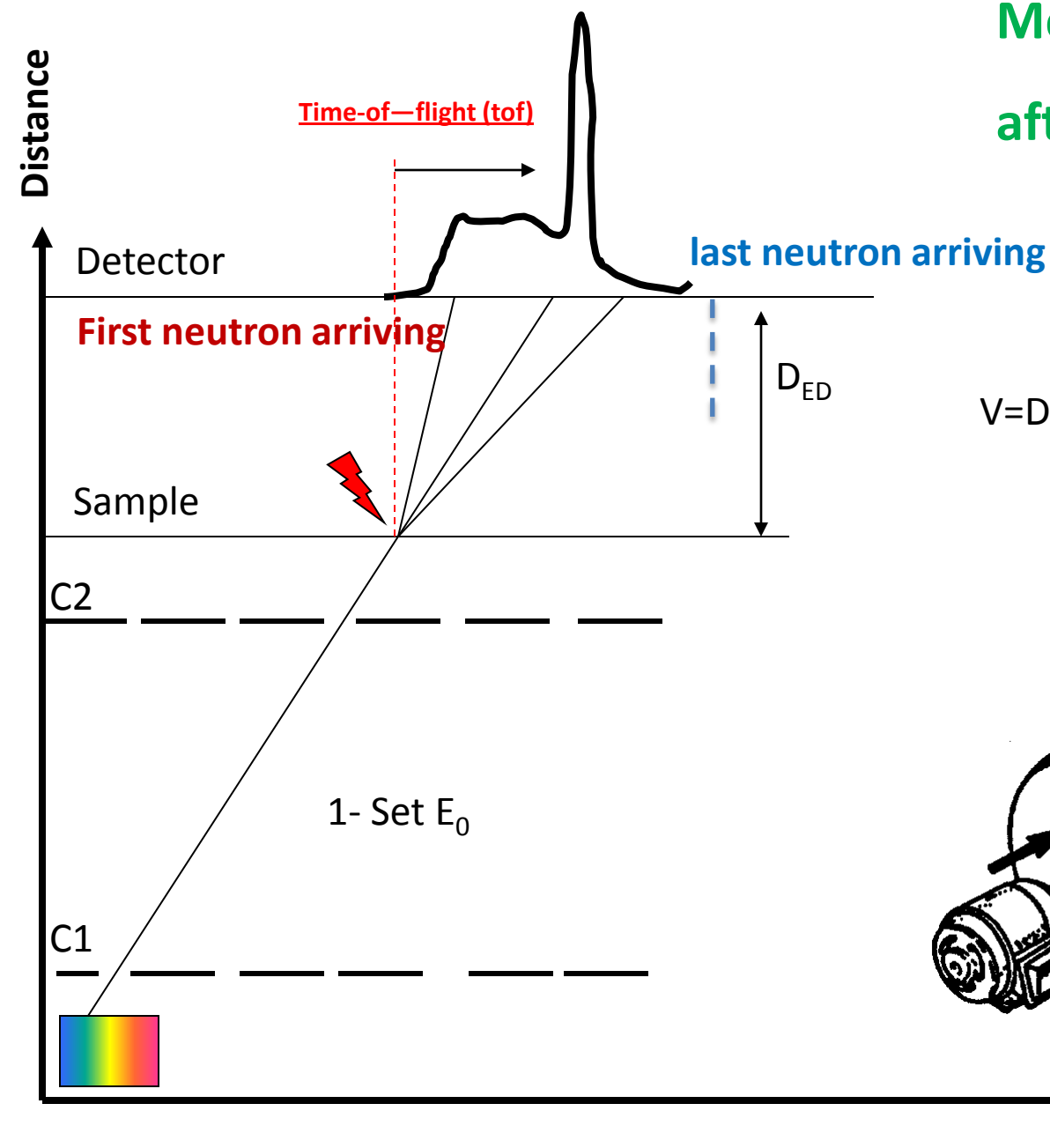


Detection  
position  
sensitive  
detectors ( $^3\text{He}$ )

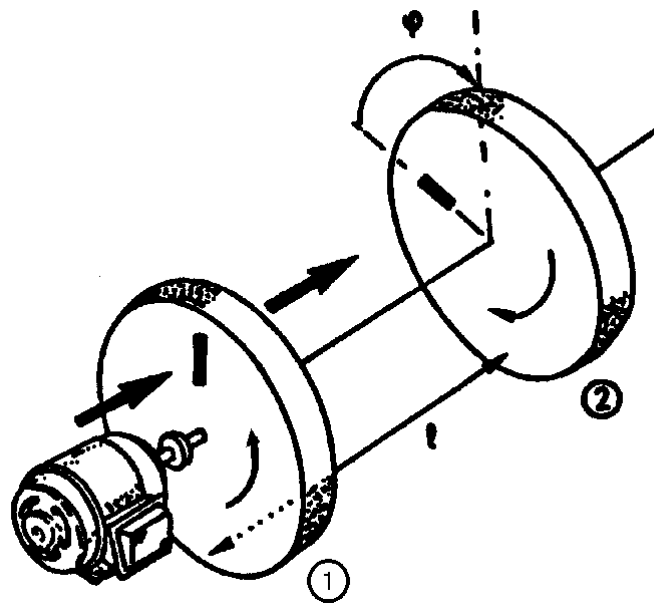
P. Lavie, LLB

# Disks choppers in cascade

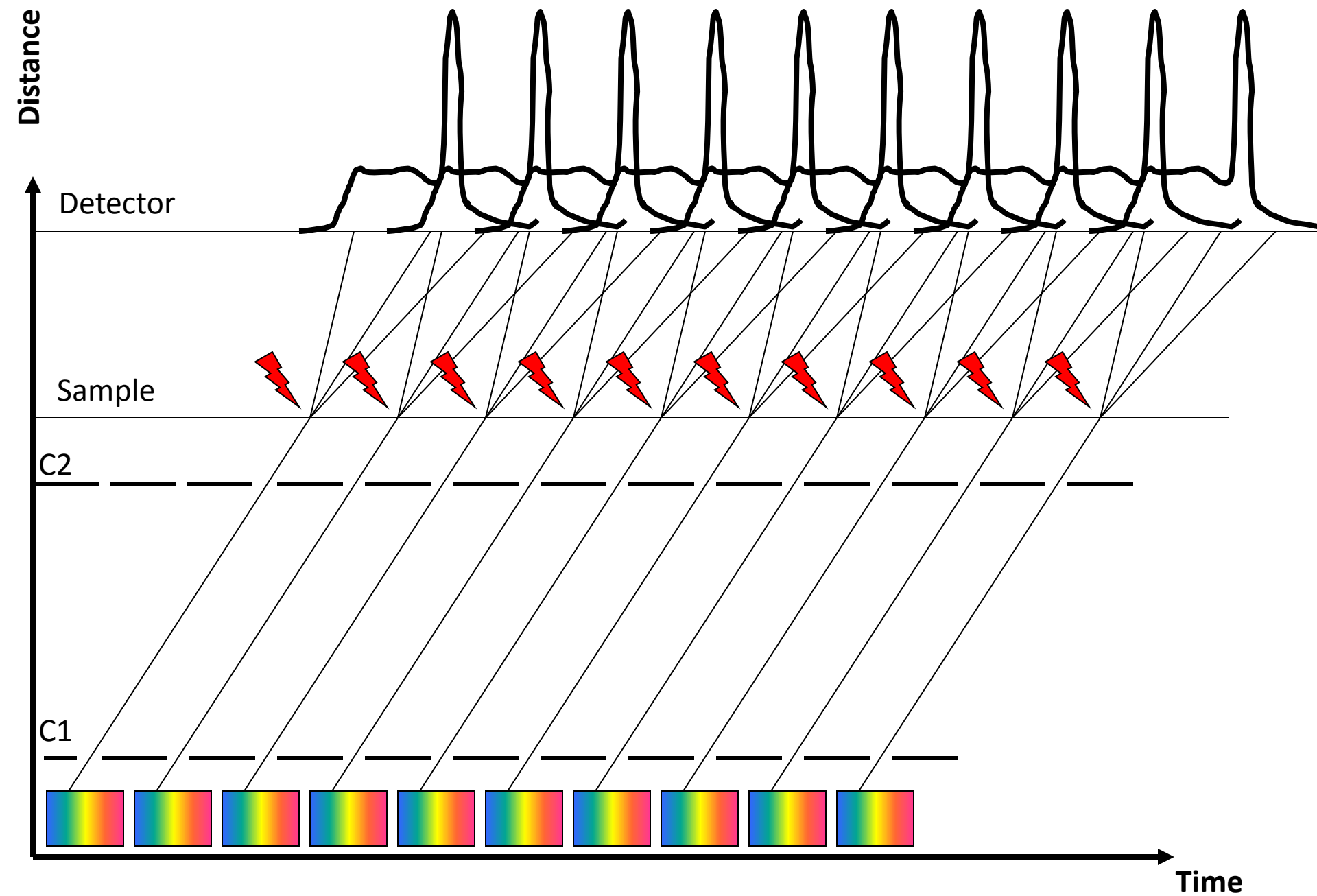
Measure the neutron energy after the sample



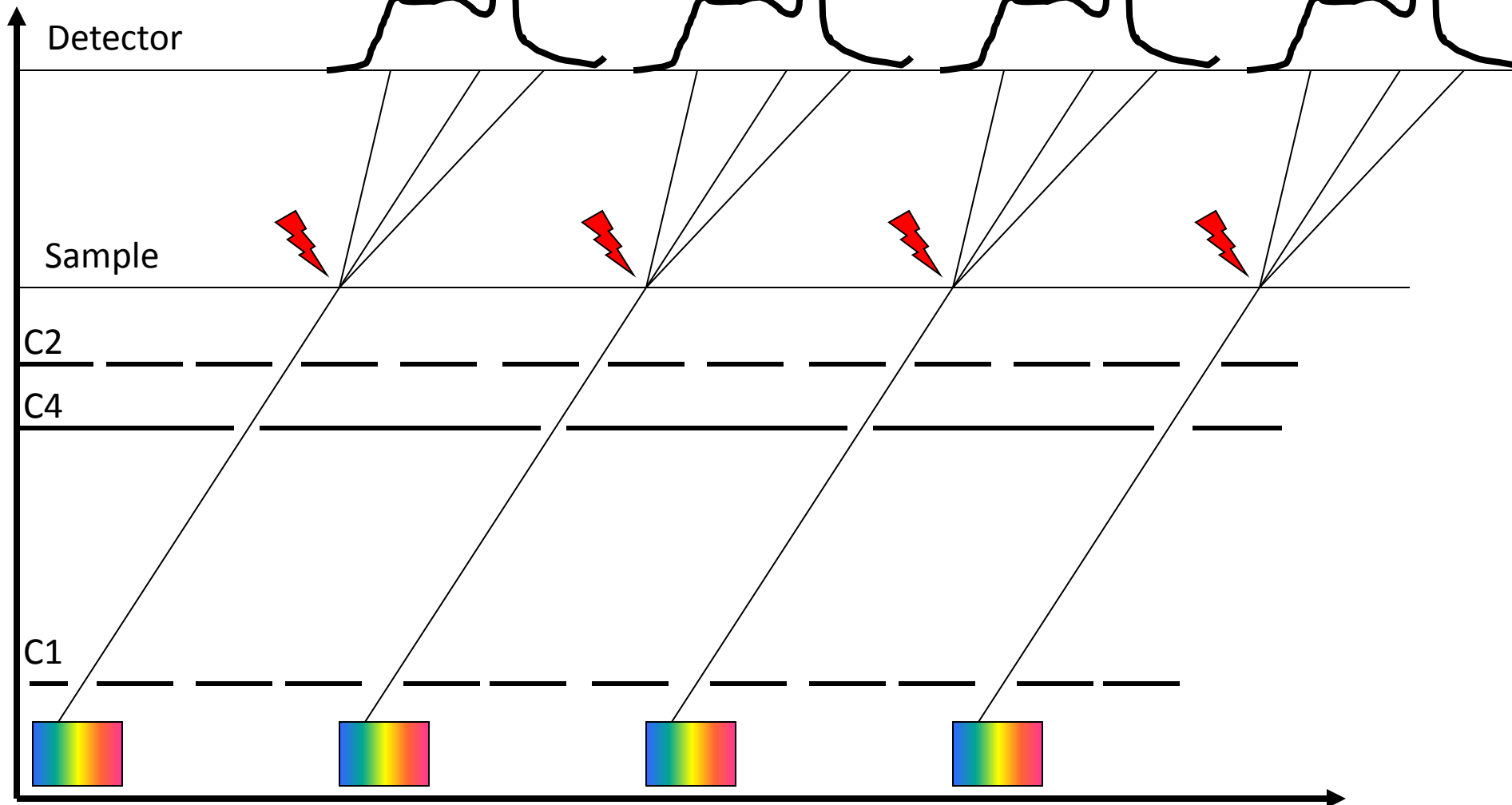
$$V = D_{ED} / \text{tof} \text{ et } E_f = 1/2 m V^2$$



# 1- Avoid frame overlap

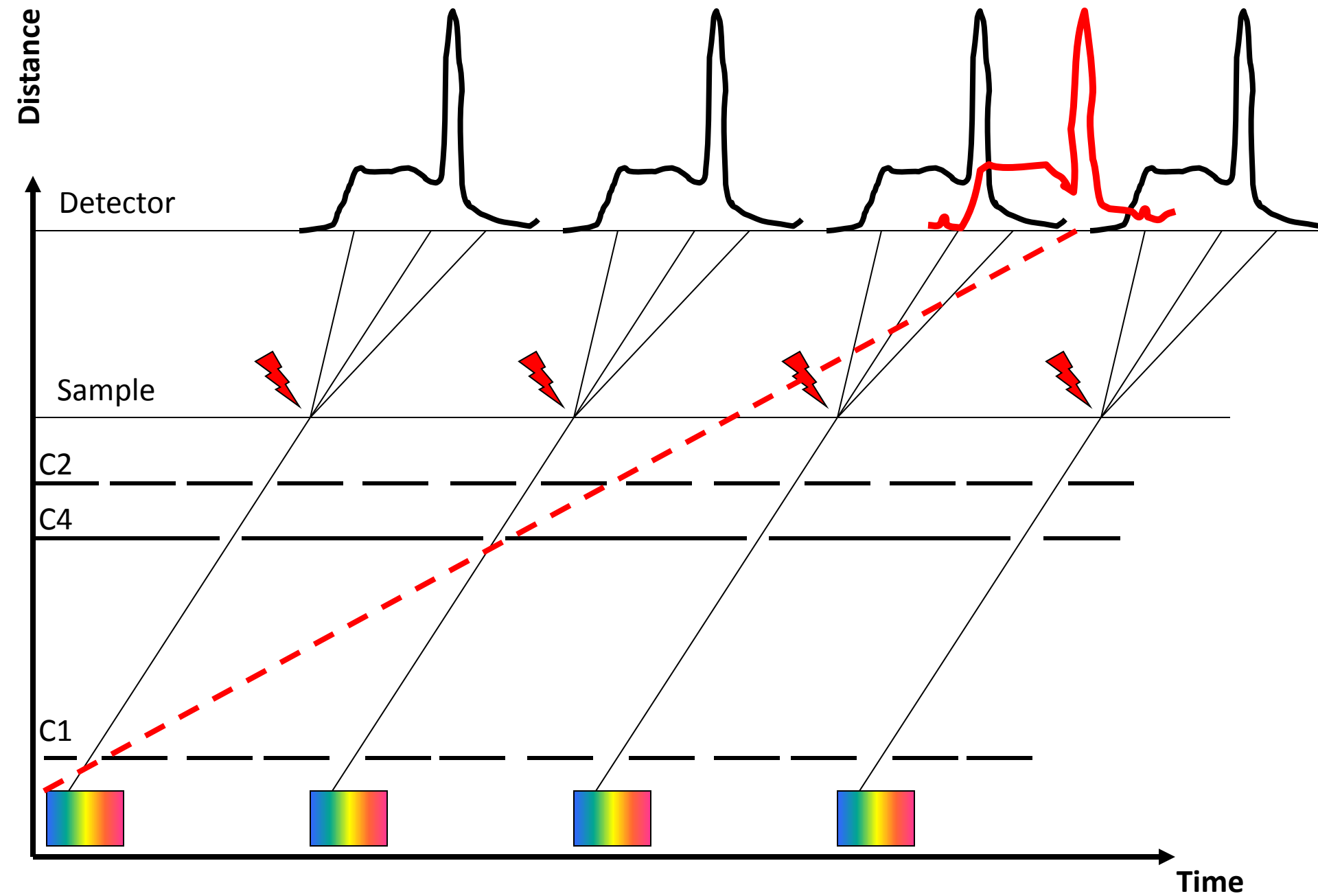


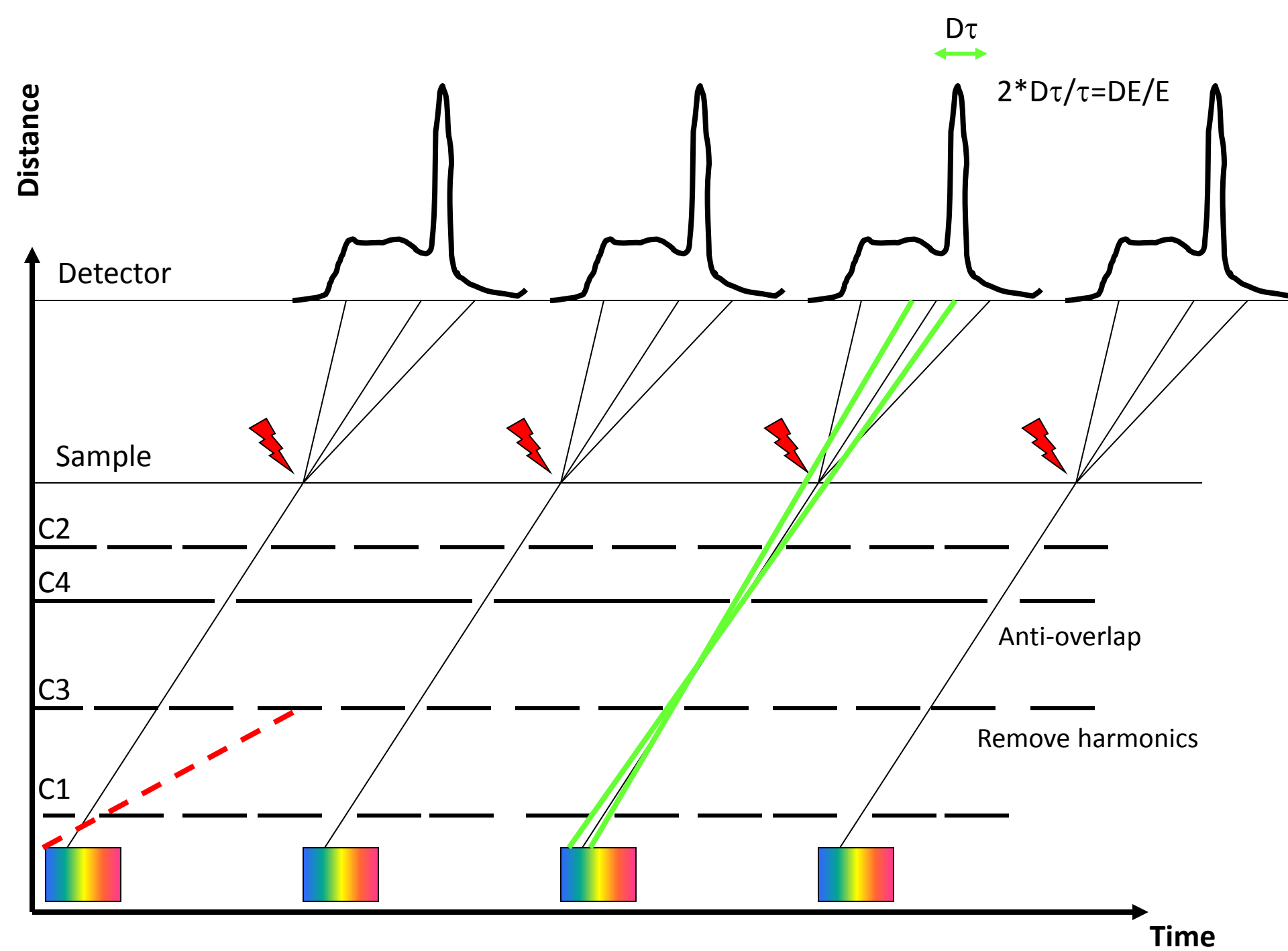
Distance



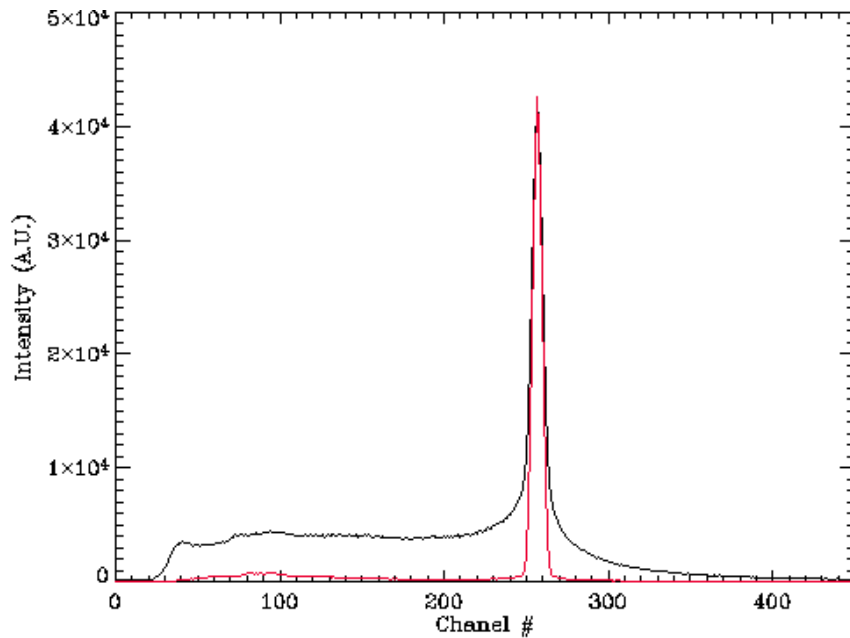
Time

## 2- Avoid any harmonics

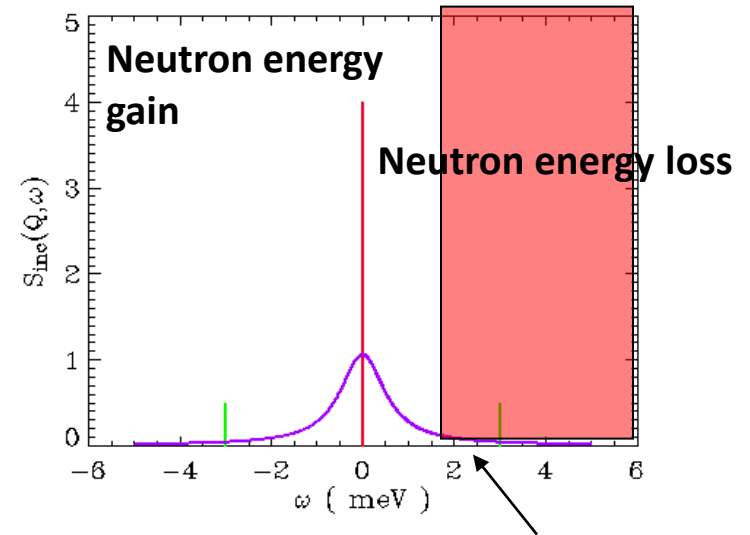
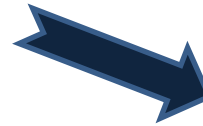




# Time-of-flight : Theory vs reality



\*  $1/t^4$



Conversion from  $(2\theta, t_{\text{time of flight}})$  to  $(Q, \omega)$

The maximum energy loss is  $E_0 \dots$

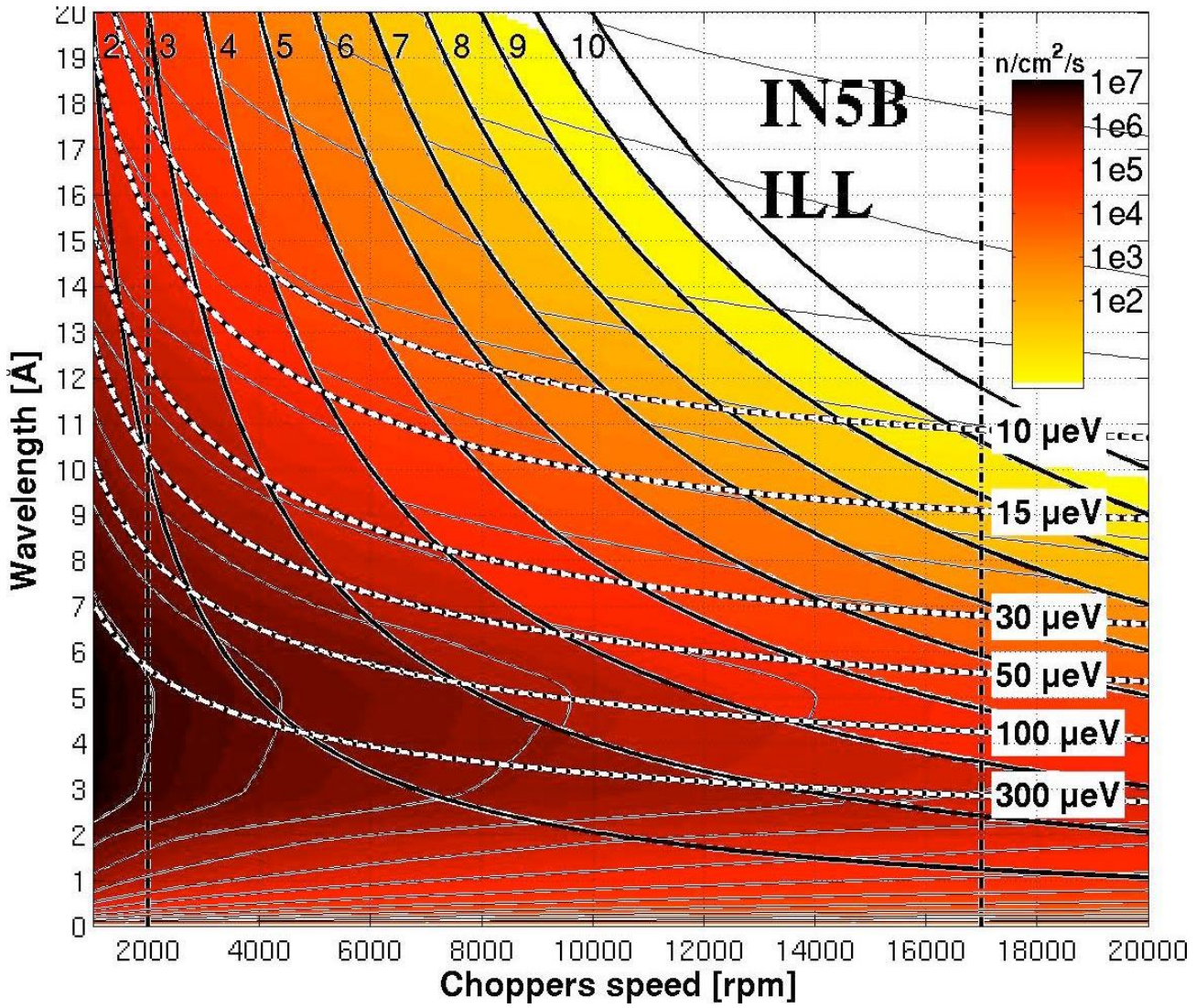
**NB:** At 298 K,  $k_B T = 25$  meV

To measure long correlation times :  
 Increase the chopper speed and/or  $I_0$  .  
 But flux drops !

$$S^{\text{Mesuré}}(Q, \omega) = S^{\text{Théo}}(Q, \omega) \otimes R(\omega)$$



Find a good compromise between **flux**,  
**energy resolution** and **wavelength**

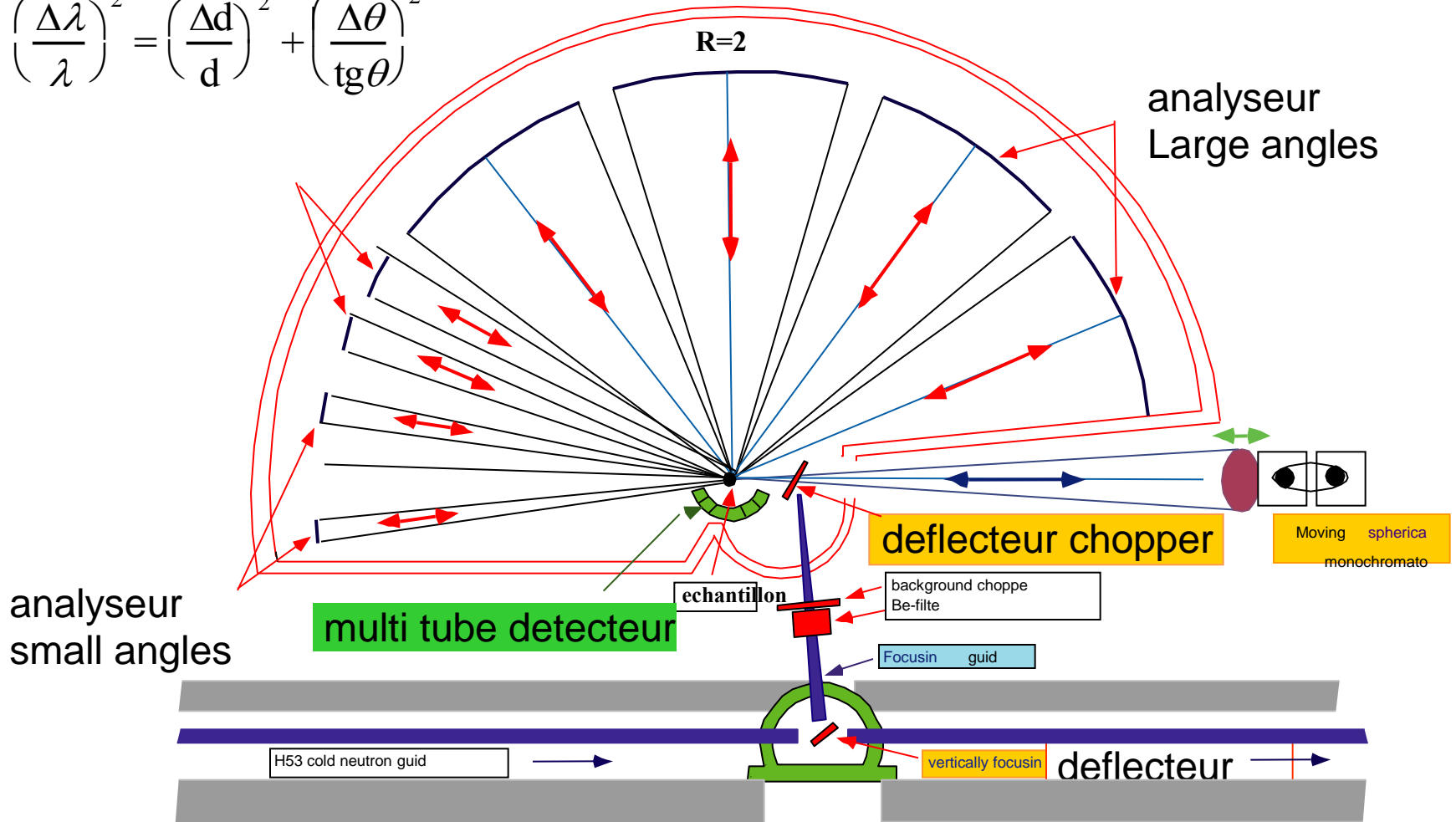


# Backscattering Spectrometers

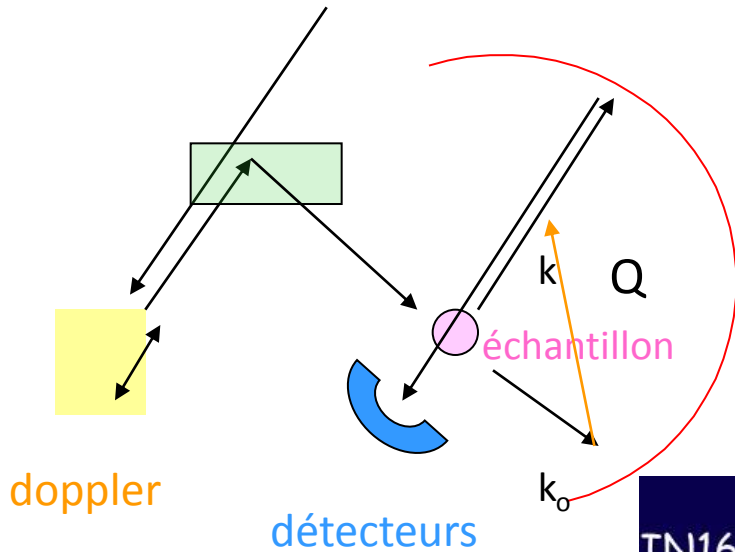
B. Frick, IN16, ILL

monochromator and analyseur : perfect crystals in backscattering ( $2q=180^\circ$ )  
 Bragg law differentiation

$$\left(\frac{\Delta\lambda}{\lambda}\right)^2 = \left(\frac{\Delta d}{d}\right)^2 + \left(\frac{\Delta\theta}{\text{tg}\theta}\right)^2$$



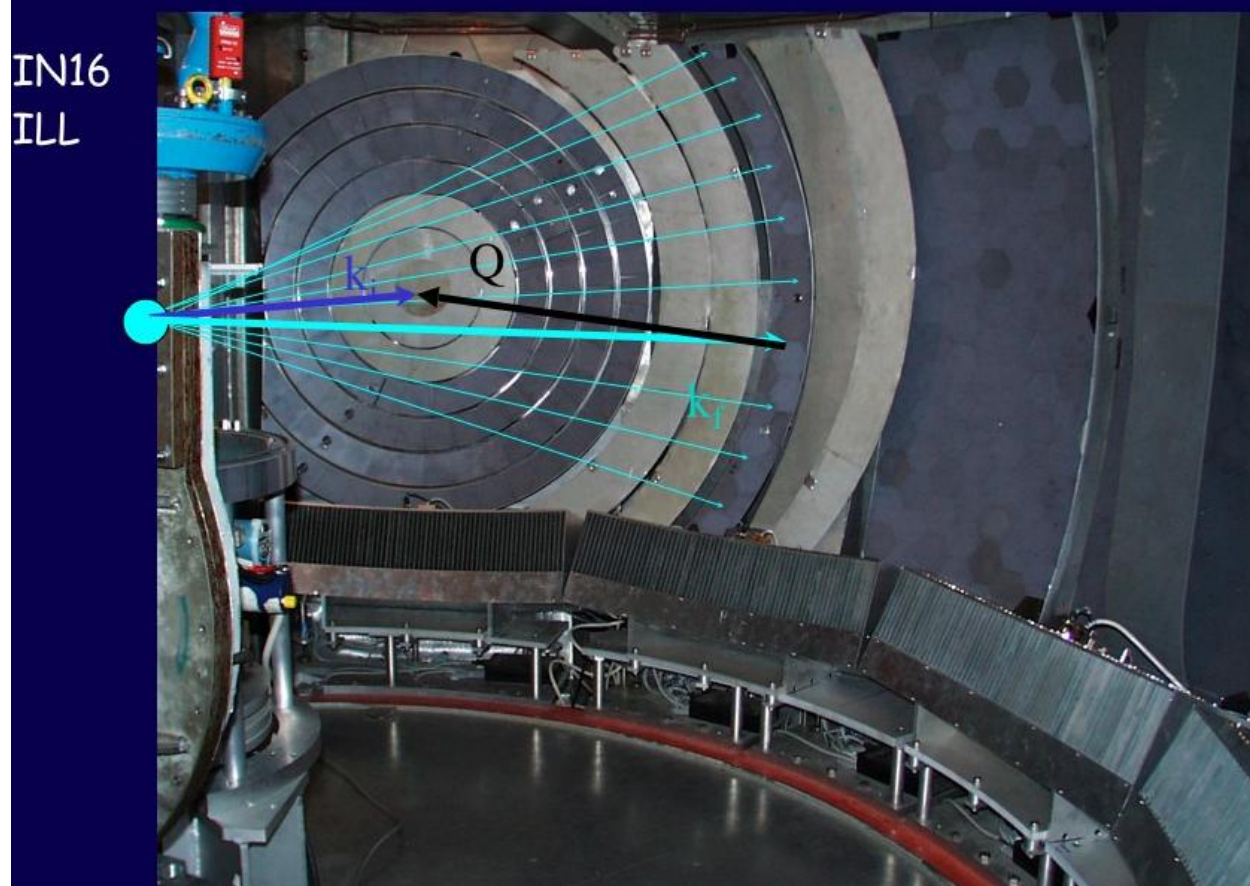
# Backscattering Spectrometers



$Q=Q_{\text{élastique}}$

Résolution  $<1\mu\text{eV}$   
Gamme  $-15 \text{ à } +15\mu\text{eV}$

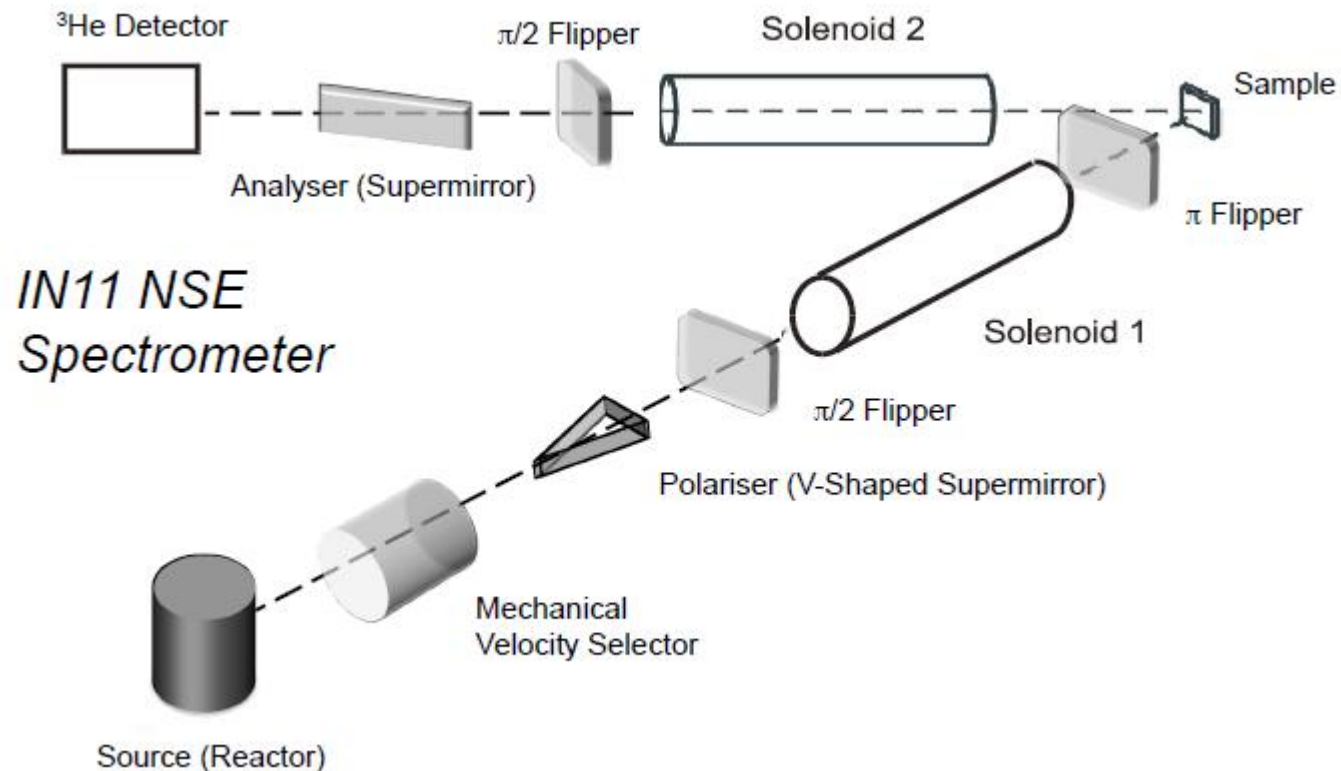
BASIS @SNS  $\pm 300 \mu\text{eV}$



# Spin Echo Spectrometers

Mezei 1972 NSE, Gähler 1987 NRSE

NSE measures the sample dynamics in the time domain, via the determination of the intermediate scattering functions  $F(Q,t)$

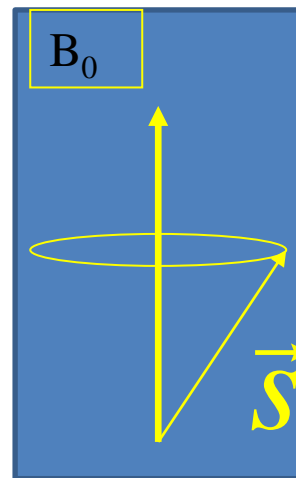
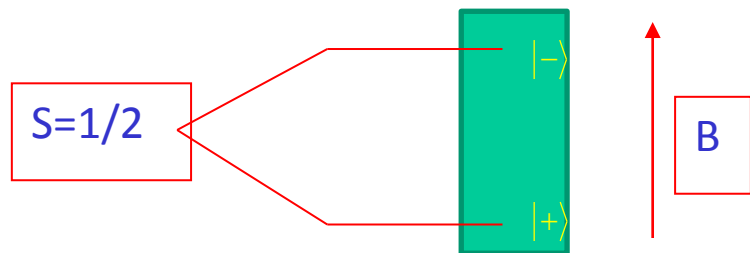


ILL, IN11A

Neutrons are polarised,  $\pi/E$  rotation, then under magnetic field

# The measured quantity : the scattered beam polarisation...

Neutron spin , precession ...



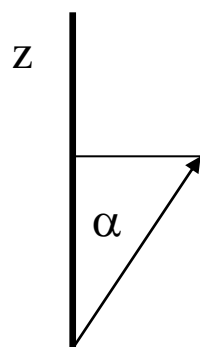
$$\frac{d\vec{s}}{dt} = \gamma \vec{s} \wedge \vec{B}_0$$

$$\omega = |\gamma_n| B_0$$

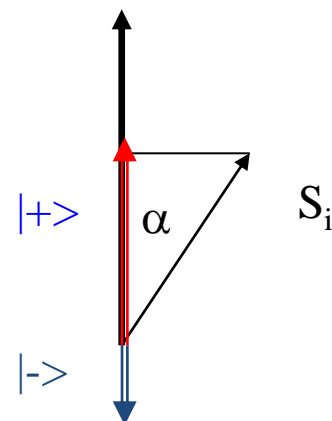
$$N = \gamma_n B_0 t / 2\pi$$

$$\gamma_n = -2913.2\pi \text{ (Gs)}^{-1}$$

$B_0 = 0$



$B_0$

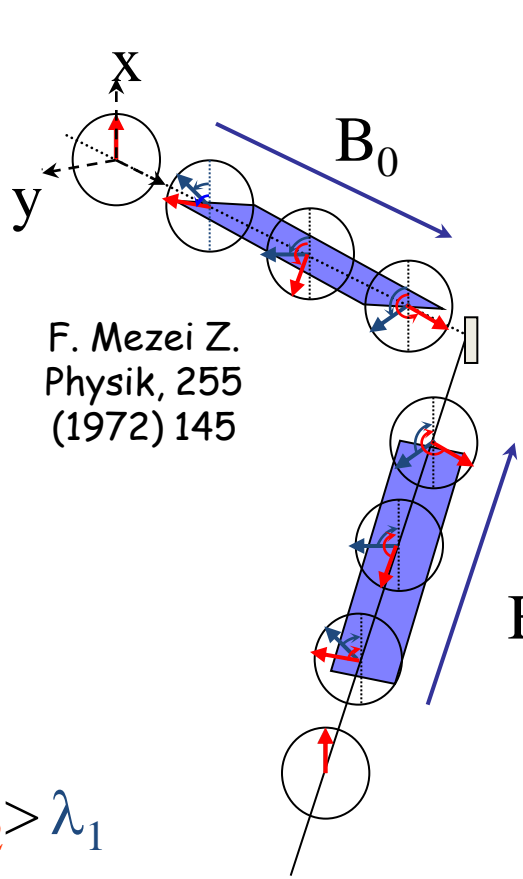


$$p_{|+\rangle} = \cos^2(\alpha/2)$$

$$p_{|-\rangle} = \sin^2(\alpha/2)$$

$$\langle P \rangle = \frac{n_+ - n_-}{n_+ + n_-} = \langle p_{|+\rangle} \rangle - \langle p_{|-\rangle} \rangle = \left\langle \cos^2\left(\frac{\alpha}{2}\right) \right\rangle - \left\langle \sin^2\left(\frac{\alpha}{2}\right) \right\rangle = \langle \cos(\alpha) \rangle$$

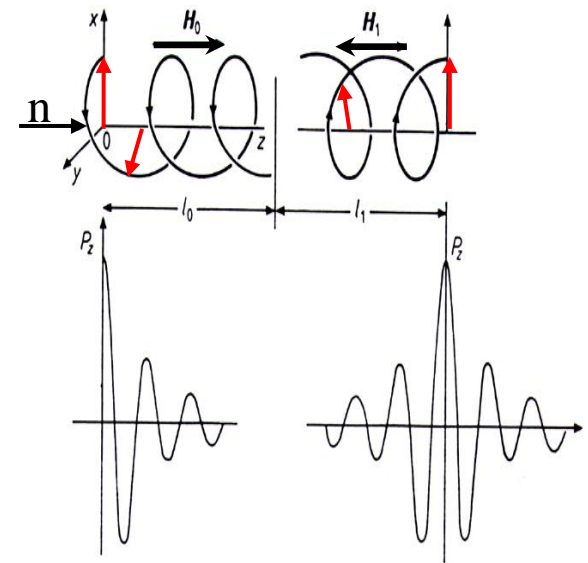
to increase the energy resolution without drastic loss of intensity as in QENS-ToF energy transfer *is causing a phase shift of the neutron spin precession angle for each scattered neutron.*



F. Mezei Z. Physik, 255 (1972) 145

$$\lambda_2 > \lambda_1$$

Polarisation



$$I(Q, t) \approx \langle P \rangle \approx \int_{-\infty}^{+\infty} S(Q, \omega) \cos(\omega \tau_{NSE}) d\omega$$

Probability of energy exchange

$S_{coh}^{-1}/3S_{inc}$  → Attention aux systèmes

$$\tau_{NSE} = \frac{m^2 \gamma \int B dz}{2\pi \hbar^2} (\lambda_0')^3$$

# Spin Echo Spectrometers

	<b>IN11</b>	<b>IN15</b>
Instrument type	NSE	NSE
Beam wavel. [ $\text{\AA}$ ]	4–12	6–27
Beam energy [meV]	0.6 – 5	0.1 – 2.3
Time range [ns]	0.001 – 50	0.002 – 1000
Momentum transfer range [ $\text{\AA}^{-1}$ ]	0.02–2.7	0.01–1.8
Max. sample flux [ $\text{cm}^{-2}\text{s}^{-1}$ ]	$2 \times 10^7$	$2 \times 10^8$
Detector efficiency	$\sim 1$	$\sim 1$
Det. backgr. [Hz]	$\sim 1$	$\sim 1$
Det. solid angle [sr]	$3 \times 10^{-4}$ IN11A $2 \times 10^{-2}$ IN11C	$4 \times 10^{-3}$

## Comparaison TOF-BS et NSE

- **Frequency measurement**
- **Scan at fixed  $\omega$**
- **$S(Q, \omega) = S(Q, \omega) \otimes R(Q, \omega)$**
- **Self motions**
- **Shorter dynamical range**
- **Good Q resolution**
- **Excitations, vibrations**

- Time measurement
- Scan at fixed t
- $S(Q, t) = S(Q, t) \cdot R(Q, t)$
- Collective motions
- Large dynamical range (3 to 4 décades)
- $\Delta\lambda/\lambda \sim 15\% = \Delta Q/Q$





# Recent Progress on Polymer Dynamics by Neutron Scattering: From Simple Polymers to Complex Materials

Juan Colmenero,<sup>1,2</sup> Arantxa Arbe<sup>1</sup>

**TABLE 2** Currently operating high-level neutron facilities in the world and the available QENS spectrometers on them

Facility	Instrument	Type
Institute Laue-Langevin (ILL)	IN10	BS
Grenoble, France	IN16	BS
www.ill.eu	IN16b <sup>a</sup>	BS
	IN13 <sup>b</sup>	BS
	IN5	ToF
	IN6	ToF
	IN11	NSE

Helmholtz Zentrum Berlin (HZB)	NEAT <sup>a</sup>	ToF
Berlin, Germany		
www.helmholtz-berlin.de		
Paul Scherrer Institute (PSI)	MARS	BS-ToF
Villigen, Switzerland	FOCUS	ToF
sinq.web.psi.ch		
Laboratoire Léon-Brillouin (LLB)	FA# <sup>c</sup>	ToF
Saclay, France	MUSES	NSE
www-llb.cea.fr		
Spallation Neutron Source (SNS)	BASIS	BS-ToF
Oak Ridge, USA	CNCS	ToF

ISIS Facility, Rutherford  
 Appleton Laboratory  
 Oxford, United Kingdom  
 www.isis.stfc.ac.uk

Maier-Leibnitz Zentrum (MLZ)  
 Garching, Germany  
 www.frm2.tum.de  
 & www.fz-juelich.de/jcns

## Quasielastic Neutron Scattering in Biology Part I: Methods

Ruep E. Lechner<sup>1</sup> and Stéphane Longeville<sup>2</sup>

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Technology Organisation (ANSTO)  
 Sydney, Australia  
 www.ansto.gov.au