

POLARIZED NEUTRON DIFFRACTION DATA ANALYSIS

$$F_M(hkl) \Rightarrow M_z(x,y,z)$$

$$F_M(q) \Rightarrow \rho_s(x,y,z)$$

- **Fourier** method $\rho_s = \sum F_M(q)e^{-iqr}$
- **Refinement** of multipoles $\rho_s = \sum p_{lm}R_l Y_{lm}$
- **MEM**, maximum entropy method and others...

Model-free methods

Fourier summation

$$\rho(\vec{r}) = \frac{1}{V} \sum_{\vec{K}}^{\text{Nobs}} F_M(\vec{K}) e^{-i\vec{K}\vec{r}}$$

Limitations:

- centrosymmetrical space group only
- exact only if infinite number of F_M 's
- artefacts due to missing F_M for weak nuclear F_N

NUMERICAL INVERSION PROBLEM

DATA

$$F_M(q) \Rightarrow \rho_s(x,y,z)$$

IMAGE

- Complete, noise -free data

1- to -1 mapping

one set $F_M(q) \Leftrightarrow$ one ρ_s

- Incomplete, noise data

1- to -many mapping

one $F_M(q) \Leftrightarrow$ many ρ_s

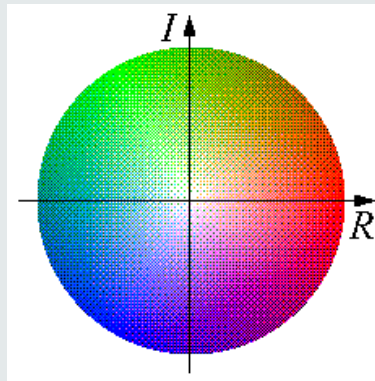
Which map to chose?

Representation of complex numbers on 2Dmap

by Kevin Cowtan, <http://www.ysbl.york.ac.uk/~cowtan>

amplitudes and phases or $\text{Re}(F)$ and $\text{Im}(F)$

Amplitude is represented by colour **saturation** and **brightness**, while phase is given by **hue**.



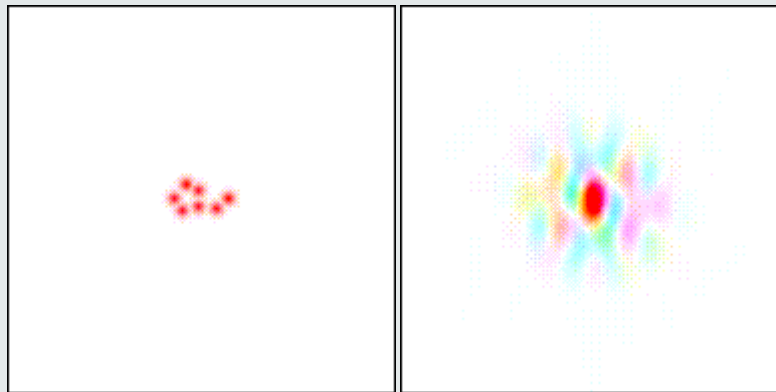
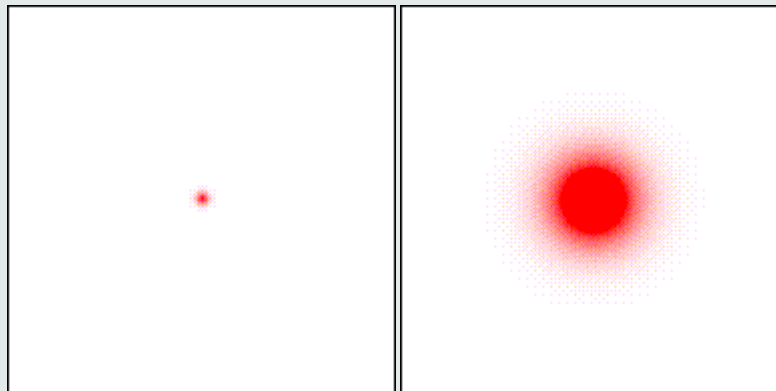
Phase **0 degrees** is *red*, **120 degrees** is *green*, and **240 degrees** is *blue*.
positive Real's are *red*, and negative Real 's are *cyan*.

White represents **zero** magnitude.

Fourier transform (FT) and Diffraction pattern

by Kevin Cowtan, <http://www.ytbl.york.ac.uk/~cowtan>

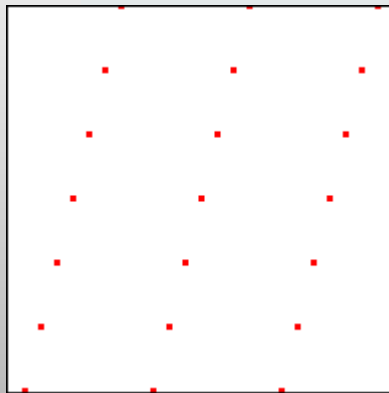
$$\rho_s = \sum F_M(\mathbf{q})e^{-i\mathbf{q}\mathbf{r}}$$



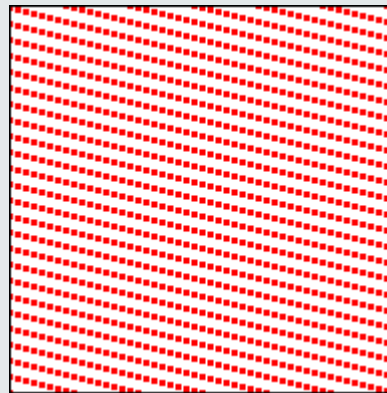
Fourier transform (*FT*) and Diffraction pattern

by Kevin Cowtan, <http://www.yybl.york.ac.uk/~cowtan>

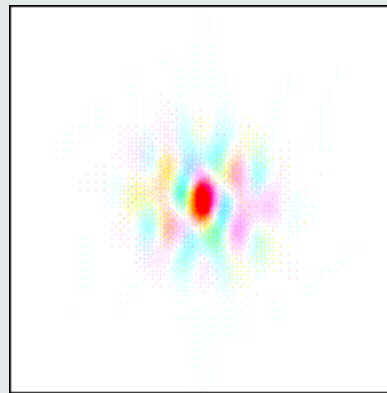
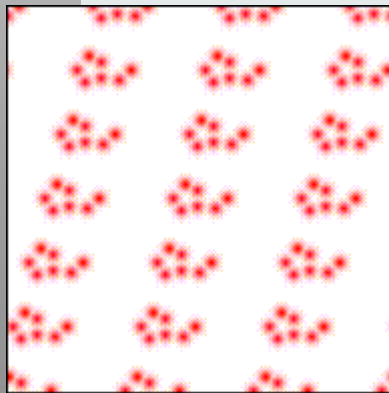
Lattice, and its FT:



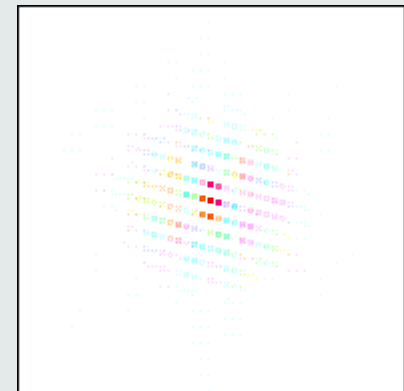
Crystal



1 Molecule FT:



*FT of the crystal =
Product of molecule FT
and Rec. Latt. FT*



Duck Fourier Transform

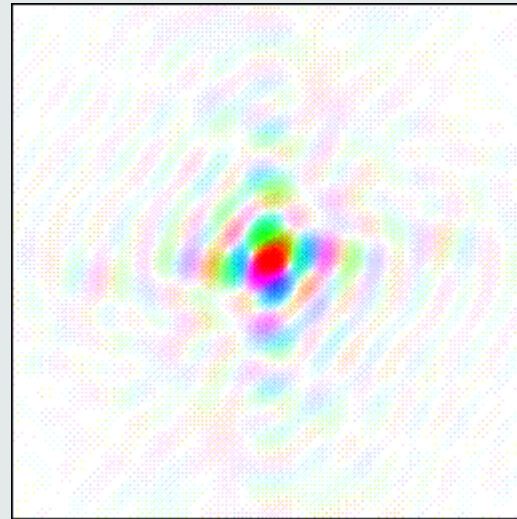
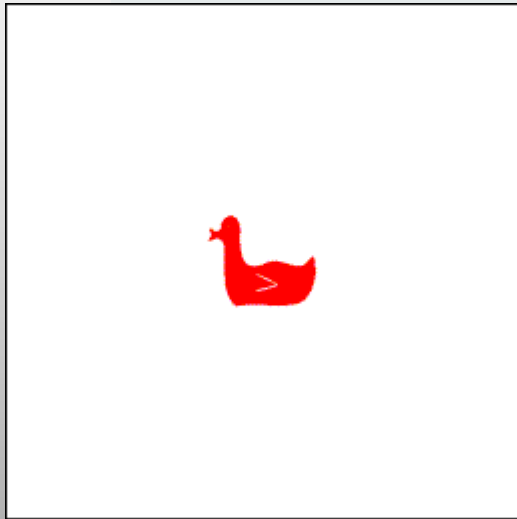
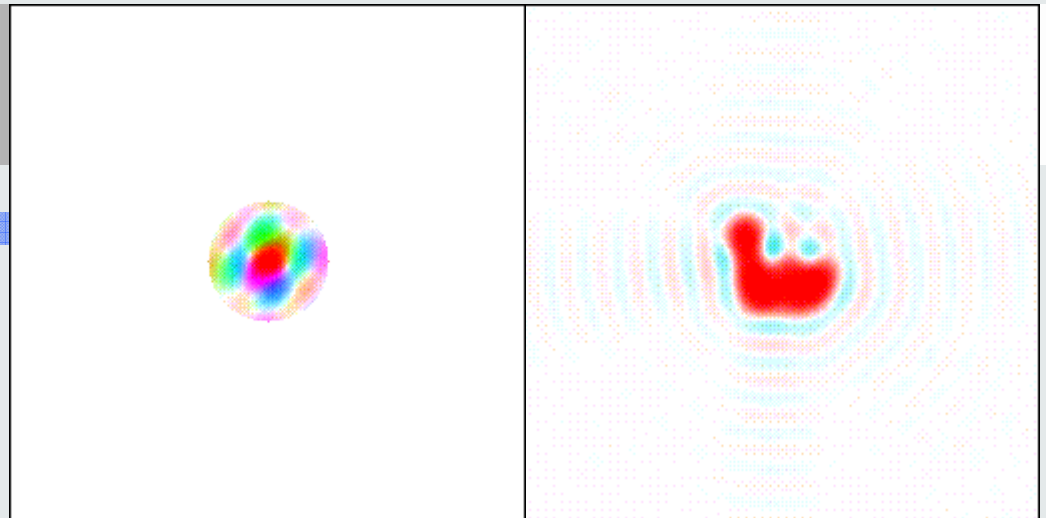


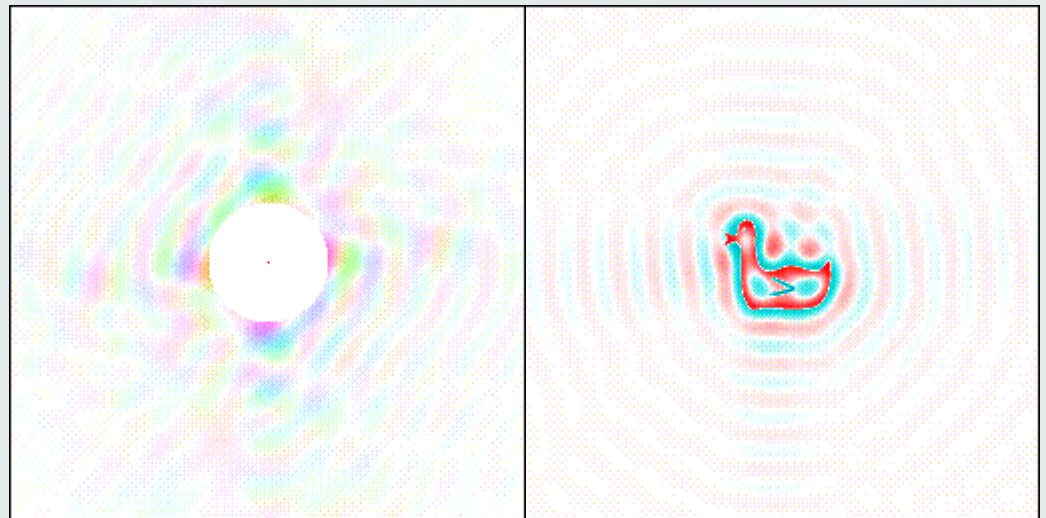
Image is real but its FT is complex (hermitian) !!

by Kevin Cowtan, <http://www.yesbl.york.ac.uk/~cowtan>

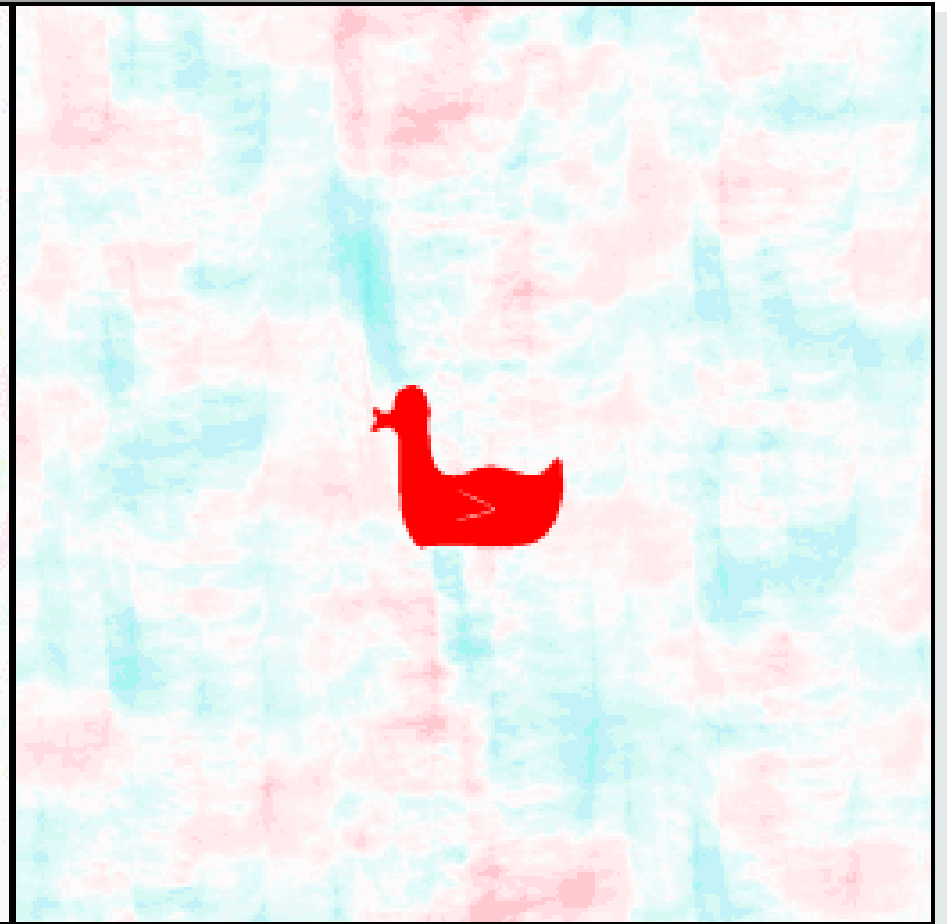
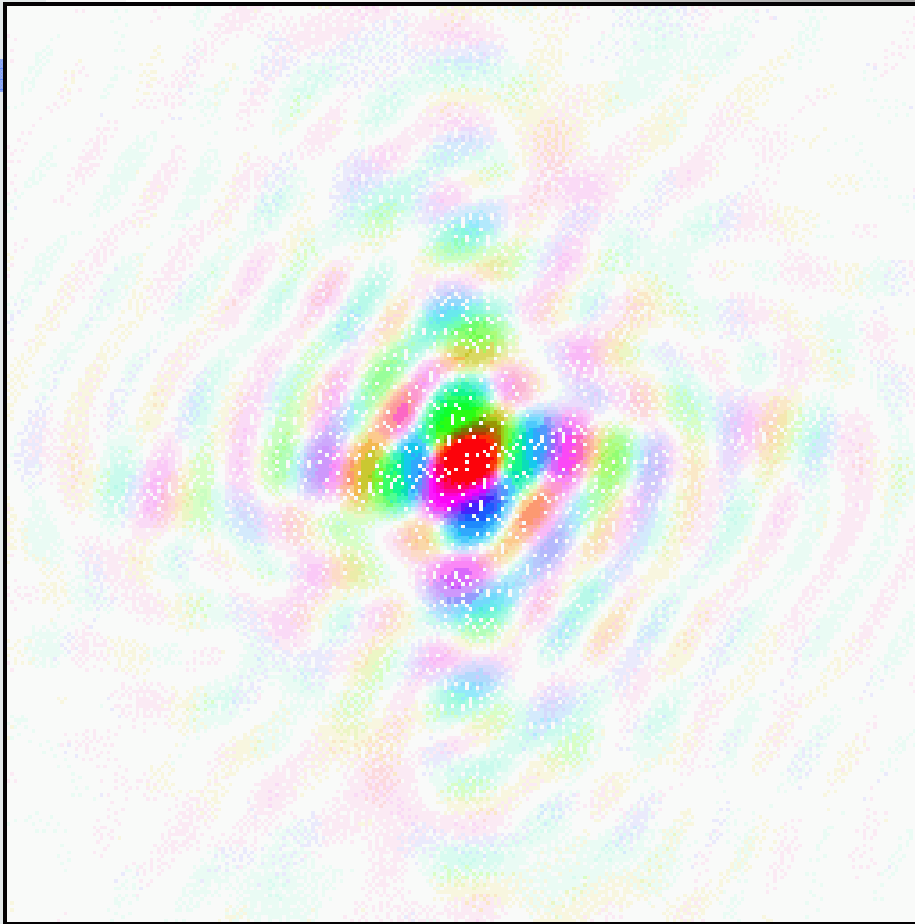
Low resolution Duck

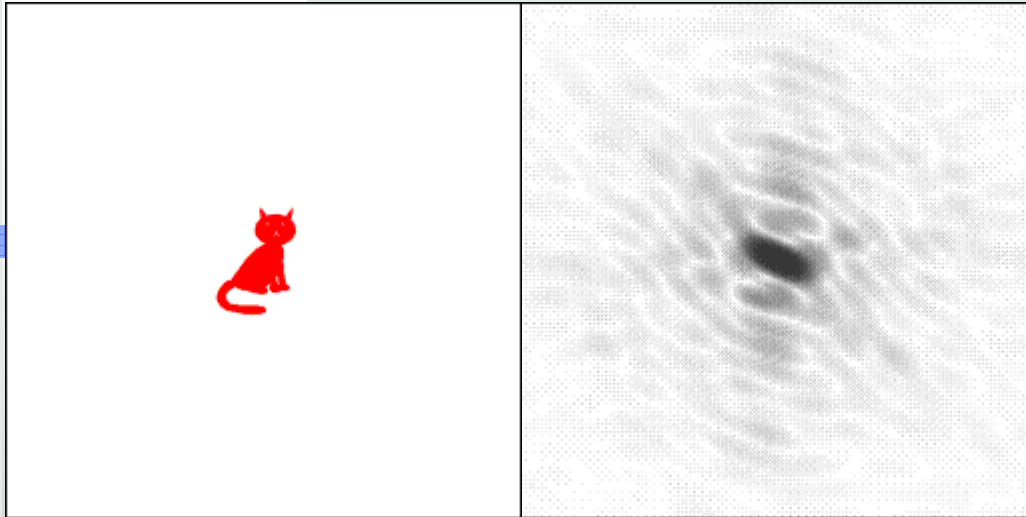


High resolution Duck

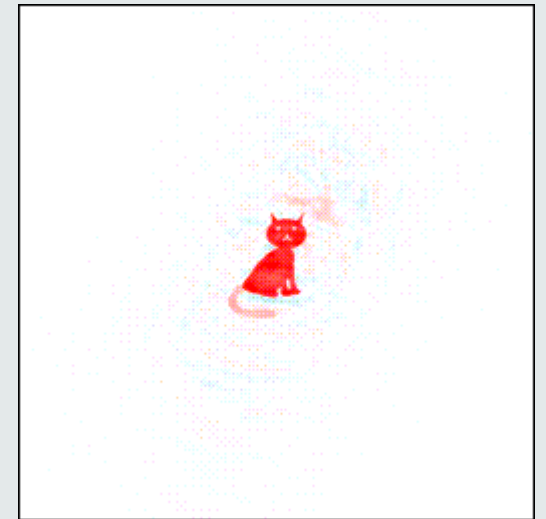


Random Missing of 10% data

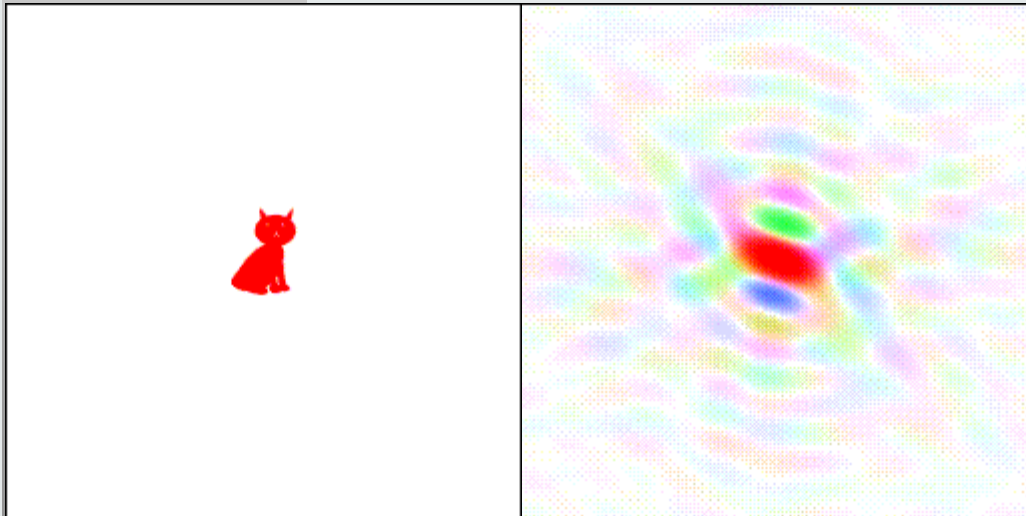




experiment



similar cat



Iteration

REFINEMENT OF A MODEL

Experiment: n_{obs} ; $F_i^{\text{obs}}(q)$, $\sigma_i(q)$

Model $\rho_s(r)$, m_{par}

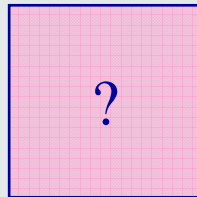
$$\chi^2 = \sum (F_i^{\text{obs}} - F_i^{\text{calc}})^2 / \sum \sigma_i^2 (n_{\text{obs}} - m_{\text{par}})$$

where $F_i^{\text{calc}} = \int \rho_s(r) e^{-iqr}$

- **Spherical approximation** $\rho_s = \sum p_j \rho_j(r)$
- **Multipoles approximation** $\rho_s = \sum p_{lm} R_l Y_{lm}$
- **Wave function approximation** $\rho_s = \sum p_{lm} \psi_{lm}$

GLOBAL OPTIMISATION ALGORITHM

Possible Moment Distributions in the unit cell containing
 $4 (\pm 1) \mu_B$



Consider everything. Keep good.
Avoid evil whenever you recognize it. (St. Paul)

GLOBAL OPTIMISATION

1	1
1	1

2	0
1	1

2	0
2	0

3	0
1	0

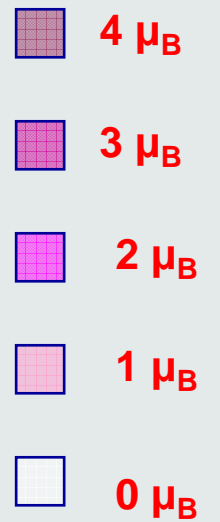
4	0
0	0

2	1
0	1

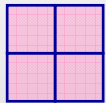
3	1
0	0

2	1
1	0

3	0
0	1



GLOBAL OPTIMISATION



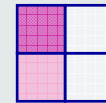
1



12



4



12



4

 4 μ_B

 3 μ_B

 2 μ_B

 1 μ_B

 0 μ_B

33

4	0
0	0

SPIN DISTRIBUTION

$M_{\text{tot}}=4$

EXPERIMENT GIVES

\Rightarrow

3(1)

	1(1)
--	------

EXPERIMENT GIVES

=>

4(1)

	1(1)

$\chi^2 = 5$

1	1
1	1

$\chi^2 = 4$

2	0
1	1

$\chi^2 = 5$

2	0
2	0

$\chi^2 = 2$

3	0
1	0

$\chi^2 = 1$

4	0
0	0

$\chi^2 = 4$

$\chi^2 = 5$

$\chi^2 = 1$

$\chi^2 = 1$

χ^2 VERSUS GO and MEM

3(1)	0(1)
0(1)	0(1)

- χ^2 (ref.)

no solution

- Gl. Opt.

3 maps

- MEM

1 map

4	0
0	0

$\chi^2 = 1$

3	0
1	0

$\chi^2 = 1$

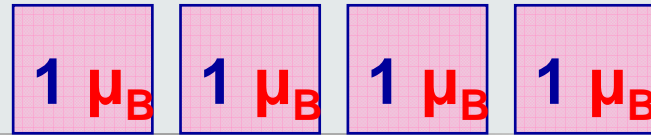
4	0
0	0

$\chi^2 = 1$

3	
	1

$\chi^2 = 1$

3	
	1



MEM

- 4 moments of $1 \mu_B$ in 4 cells
- N moments of $1 \mu_B$ in M cells

- Number of way to get a map

$$g = \frac{N!}{\prod_1^M n_j!}$$

4	0
0	0

- Entropy of the map

$$S = \ln g \approx -N \sum_1^M f_j \ln f_j$$

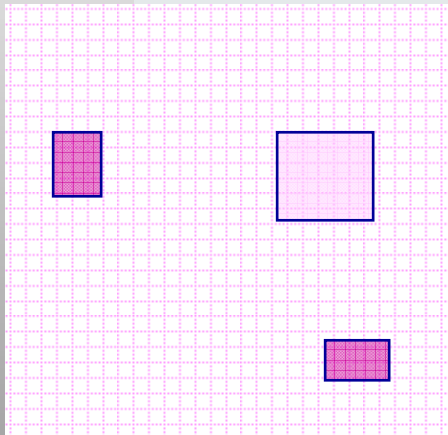
3	0
1	0

- Refinement on

$$\chi^2 - \ln g$$

GLOBAL OPTIMISATION ALGORITHM

Possible Moment Distributions in the unit cell containing
 $3.95 (\pm 0.5) \mu_B$



$20 \times 20 = 400$ cells
of $0.01 \mu_B$

$> N!$ maps

□

$> 400!$

MEM SOLUTION

For given $F_M(q) \Rightarrow$ MEM chose an IMAGE ρ_s that is minimally changed from a default image (prior distribution) as to achieve desired χ^2

For given $F_M(q) \Rightarrow$ MEM chose a most featureless map that allows to achieve desired χ^2

MEM SOLUTION

MEM has acquired a certain “cult” popularity; one sometimes hears that it gives an intrinsically “better” estimate than other methods. Don’ t believe it. MEM has the very cute property of being able to fit sharp features, but there is nothing else magical about it.
(Num. Recipes)

NOUVELLES APPROCHES DANS LA DIFFRACTION DE NEUTRONS POLARISES

A. GUKASOV

Laboratoire Léon Brillouin, CEA-CNRS, Saclay, France

RESUME

*Dans l'état paramagnétique les moments d'atomes équivalents sont égaux,
mais sous champ magnétique **certains sont plus égaux que d'autres***

POLARIZED NEUTRON APPLICATIONS

- **Localization of magnetic density (position and magnitude)**
- **Space distribution of magnetic moment (formfactor, L / S ratio)**
- **Magnetic structure refinement**
- **Site magnetization and susceptibility**

COLLINEAR DENSITIES IN PND

- Covalency in antiferromagnetic garnet $\text{Ca}_3\text{Fe}_2\text{Ge}_3\text{O}_{12}$
- Hybridization in ruthenates $\text{Sr}(\text{Ca})_2\text{RuO}_4$
- Photo-induced spin density of the $[\text{Fe}(\text{ptz})_6](\text{BF}_4)_2$ (ptz=1-propyltetrazole)
- Field-induced ferro-metallic state in $\text{La}(\text{Pr})_{1.2}\text{Sr}_{1.8}\text{Mn}_2\text{O}_7$

NONCOLLINEAR MAGNETIZATION IN PND

- **Non-collinear spin distribution in ferr(o)imagnets**
- **Site susceptibility tensors and Anisotropic Susceptibility Parameters (ASPs)**

NEUTRON AND X-RAYS DIFFRACTION

$$I(q) \propto |F(q)|^2$$

$$F_n(q) = b_N + b_M + b_{SO} + \dots$$

- Nuclear interaction

- X-rays

$$F_N \propto b_N$$

$$b_X \propto r_0 Z f(q)$$

$$(-3.7 \text{ Fm} < b_N < 12.6 \text{ Fm})$$

$$r_0 = 2.8 \text{ Fm}$$

$$\text{Fm} = 10^{-13} \text{ cm}$$

$$\text{Hydrogen, } Z=1 \quad b_X = 2.8 \text{ Fm}$$

X- RAYS AND MAGNETIC NEUTRON DIFFRACTION

- X-rays

$$b_X \propto r_0 Z f(q)$$

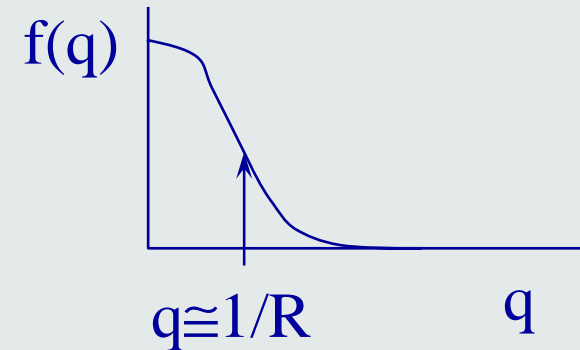
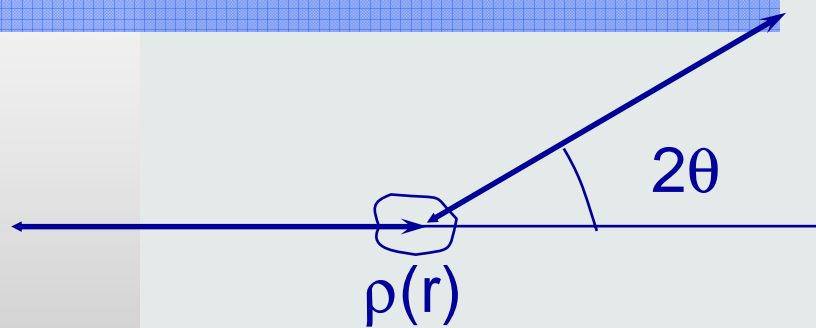
$$r_0 = 2.8 \text{ Fm}$$

- Magnetic interaction

$$F_M \propto (\gamma r_0 / 2) (\mathbf{S}_\perp \cdot \boldsymbol{\sigma}) f(q)$$

$$b_M = \pm 2.7 \text{ Fm for } S=1/2$$

FORMFACTOR AND ORBITAL/SPIN RATIO



$$f_X(q) = \int \rho(r) \exp(iqr) dr^3 / Z$$

$$f_m(q) = \int m(r) \exp(iqr) dr^3 / m$$

$$f_m(q) = \langle J_0 \rangle + (L/L+S) \langle J_2 \rangle + \dots$$

$\langle J_0 \rangle$ are radial integrals

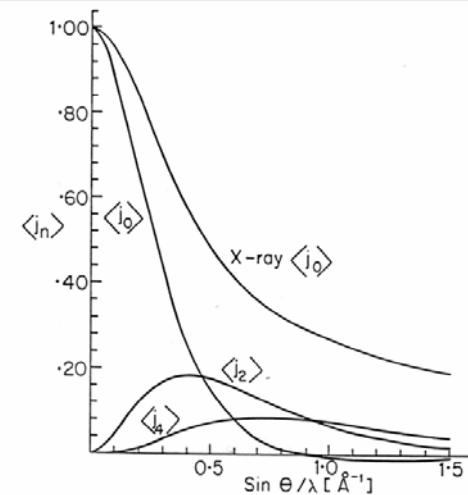
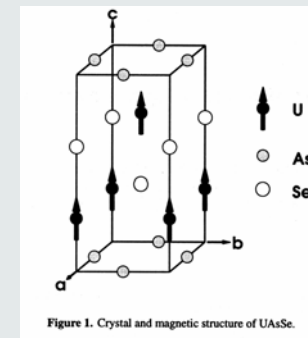
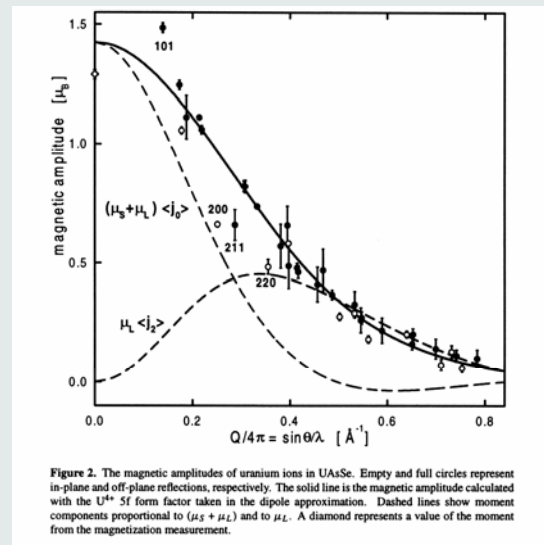


Fig. 2—The radial integrals $\langle J_0 \rangle$, $\langle J_2 \rangle$ and $\langle J_4 \rangle$ for the 3d electrons of an Fe^{2+} free ion. Also shown is the X-ray form factor to which all electrons contribute.

MAGNETIC FORMFACTOR AND ORBITAL/SPIN RATIO

- Polarized neutron diffraction study of spin and orbital moments in UAsSe



P. Wisniewski, A. G. Gukasov and Z. Henkie J. of Phys.: Condens. Matt. 11, 6311, 1999

UNPOLARIZED NEUTRON DIFFRACTION

$$I \propto |F_N|^2 + |F_M|^2$$

- Coherent scattering

$$I(q) \propto |\sum F_i|^2$$

- Nuclear interaction

$$F_N \propto b_N$$

- Incoherent scattering

$$I(q) \propto \sum |F_i|^2$$

- Magnetic interaction

$$F_M \propto (\gamma r_0 / 2) \mathbf{S}_\perp \cdot \sigma_n f(q)$$

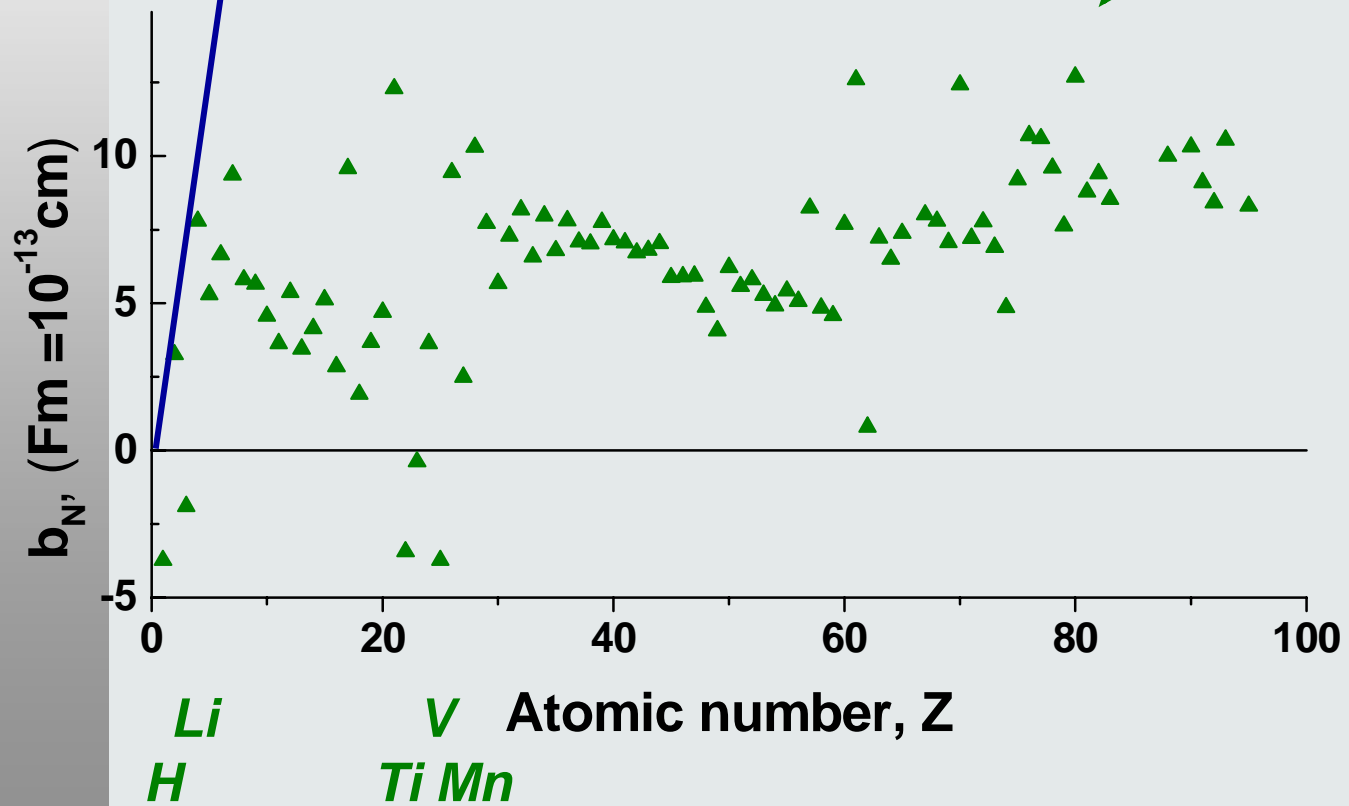
NEUTRON AND X-RAYS DIFFRACTION

X-rays

$\rightarrow r_0 Z f(\theta=0)$

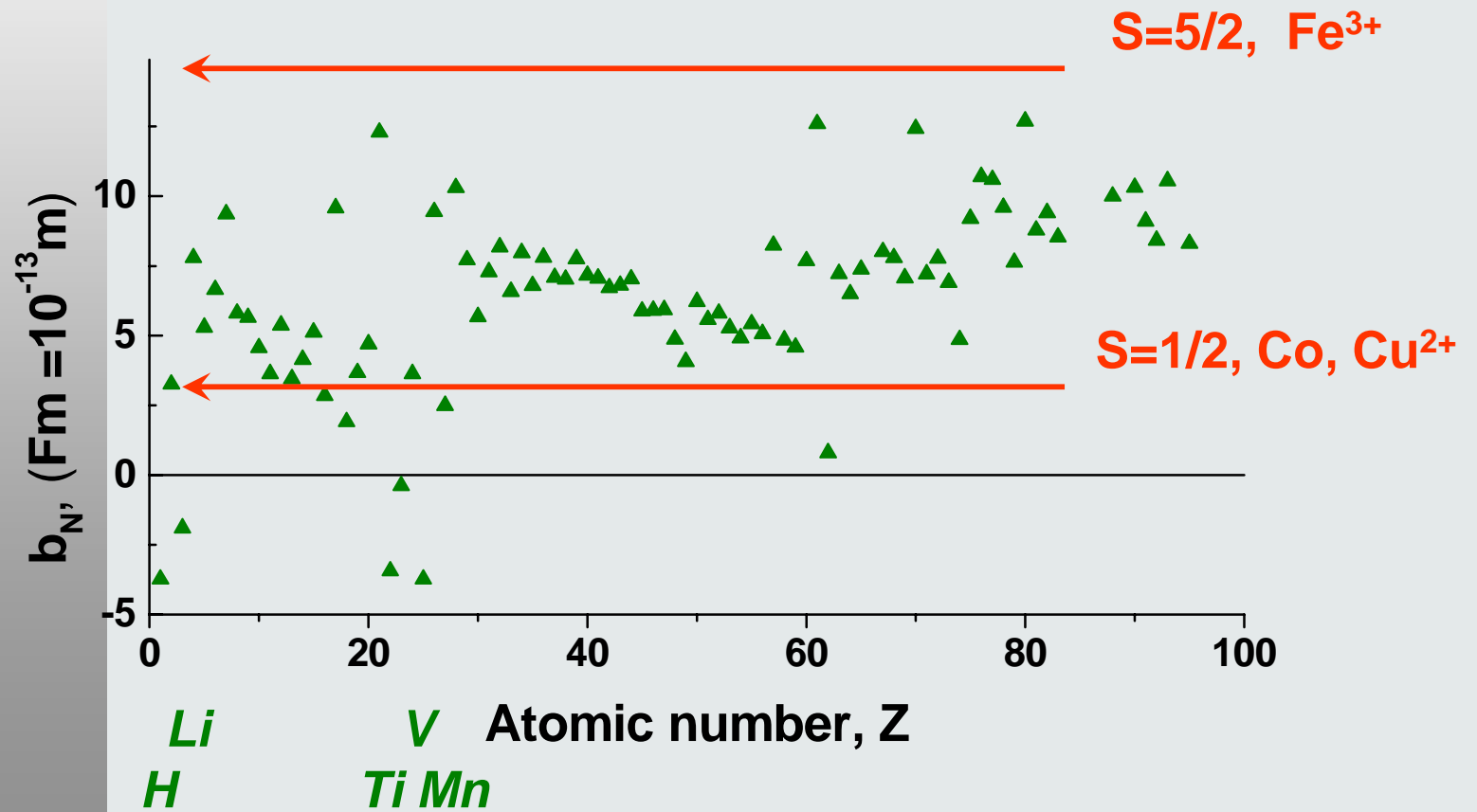
Neutrons

$b_{nuclear}$

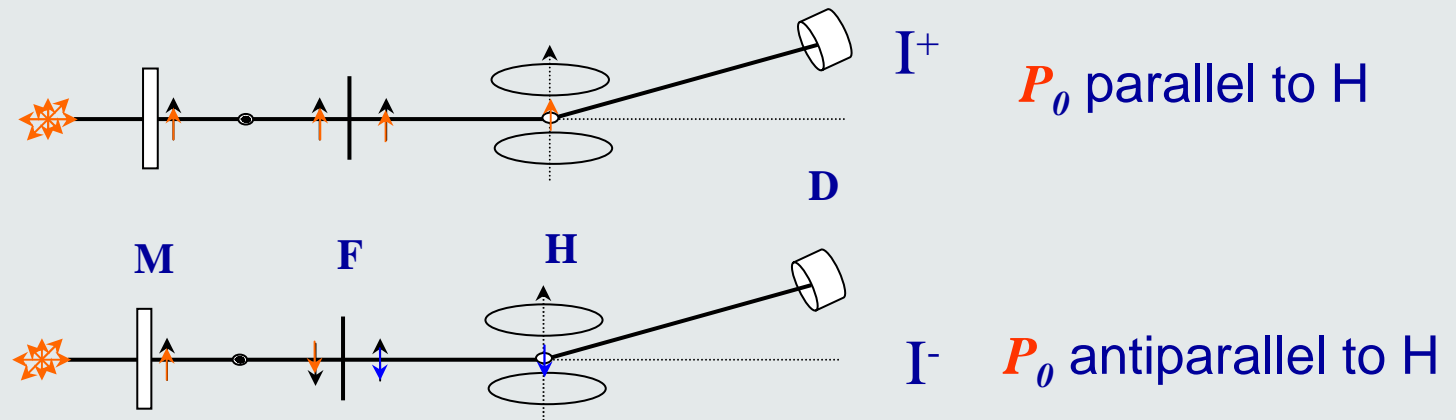


$J=10 \text{ Ho}^{3+}$

NUCLEAR AND MAGNETIC SCATTERING AMPLITUDES



POLARIZED NEUTRON DIFFRACTION



$$I^{\pm} \propto (F_N \pm F_M)^2$$

$$I^{\pm} \propto F_N^2 \pm 2F_N(P_0 * F_M) + F_M^2 \quad (P_0=1)$$

$$\text{If } F_N = F_M \quad I^+ = 4F_N^2 \quad \Gamma = 0$$

$$\text{if } P_0=0 \quad I \propto F_N^2 + F_M^2 = 2F_N^2$$

FLIPPING RATIO MEASUREMENTS

$$I^+ \propto (F_N + F_M)^2 \quad I^- \propto (F_N - F_M)^2$$

$$R = I^+ / I^- = (F_N + F_M)^2 / (F_N - F_M)^2$$

$$R = (1 + \gamma)^2 / (1 - \gamma)^2, \quad \text{where } \gamma = F_M / F_N$$

for small γ $R \cong 1 + 4\gamma$ $\gamma = (1 - R) / 4$

$$F_M(\mathbf{q}) = \gamma * F_N(\mathbf{q})$$

ADVANTAGES OF FLIPPING RATIO MEASUREMENTS

Polarized neutrons:

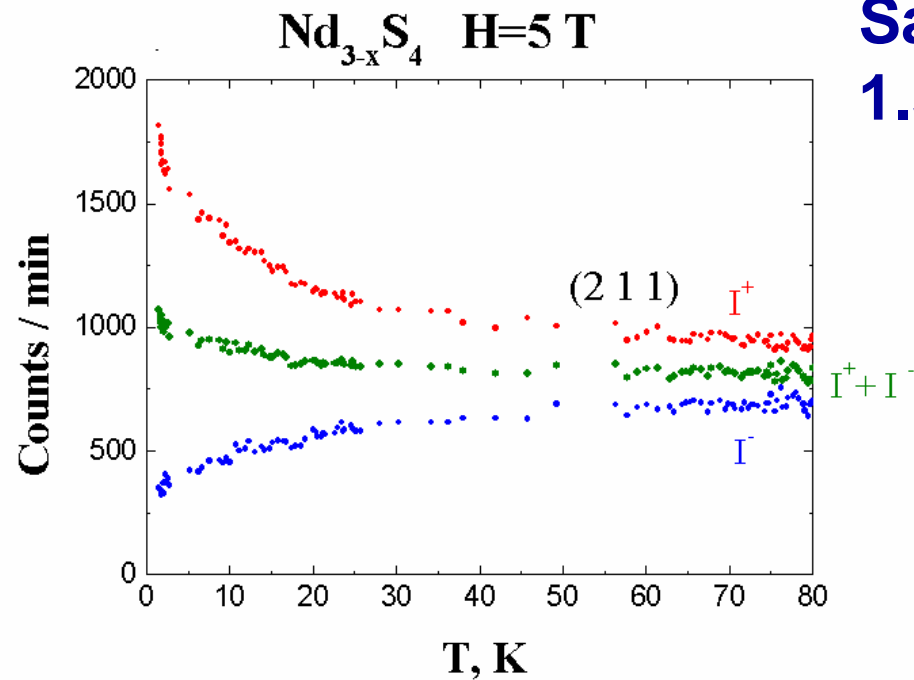
$$I^+ = F_N^2 (1 + \gamma)^2 = (1 + 2\gamma + \gamma^2)$$
$$I^- = F_N^2 (1 - \gamma)^2 = (1 - 2\gamma + \gamma^2)$$

for $\gamma = 0.1$ $I^+ = 1.21 * F_N^2$ $I^- = 0.81 * F_N^2$

Unpolarized neutrons:

for $\gamma = 0.1$ $I = F_N^2 (1 + \gamma^2) = 1.01 * F_N^2$

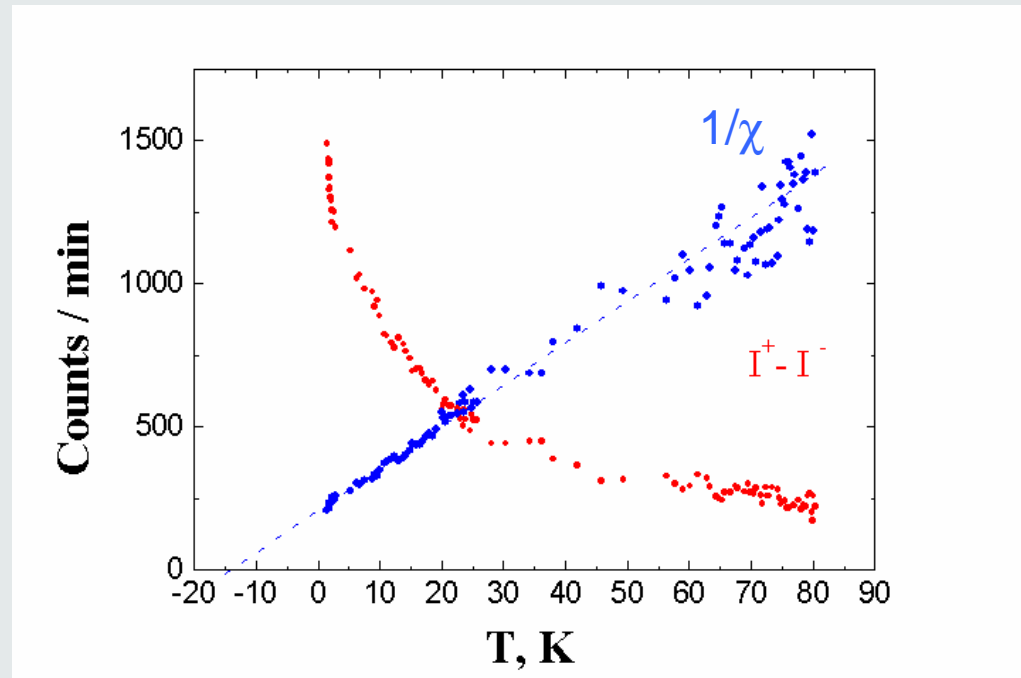
POLARIZED NEUTRONS AND MAGNETIC SUSCEPTIBILITY



Sample size:
 $1.5 \times 1.5 \times 1.5 \text{ mm}^3$

$$I^\pm \propto F_N^2 + |F_M|^2 \pm 2 F_N |F_M|$$

POLARIZED NEUTRONS AND MAGNETIC SUSCEPTIBILITY

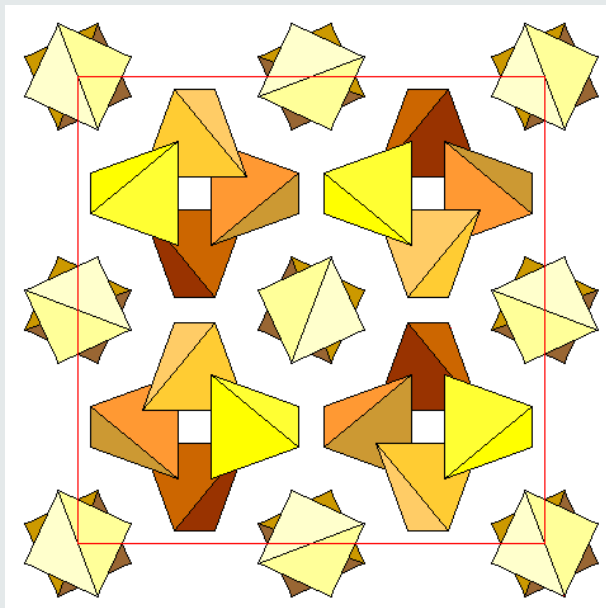


$$I(q)^+ - I(q)^- = 4 N (\mathbf{P}_0 \cdot \mathbf{M}_{\perp z}) \sim P^\alpha \cdot \chi^{\alpha\beta}(q) \cdot H^\beta$$

SPIN DENSITY ON LIGANDS O²⁻ AND COVALENCY OF Fe³⁺ IN Ca₃Fe₂Ge₃O₁₂ GARNET.

V. P. Plakhty, A. G. Gukasov, R. J. Papoular and O. P. Smirnov, *Europhys. Lett.*,
48, 233, 1999

SG 230
Ia3D



24 (d)

tetra

(3/8 0 1/4)

Si, Ge

96 (h)

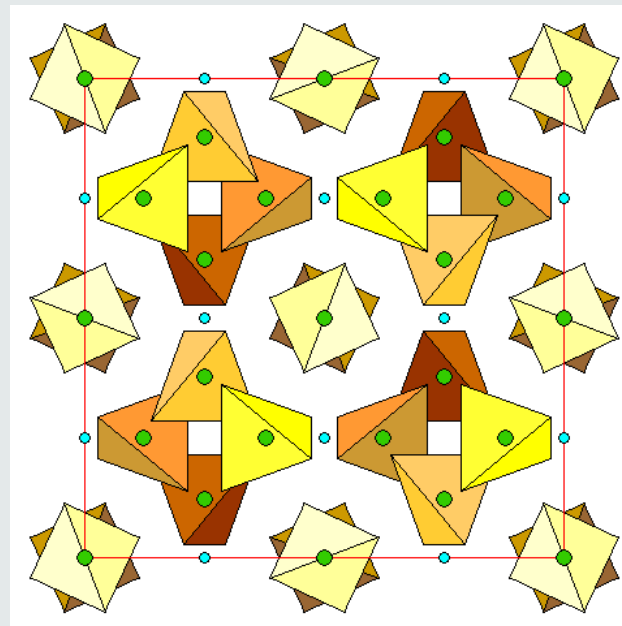
general

(x y z)

O

SPIN DENSITY ON LIGANDS O²⁻ AND COVALENCY OF Fe³⁺ IN Ca₃Fe₂Ge₃O₁₂ GARNET.

SG 230, *Ia3D*



16 (a)

octa

(0 0 0)

M^I

24 (c)

dode

(1/8 0 1/4)

M^{II}

GARNET STRUCTURE

3d $1.25 < R_{ion} < 1.46 \text{ \AA}$

4f $1.75 < R_{ion} < 1.88 \text{ \AA}$

O $R_{ion} = 1.4 \text{ \AA}$,

O²⁻ $R_{ion} = 0.66 \text{ \AA}$

16 (a) octa (0 0 0) **3d, 4f**

24 (c) dode (1/8 0 1/4) **4f, Fe³⁺, Mn²⁺**

24 (d) tetra (3/8 0 1/4) **Fe³⁺**

ALLOWED REFLECTIONS FOR GARNET

I a3d $h+k+l=2n$ (general condition for BCC)

16 (a)

octa

$h,k=2n ; h+k+l=4n$

(0 0 4)

24 (d)

tetra

$h,k=2n+1 ; l=4n+2$

(1 1 2)

24 (c)

dode

$h,k=2n+1 ; l=4n+2$

96 (h)

Oxygen

$h+k+l=2n$

(1 3 4)

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- **Refinement** of multipoles $\rho_s = \sum p_{lm} R_l Y_{lm}$
- **MEM**, maximum entropy method and others...

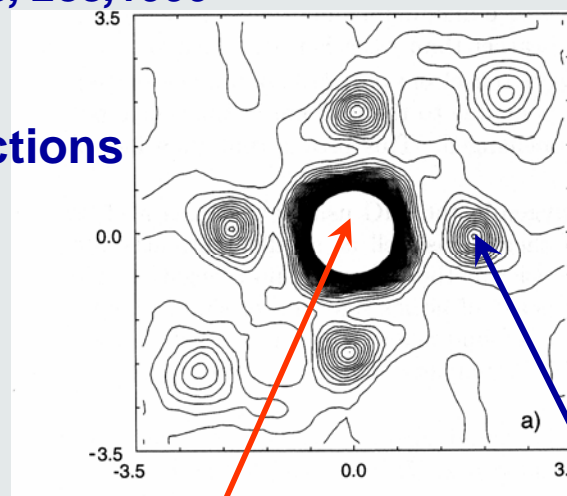
MEM SOLUTION

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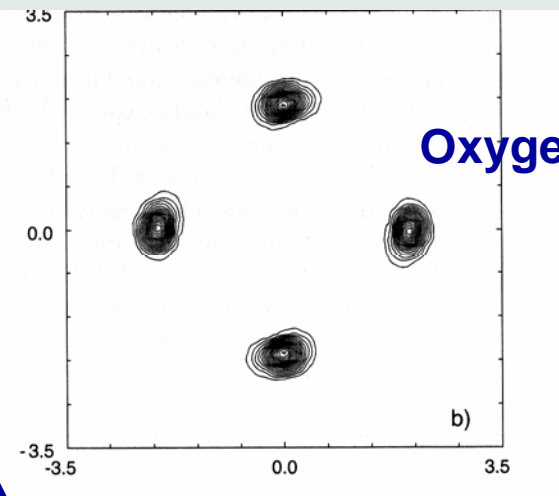
SPIN DENSITY ON LIGANDS O²⁻ AND COVALENCY OF Fe³⁺ IN Ca₃Fe₂Ge₃O₁₂ GARNET.

- V. P. Plakhty, A. G. Gukasov, R. J. Papoular and O. P. Smirnov, *Europhys. Lett.*, 48, 233, 1999

All reflections



Oxygen reflections

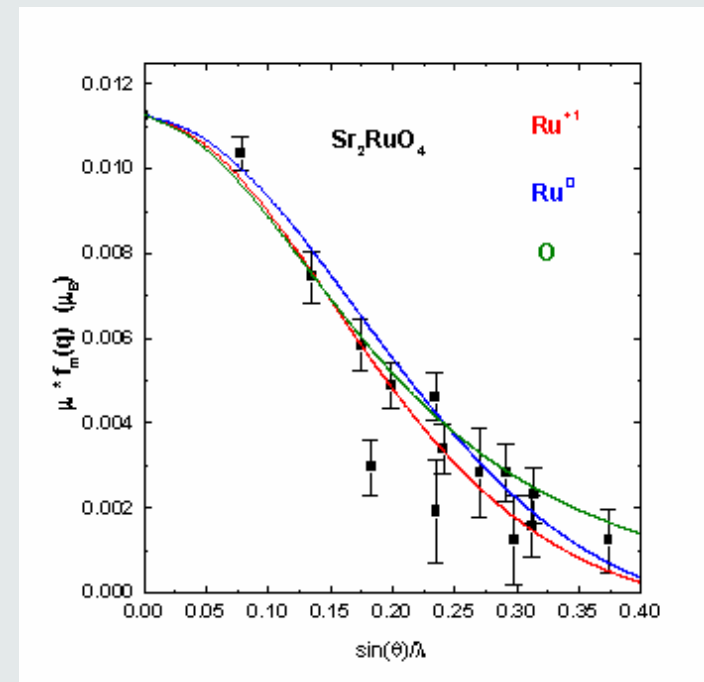
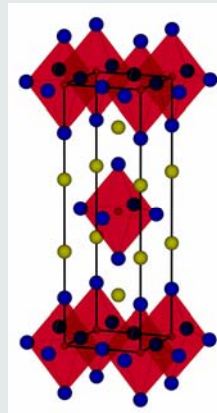


Fe³⁺ 0.59(1)μ_B

O²⁻ 0.015(2)μ_B ≈ 2.5% of Fe

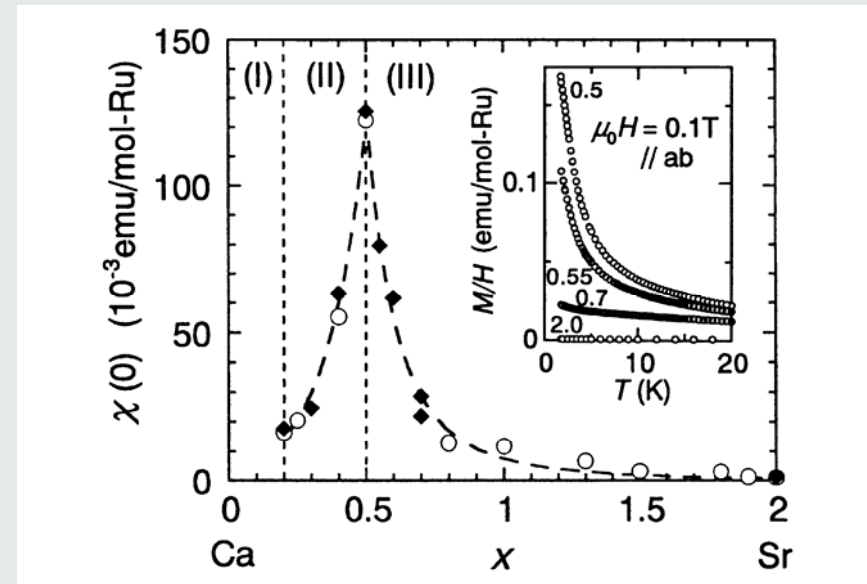
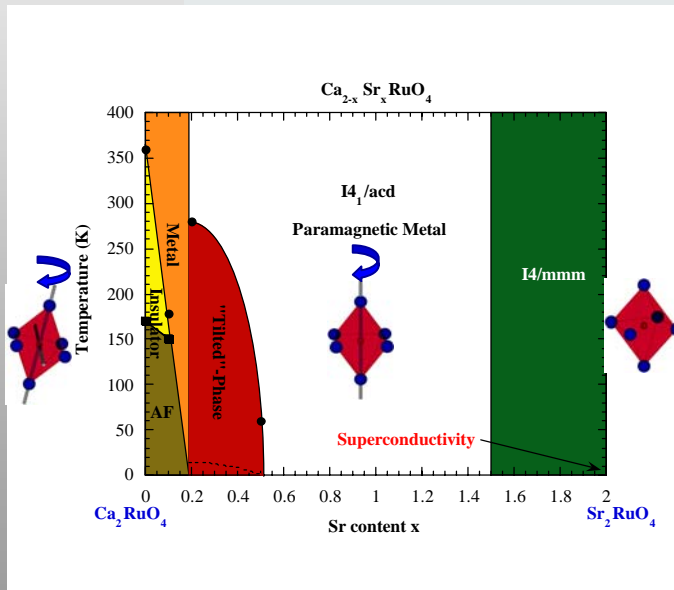
δM/M ≈ 13% for Fe

SPIN DENSITY ON LIGANDS O²⁻ AND FORMFACTOR OF Ru in Sr₂RuO₄

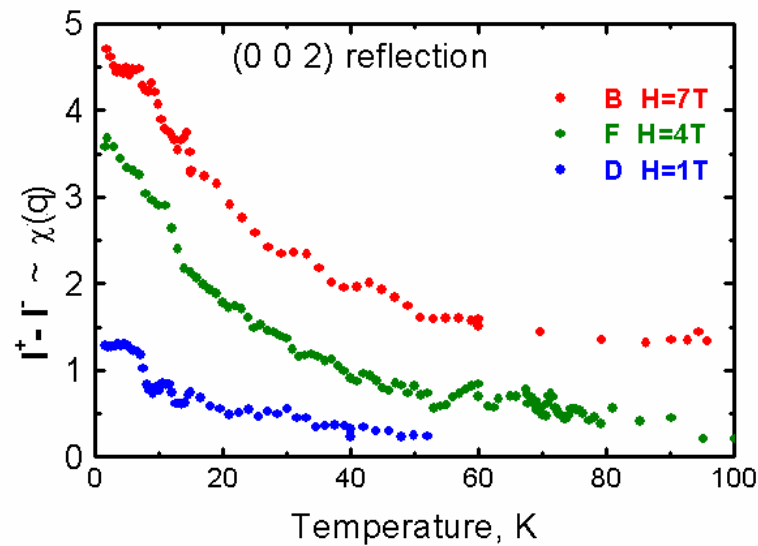


SPIN DENSITY ON LIGANDS O²⁻ IN Ca_{1.5}Sr_{0.5}RuO₄

O. Friedt, M Braden, G. André, P. Adelemann, S Nakatsuji and Y Maeno. *Phys. Rev.*, B63, 174432, 2001



MAGNETIC SUSCEPTIBILITY OF $\text{Ca}_{1.5}\text{Sr}_{0.5}\text{RuO}_4$; POLARIZED NEUTRON MEASUREMENTS



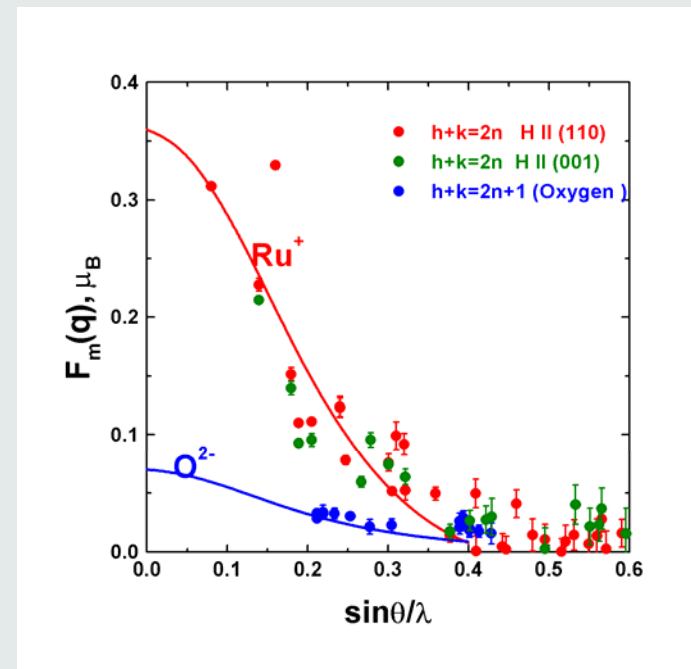
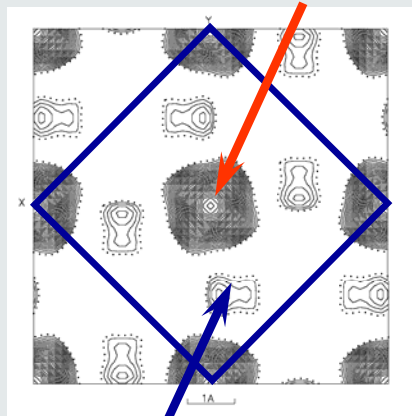
$$I^{\pm} \propto F_N^2 + |F_M|^2 \pm 2 F_N |F_M|$$

$$I(q)^+ - I(q)^- = 4 N \mathbf{M}_{\perp z} \sim \chi^{\alpha\beta}(\mathbf{q}) \cdot \mathbf{H}^{\beta}$$

ANOMALOUS SPIN DENSITY ON OXYGEN IN $\text{Ca}(\text{Sr})_2\text{RuO}_4$

A Gukasov, M Braden, R J Papoular, S Nakatsuji and Y Maeno PRL, 89, 087202-1, 2002

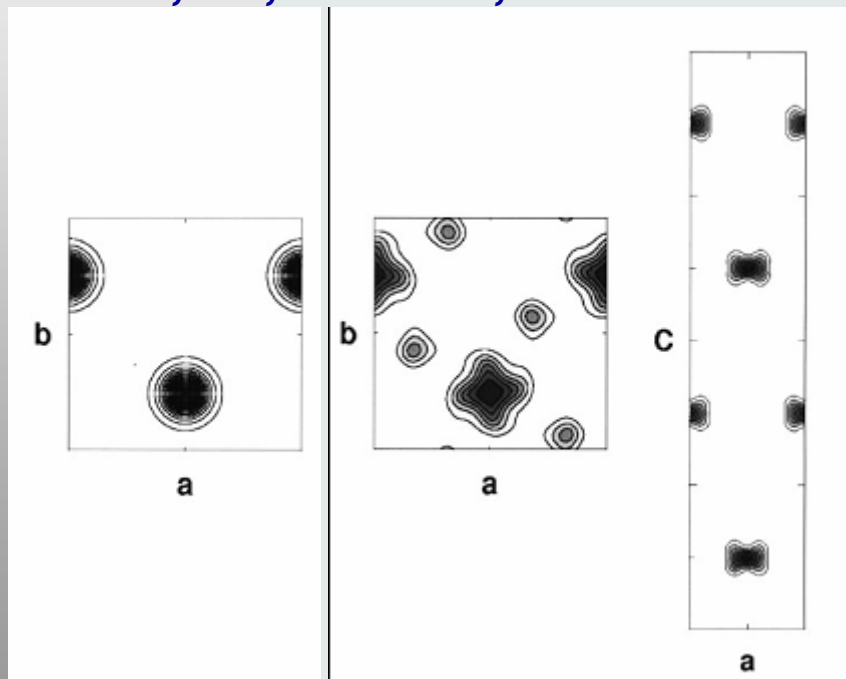
$\text{Ru}^{4+} \ 0.36(1)\mu_B$



$\text{O}^{2-} \ 0.070(2)\mu_B \approx 19\% \text{ of Ru}$

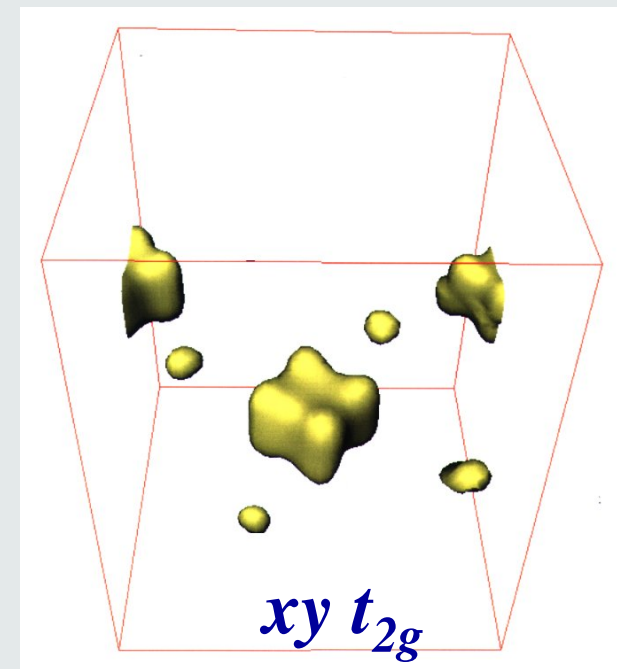
ANOMALOUS SPIN DENSITY ON OXYGEN IN $\text{Ca}(\text{Sr})_2\text{RuO}_4$

A Gukasov, M Braden, R J Papoular, S Nakatsuji and Y Maeno
PRL, 89, 087202-1, 2002



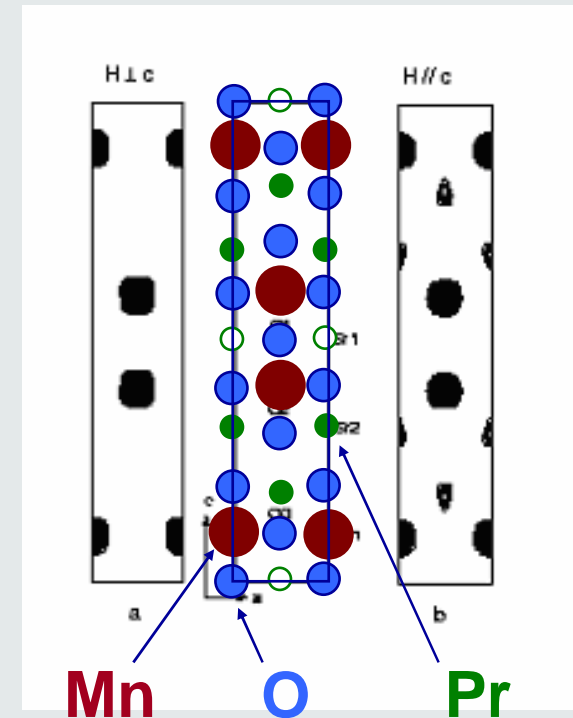
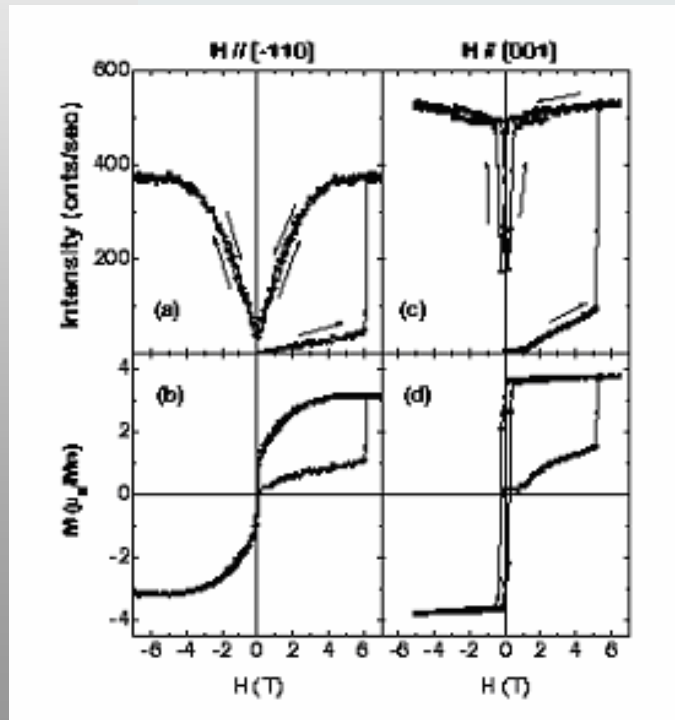
Ru^{4+} $0.36(1)\mu_B$

O^{2-} $0.070(2)\mu_B \approx 19\%$ of Ru

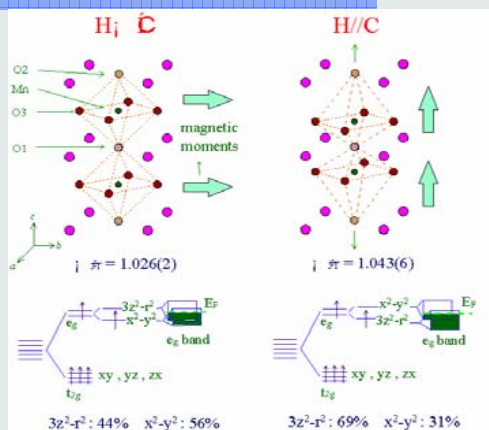


ON THE ORIGIN OF THE FIELD INDUCED METALIC STATE OF DOUBLE LAYERED MANGANITE $\text{La}(\text{Pr})_{1.2}\text{Sr}_{1.8}\text{Mn}_2\text{O}_7$

F. Wang, A. Gukasov, F. Moussa, M. Hennion, M. Apostu, R. Suryanarayanan and A. Revcolevschi., PRL, 2003



MULTIPOLE REFINEMENT FOR TWO FIELD-INDUCED STATES OF $\text{La}(\text{Pr})_{1.2}\text{Sr}_{1.8}\text{Mn}_2\text{O}_7$



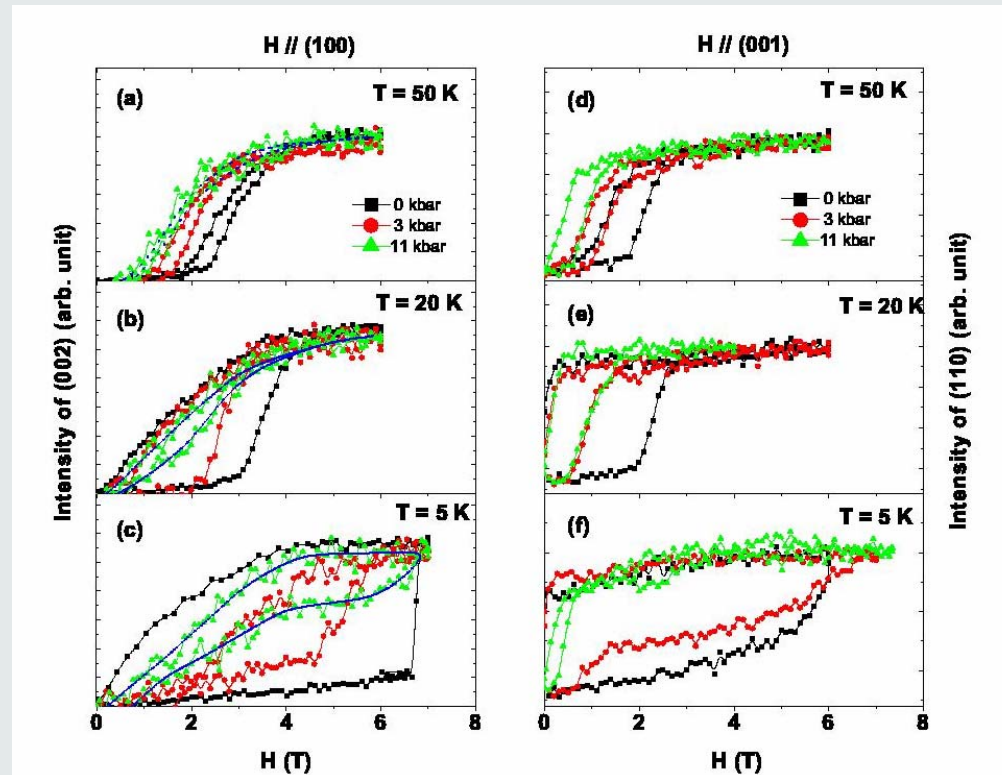
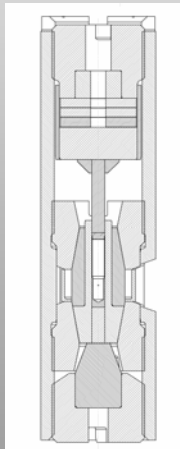
Mn $(\mu_S + \mu_L) = 3.36(3) \mu_B$
Mn $\mu_L = -0.48(4) \mu_B$
Mn $Y_{40} = 0.50(7)$

Pr $(\mu_S + \mu) = 0 \mu_B$
Pr $\mu_L = 0 \mu_B$

Mn $(\mu_S + \mu_L) = 3.12(5) \mu_B$
Mn $\mu_L = -0.58(7) \mu_B$
Mn $Y_{44+} = 0.35(6)$

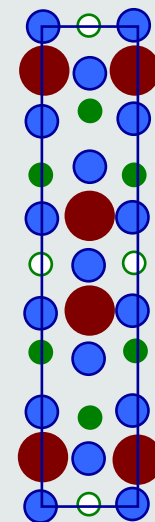
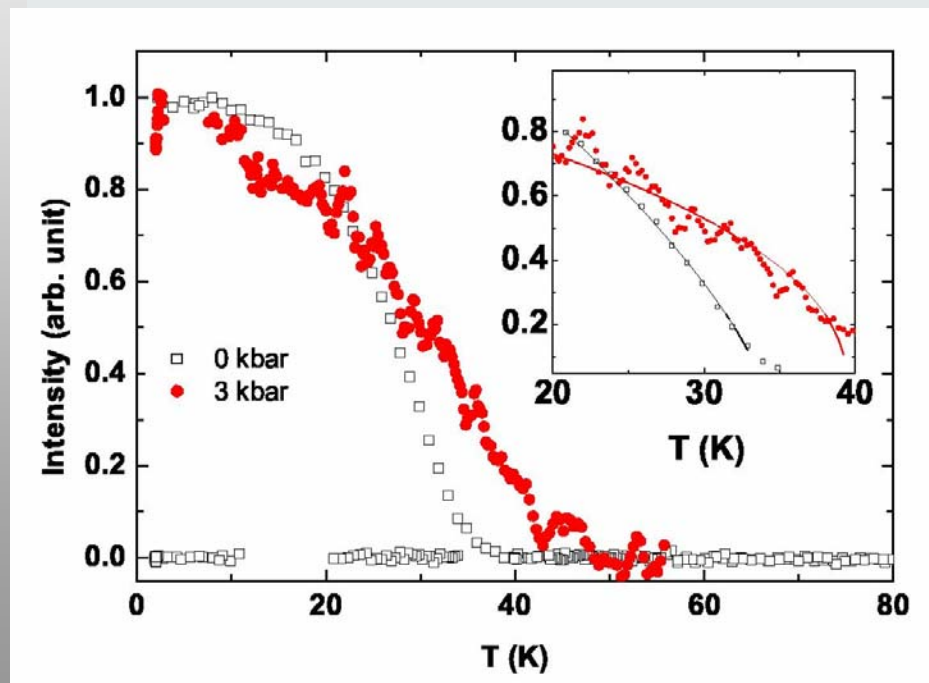
Pr $(\mu_S + \mu) = 0.50(3) \mu_B$
Pr $\mu_L = 0.77(4) \mu_B$

Spin-lattice interplay and pressure effect on the field-induced ferromagnetic metallic transition in $\text{La}(\text{Pr})_{1.2}\text{Sr}_{1.8}\text{Mn}_2\text{O}_7$



Spin-lattice interplay and pressure effect on the field-induced ferromagnetic metallic transition in $\text{La}(\text{Pr})_{1.2}\text{Sr}_{1.8}\text{Mn}_2\text{O}_7$

A. Gukasov, B Anighoefer, F. Wang et al. (in preparation)



SPIN DENSITY, WHAT IS THIS ?

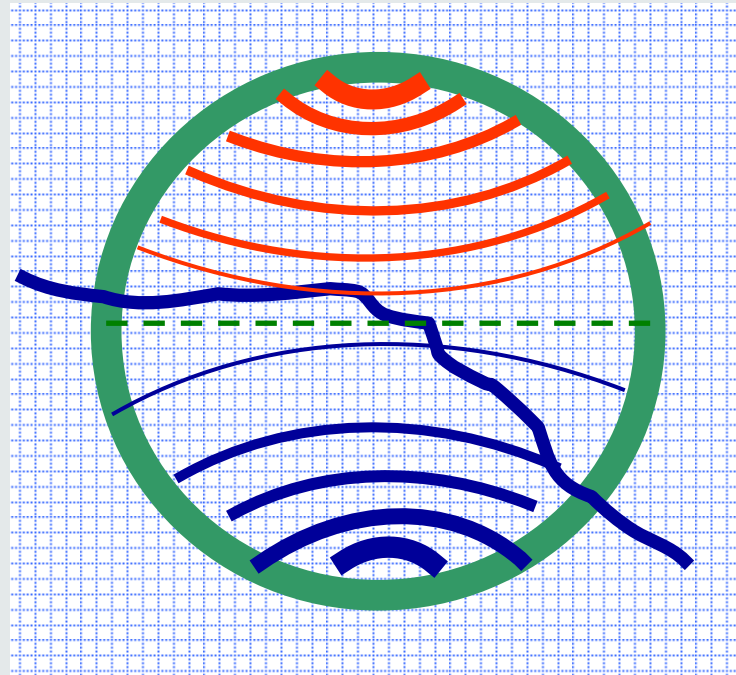
DENSITY OF A PSEUDOVECTOR ?

SPEED DENSITY

DENSITY OF A VECTOR ?

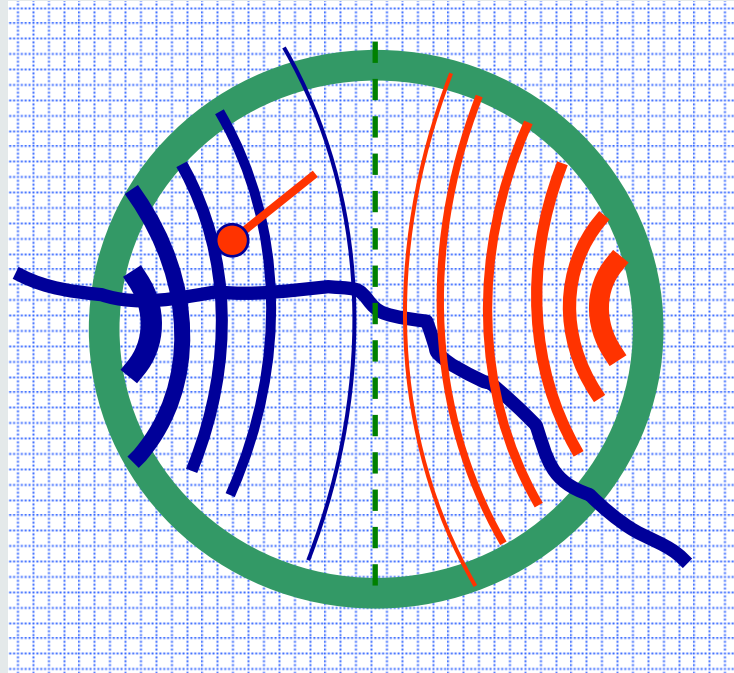
SPEED DENSITY OF CARS IN PARIS

V_N



SPEED DENSITY OF CARS IN PARIS

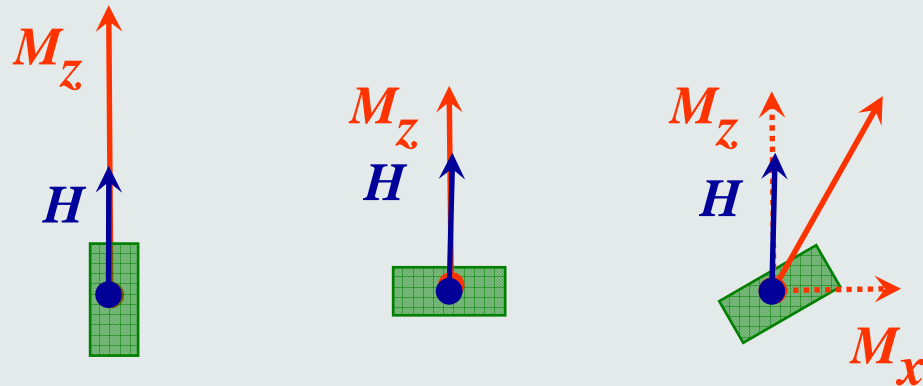
V_E



COLLINEAR AND NON-COLLINEAR SPIN DENSITIES (DISTRIBUTION)

Bulk magnetisation

$$M_i(\mathbf{r}) = \chi_{ij} H_j$$



$$F^{\pm} \propto F_N^2 \pm 2(\underline{P}_0^* \underline{E}_M) F_N + F_M^2$$

$$F^{\pm} \propto F_N^2 \pm 2F_{Mz} F_N + F_M^2$$

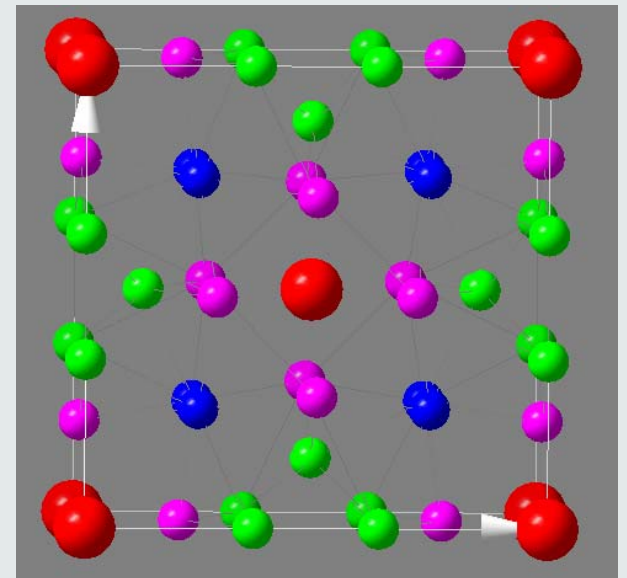
NONCOLLINEAR MAGNETIZATION IN $\text{HoCo}_{10}\text{Ti}_2$

Yuri Janssen, A. Gukasov, E. Brück, K.H.J. Buschow and F.R. de Boer

ThMn₁₂ structure I4/mmm

a=b=8.4 Å, c=4.7 Å

2	(a)	(0 0 0)	Ho	
8	(f)	($\frac{1}{4}$ $\frac{1}{4}$ $\frac{1}{4}$)	Co1	
8	(j)	(0.28 $\frac{1}{2}$ 0)	Co2	
8	(i)	(0.36 0 0)	Co3	0.56(1)
			Ti	0.44(1)

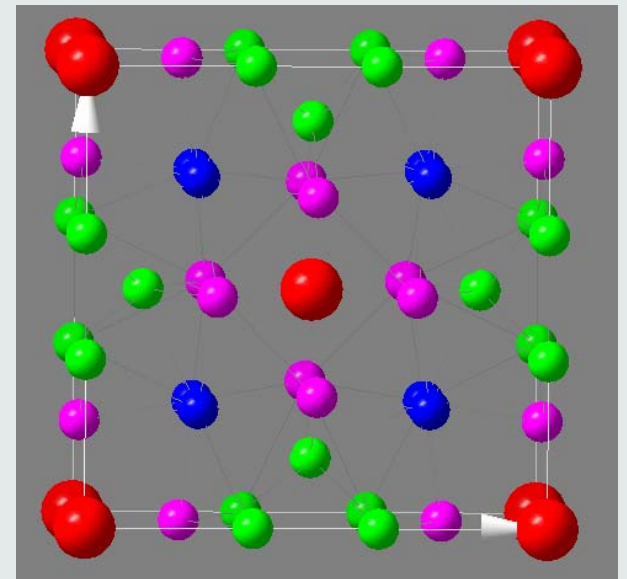
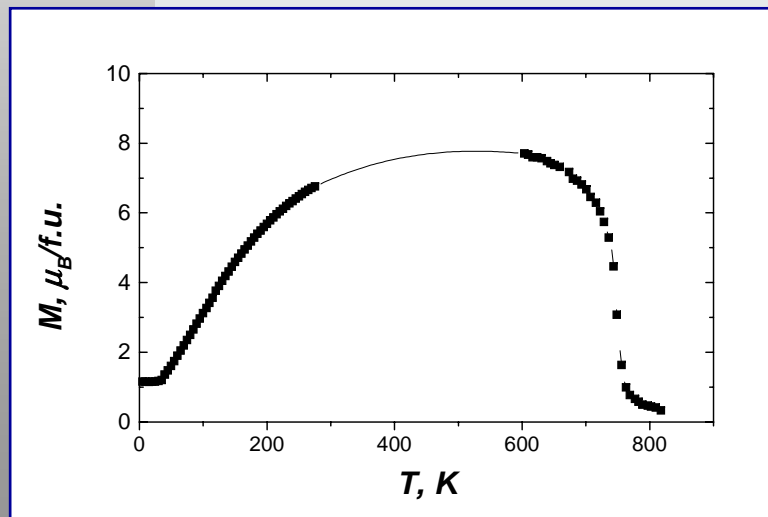


NONCOLLINEAR MAGNETIZATION IN $\text{HoCo}_{10}\text{Ti}_2$

Yuri Janssen, A. Gukasov, E. Brück, K.H.J. Buschow and F.R. de Boer

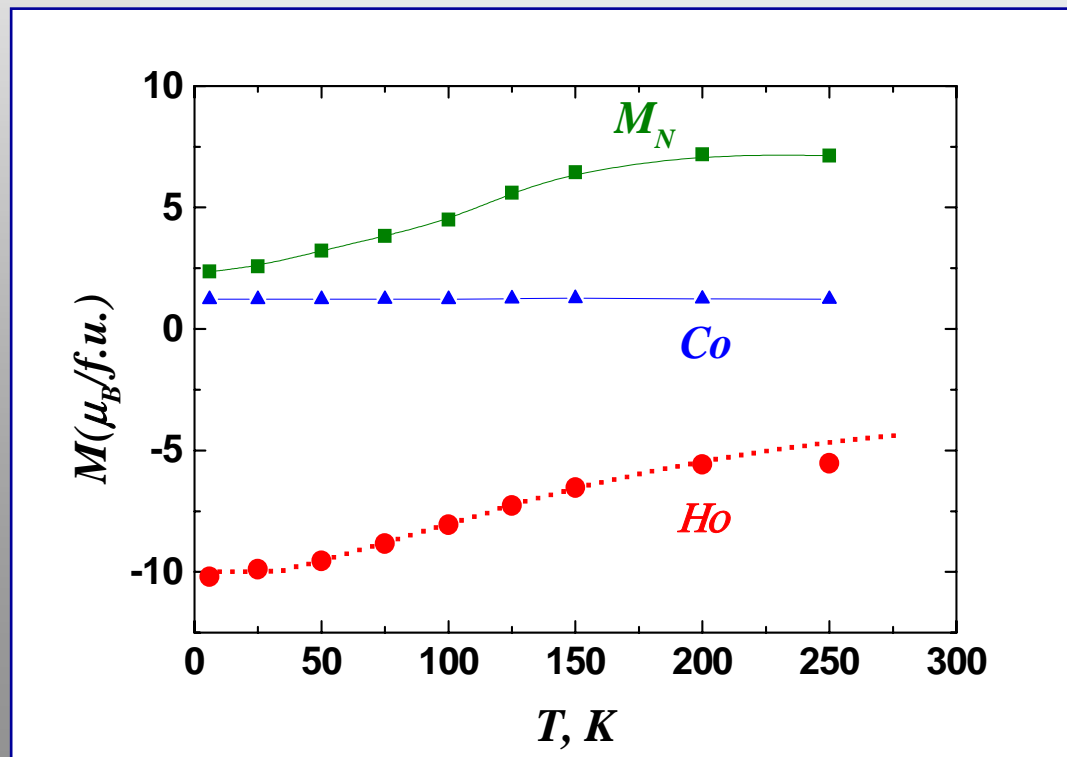
ThMn₁₂ structure I4/mmm

a=b=8.4 Å, c=4.7 Å



HoCo₁₀Ti₂, UNPOLARIZED NEUTRON DIFFRACTION

Single crystal of diameter **1.2 mm !**
6T2, 4-circles LLB, 86 independent reflections per T



Ho 10.0(1) μ_B

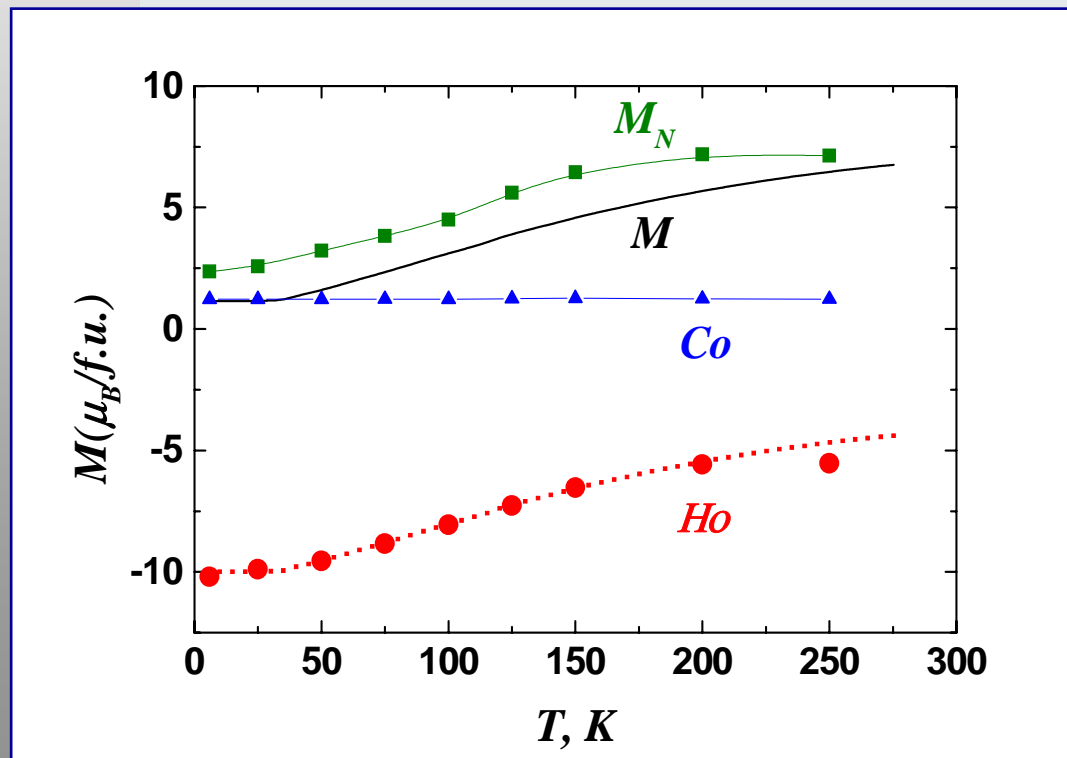
Co1 1.25(3) μ_B

Co2 1.24(3) μ_B

Co3 1.27(3) μ_B

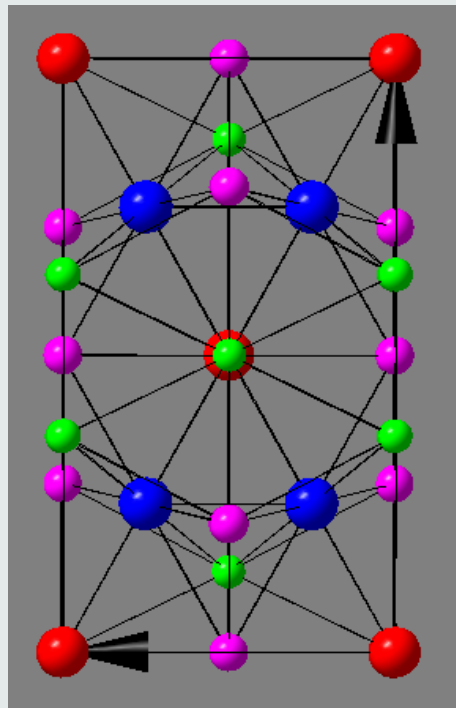
HoCo₁₀Ti₂, UNPOLARIZED NEUTRONS

Single crystal of diameter **1.2 mm !**
6T2, 4-circles LLB, 86 independent reflections per T

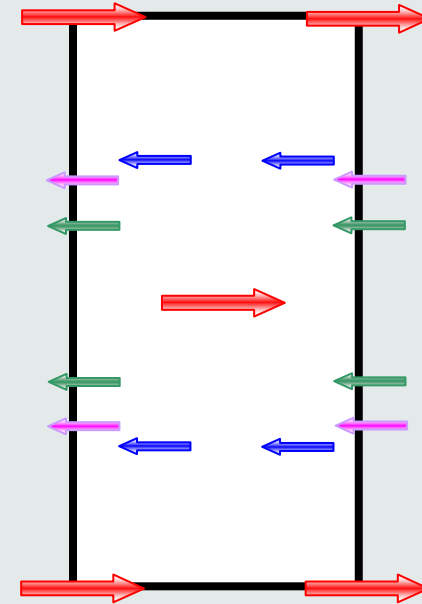


Ho	10.0(1) μ_B
Co1	1.25(3) μ_B
Co2	1.24(3) μ_B
Co3	1.27(3) μ_B
M_N	2.5 μ_B
M	1.2 μ_B

HoCo₁₀Ti₂, UNPOLARIZED NEUTRONS



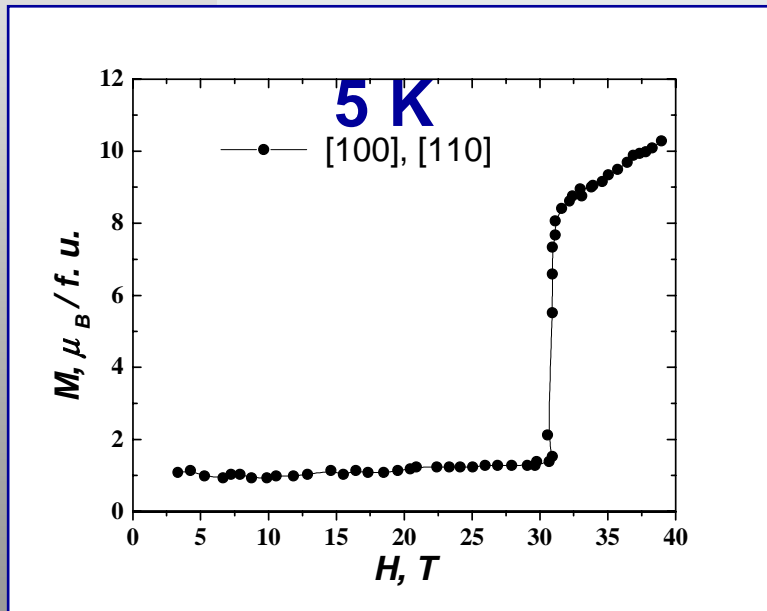
5 K



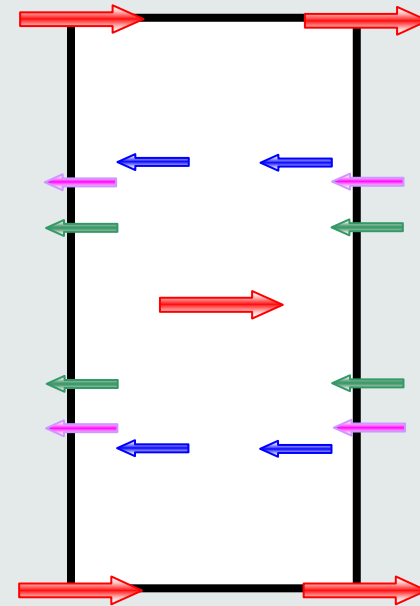
$$M_N = 2.5 \mu_B \quad M = 1.2 \mu_B$$

$$M_{\text{cond}} = 0.13 \mu_B / \text{Co}$$

MAGNETIC ANISOTROPY IN $\text{HoCo}_{10}\text{Ti}_2$

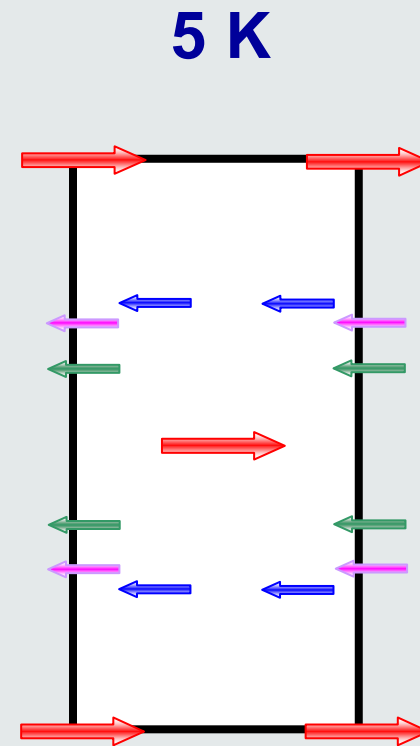
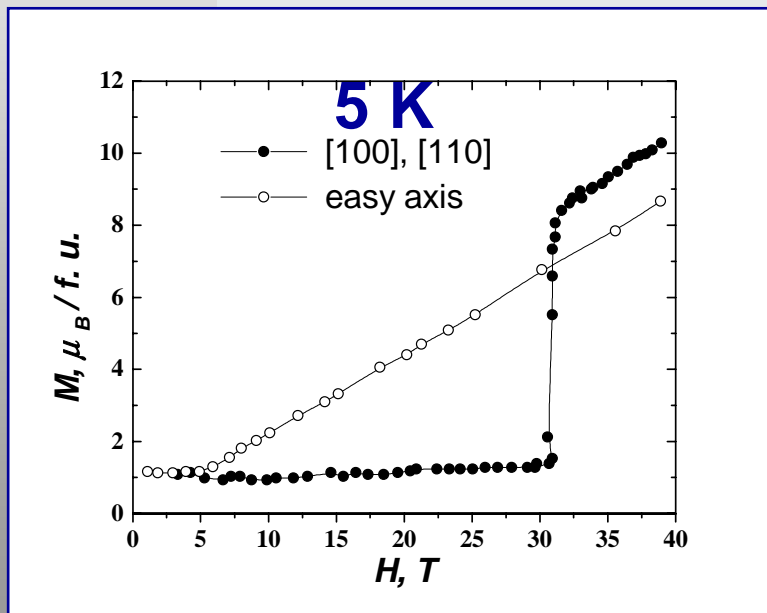


5 K



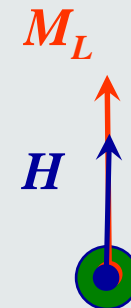
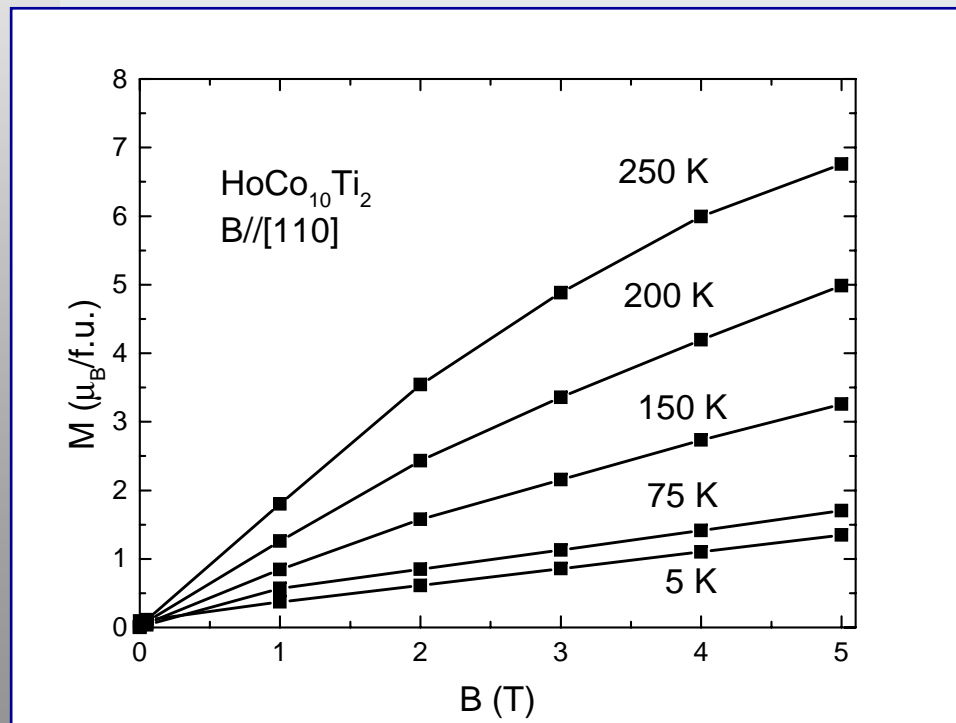
$$M_{\text{TOT}} = 10 \times 1.25 + 10 = 22.5 \mu_B$$

MAGNETIC ANISOTROPY IN $\text{HoCo}_{10}\text{Ti}_2$



$$M_{\text{TOT}} = 10 \times 1.25 + 10 = 22.5 \mu_B$$

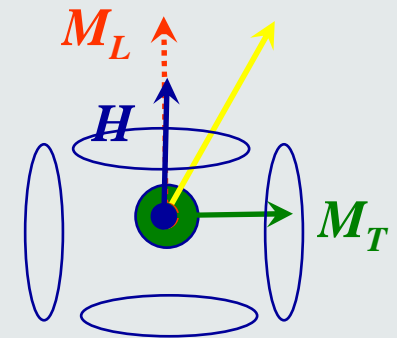
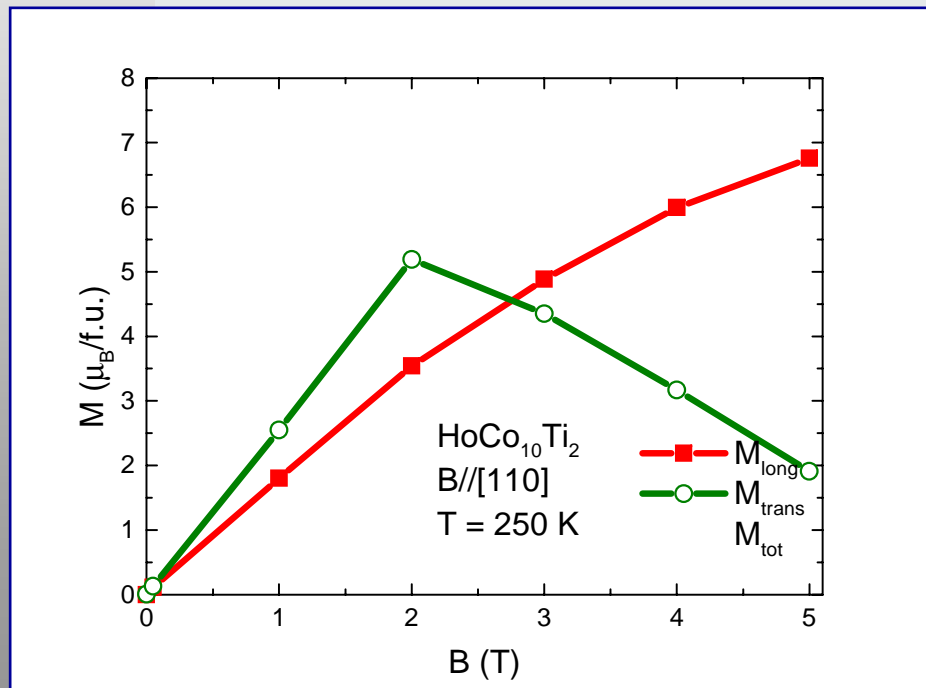
LONGITUDINAL MAGNETIZATION IN $\text{HoCo}_{10}\text{Ti}_2$



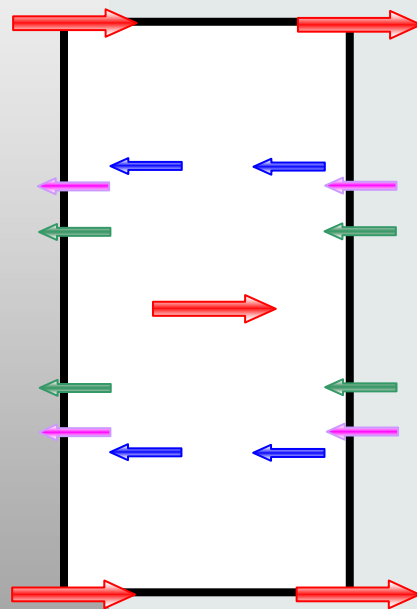
POLAR MAGNETIZATION MEASUREMENT IN $\text{HoCo}_{10}\text{Ti}_2$

Yuri Janssen. Ph. D Thesis

250 K

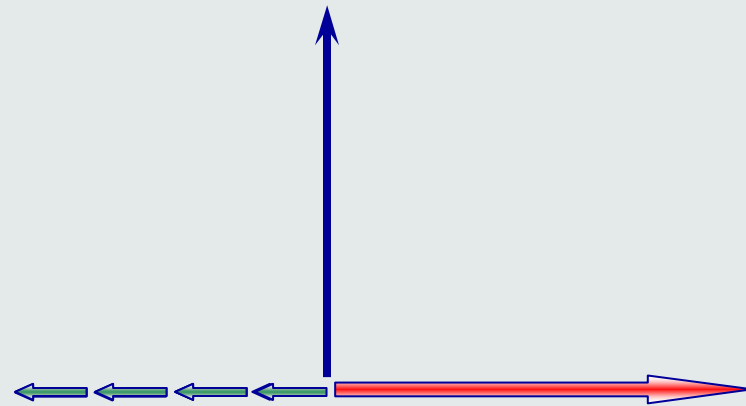


MAGNETIC ANISOTROPY IN $\text{HoCo}_{10}\text{Ti}_2$

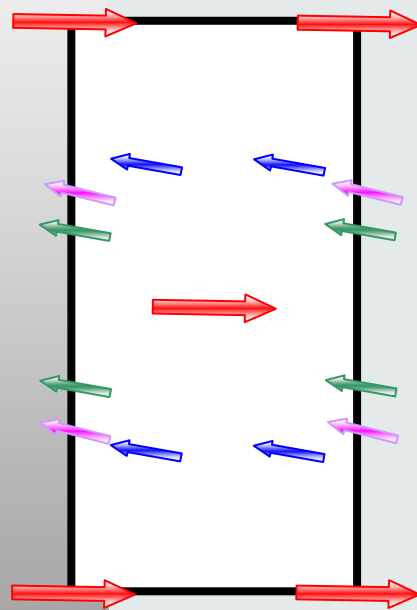


5 K

H 7.5 T 5 K

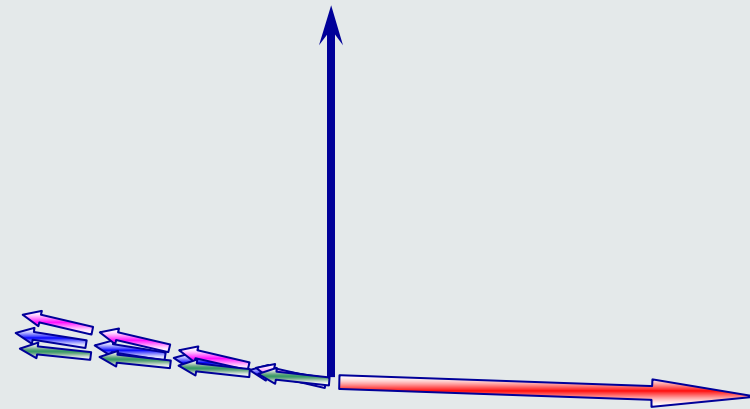


MAGNETIC ANISOTROPY IN $\text{HoCo}_{10}\text{Ti}_2$

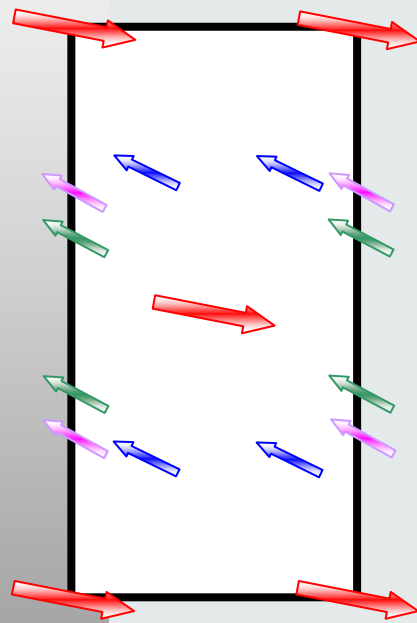


50 K

H 7.5 T 50 K

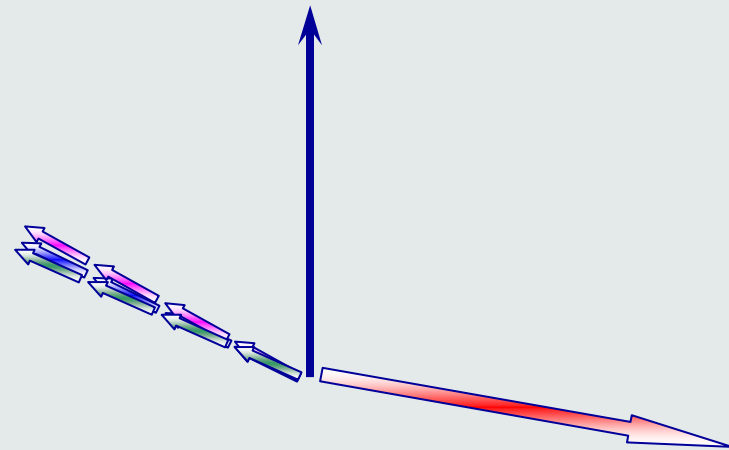


MAGNETIC ANISOTROPY IN $\text{HoCo}_{10}\text{Ti}_2$

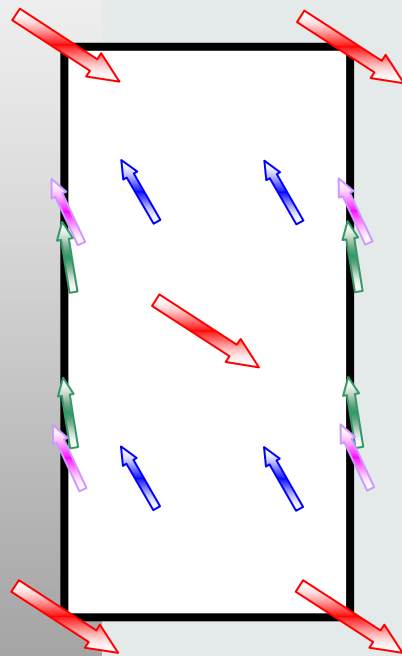


100 K

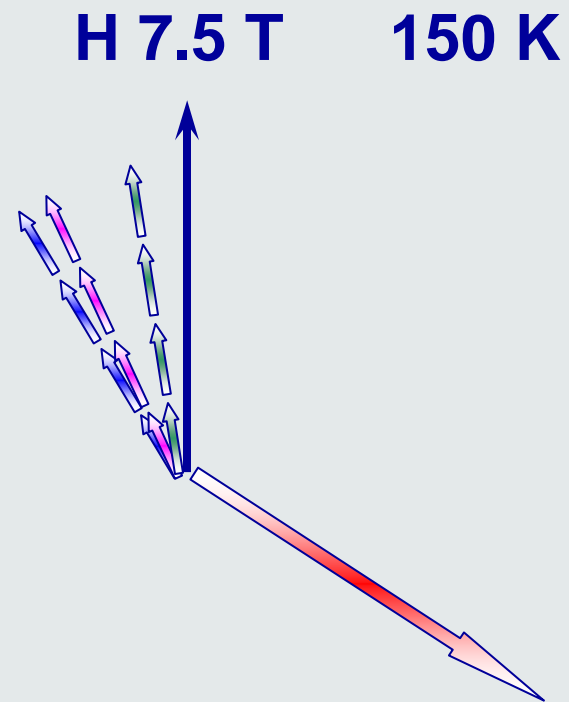
H 7.5 T 100 K



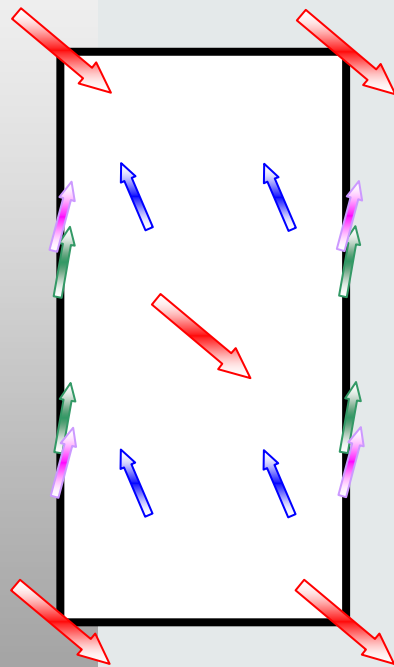
MAGNETIC ANISOTROPY IN $\text{HoCo}_{10}\text{Ti}_2$



150 K

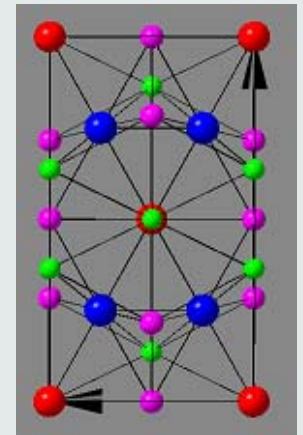
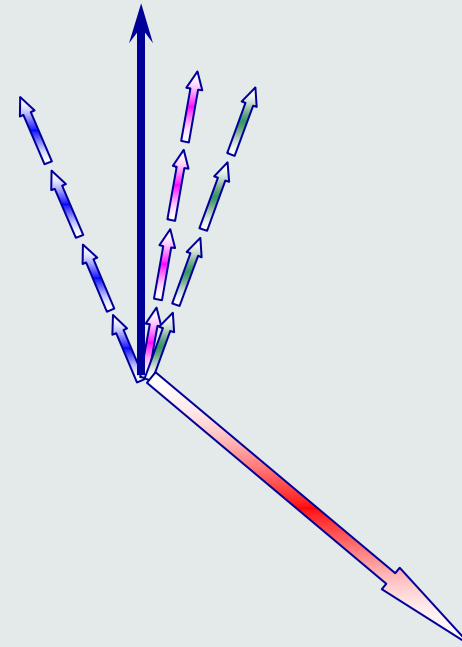


MAGNETIC ANISOTROPY IN $\text{HoCo}_{10}\text{Ti}_2$



200 K

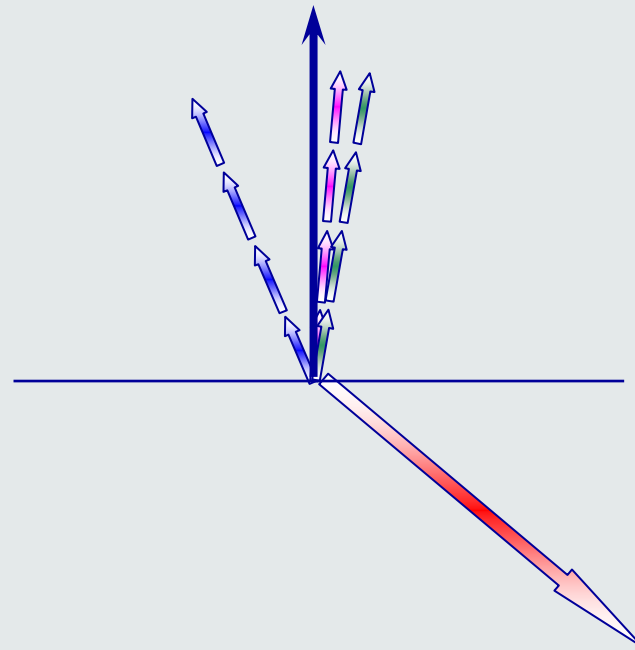
H 7.5 T 200 K



CONCLUSION

- **PND** gives **POLAR SITE MAGNETISATION**

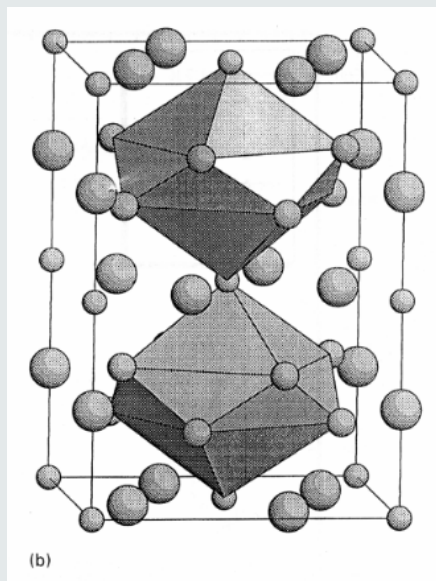
250 K H=7.5 T



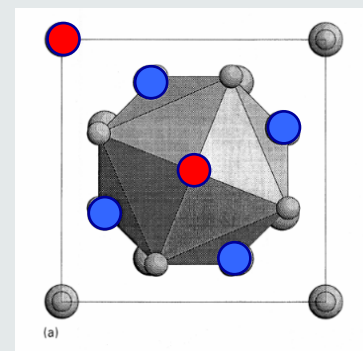
Yu. Janssen, A. Gukasov, E. Brück, K.H.J. Buschow and F.R. de Boer.

MAGNETIC STRUCTURE OF $U_3Al_2Si_3$: POLARIZED NEUTRONS DIFFRACTION REFINEMENT

Ternary compounds $U_3M_2M'_3$ with $M=Al, Ga$ $M' = Si, Ge$
SG $I4/mcm$ derivative of the antitype- Cr_5B_3



$U1, U2$



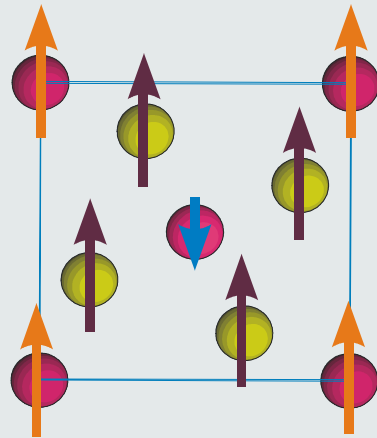
$4_z \times U3$

F. Weitzer, M Potel, H Noel, P Rogl, J Sol. St. Chem, 111, 267, 1994

NEUTRON POWDER DIFFRACTION FROM $U_3Al_2Si_3$

G4.1 ORPHEE, CEA-Saclay

no extra peaks
 $k=0$



$$U1 = 1.13 \mu_B$$

$$U2 = -0.46 \mu_B$$

$$4 \times U3 = 1.26 \mu_B$$

Spin direction in the ab plane

SINGLE CRYSTAL . UNPOLARIZED NEUTRONS

4-circle 6T2 LLB, Saclay 0.9 Å; 227 reflections (122 independent) measured at 70K

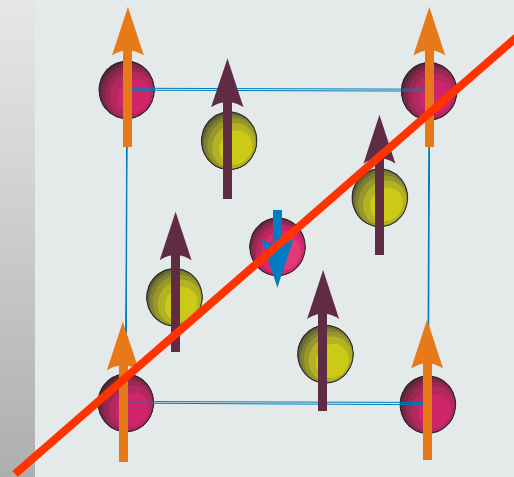
$$R_{F2} = 5.05\%$$

Magnetic structure

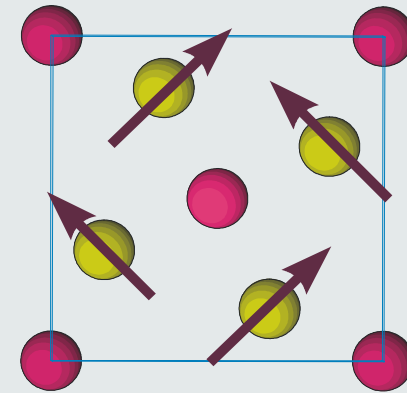
-compatible with powder results **but -**
there is another (noncollinear) solutions with
about the same $R_{F2} = 6.8-7.1\%$

POLARIZED NEUTRONS

5C1 LLB, Saclay 0.84 Å $H=2T \parallel 110$ and $H \parallel 100$



$$\chi^2=62.5$$



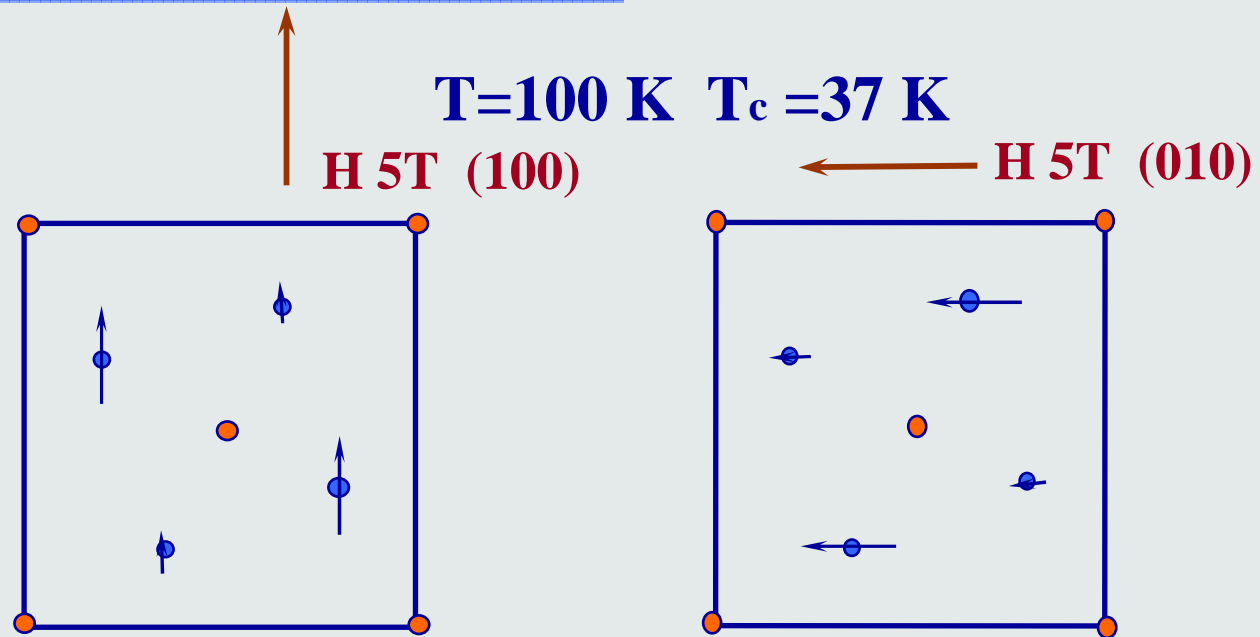
$$\chi^2=5.3$$

BEST MODEL : $\chi^2=3.2$

$$\theta=38^\circ(3) \quad \theta=-42^\circ(3) \quad U1 = U2 = 0.16 \mu_B$$

$$4 \times U3 = 1.29 \mu_B$$

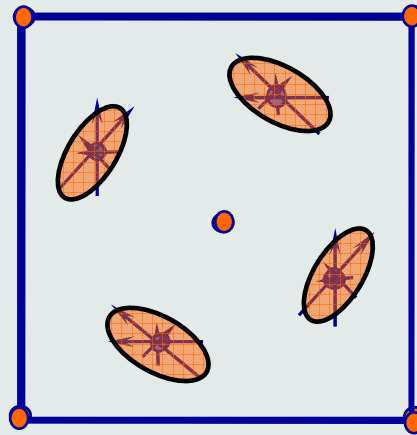
SITE SUSCEPTIBILITY IN PARAMAGNETIC REGION ($U_3Al_2Si_3$)



SITE SUSCEPTIBILITY IN PARAMAGNETIC REGION ($U_3Al_2Si_3$)

100 K H 5T (100)

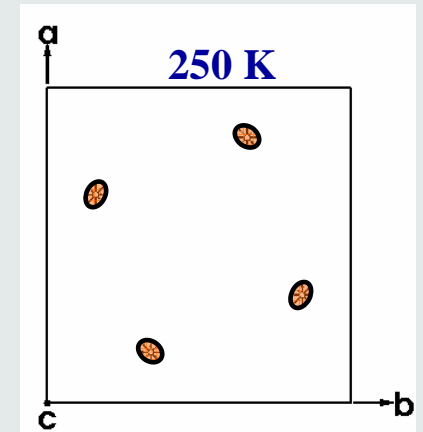
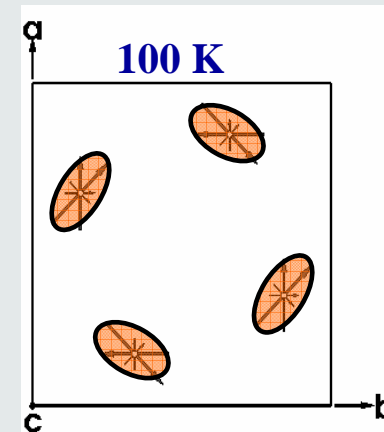
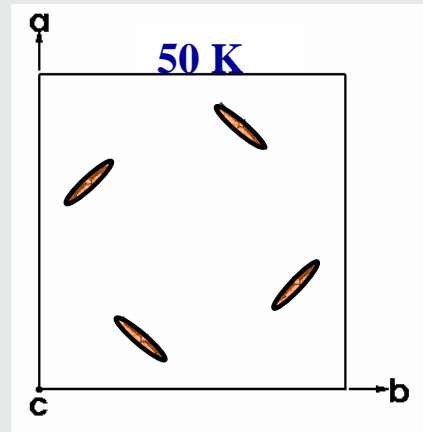
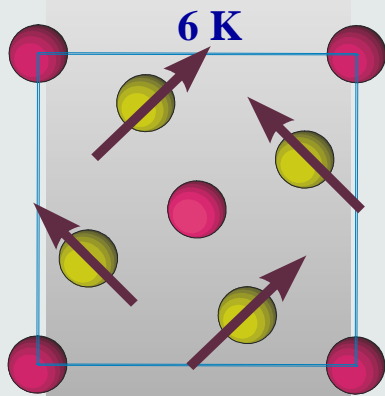
100 K H 5T (110)



$$M^\alpha(\mathbf{r}) = \chi^{\alpha\beta}(\mathbf{r}) H^\beta$$

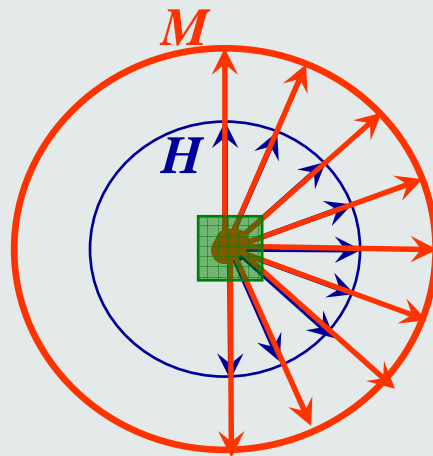
$U_3Al_2Si_3$ IN PARAMAGNETIC REGION

*A Gukasov, P Rogl, P J Brown, M Mihalik and A Menovsky.
J. Phys. C, 14, 8984 2002*



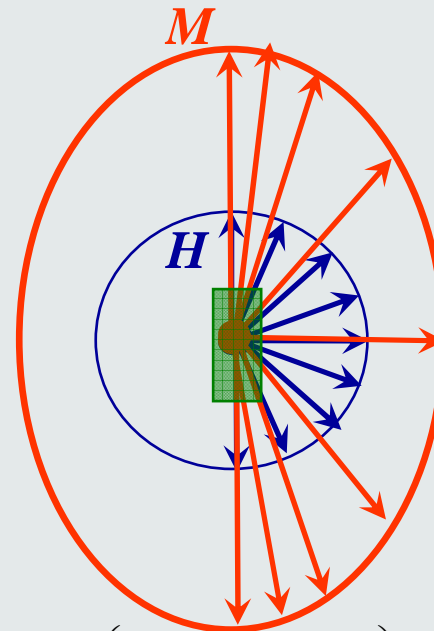
ANISOTROPIC SUSCEPTIBILITY

CUBIC, $\chi_{11} = \chi_{22} = \chi_{33}$



$$\chi_{ij} = \begin{pmatrix} \chi_{11} & 0 & 0 \\ 0 & \chi_{11} & 0 \\ 0 & 0 & \chi_{11} \end{pmatrix}$$

UNIAXIAL $\chi_{11} = \chi_{22} < \chi_{33}$



$$\chi_{ij} = \begin{pmatrix} \chi_{11} & 0 & 0 \\ 0 & \chi_{11} & 0 \\ 0 & 0 & \chi_{33} \end{pmatrix}$$

ANISOTROPIC SUSCEPTIBILITIES

$$\chi_{ij} = \begin{pmatrix} \chi_{11} & \chi_{12} & \chi_{13} \\ & \chi_{22} & \chi_{23} \\ & & \chi_{33} \end{pmatrix}$$

Bulk magnetisation

$$M_i(\mathbf{r}) = \chi_{ij} H_j$$

The number of independent components of χ_{ij} is determined by the crystal symmetry class:

cubic groups	1	parameter
all uniaxial groups	2	parameters
Orthorhombic	3	...
Monoclinic	4	...
Triclinic	6	

ANISOTROPIC SUSCEPTIBILITIES

Bulk magnetisation

$$M_i = \sum_a M_i^a = \sum_a \chi_{ij}^a H_j$$

$$M_i^b = R(t) \chi_{ij}^a R(t)^{-1} H_j$$

$R(t)$ is the symmetry operator $r_b = R(t) r_a$

$$M_i = \sum_a R(t) \chi_{ij}^a R(t)^{-1} H_j$$

REFINEMENT OF ANISOTROPIC SUSCEPTIBILITIES

$$I^{\pm} \propto N^2 \pm 2 P_0 N M_z + M^2$$

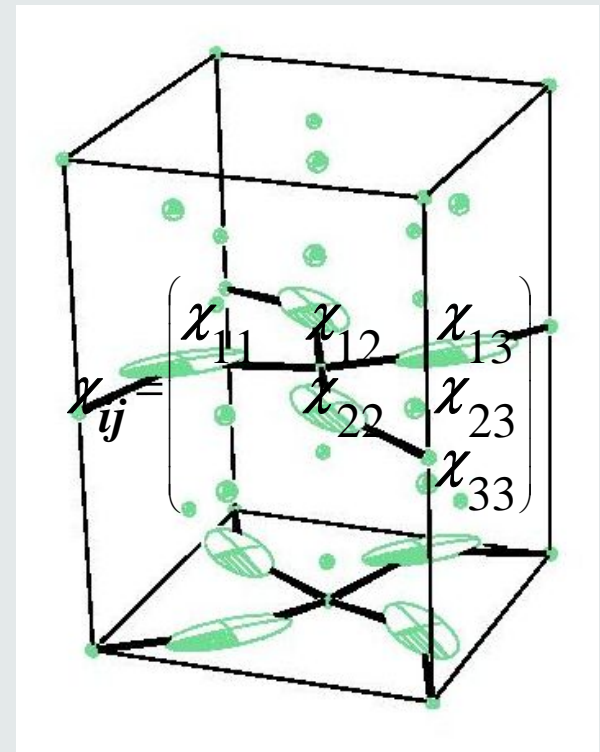
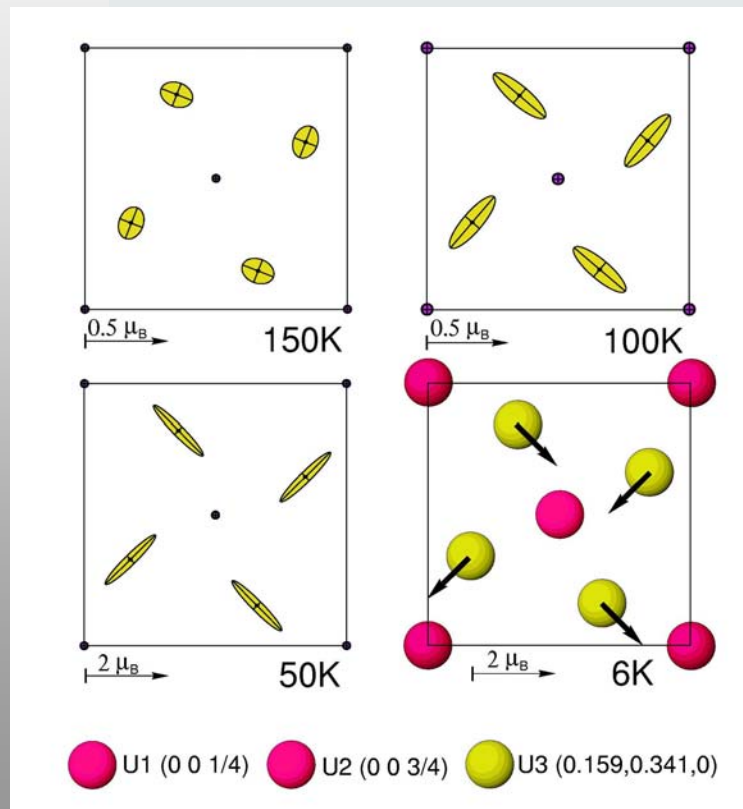
$$M_i = \chi_{ij}^a H_j$$

$$\chi_{ij} = \begin{pmatrix} \chi_{11} & \chi_{12} & \chi_{13} \\ & \chi_{22} & \chi_{23} \\ & & \chi_{33} \end{pmatrix}$$

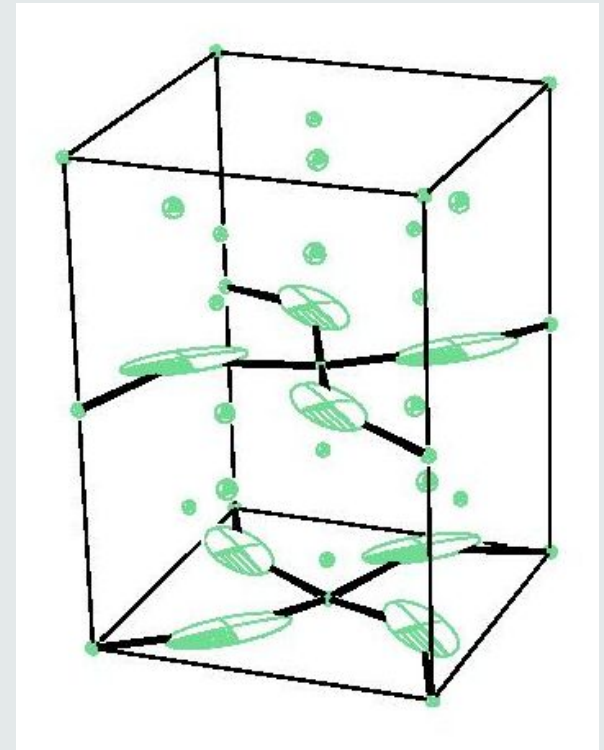
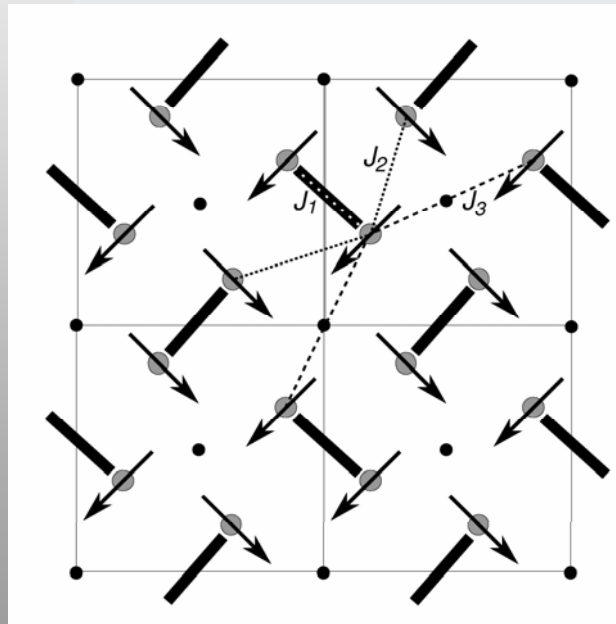
$$I^{\pm} \propto N^2 \pm 2 F_N (P_0^* \chi_{ij}^a H_j) + |\chi_{ij}^a H_j|^2$$

$$R = I^+ / I^-$$

TEMPERATURE DEPENDENCE OF *MAGNETIC ELLIPSOIDS* IN $U_3Al_2Si_3$



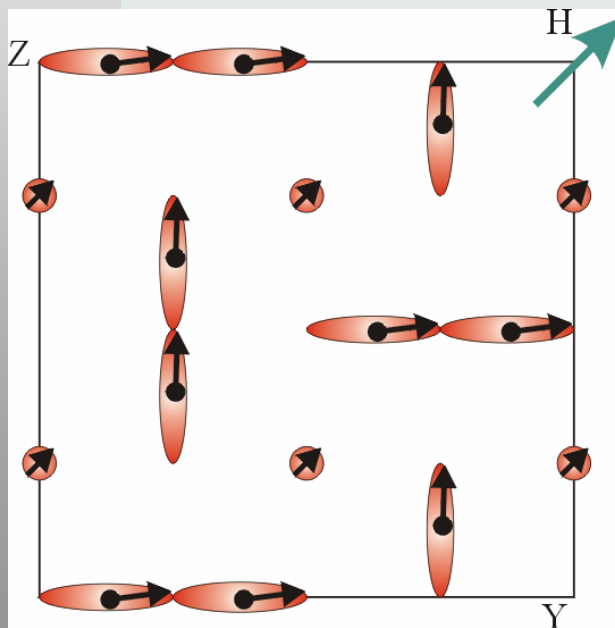
TEMPERATURE DEPENDENCE OF *MAGNETIC ELLIPSOIDS* IN $U_3Al_2Si_3$



PROLATE AND OBLATE MAGNETIC ELLIPSOIDS

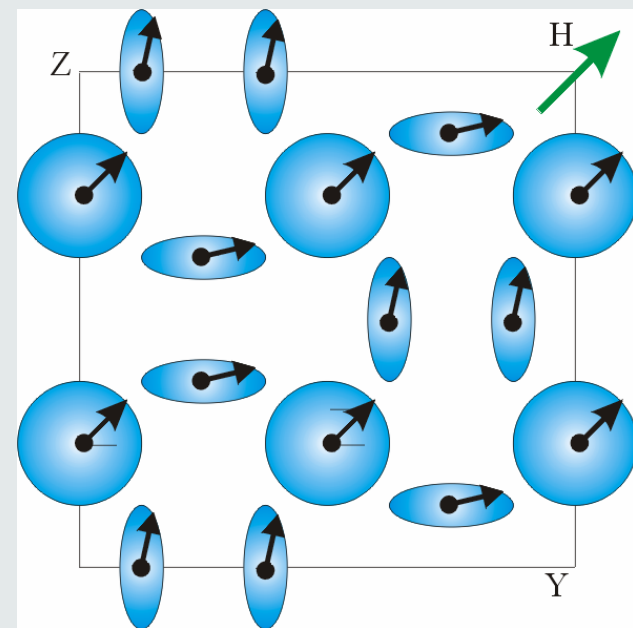
Prolate Sm_3Te_4

$$\chi_{11} < \chi_{33}$$

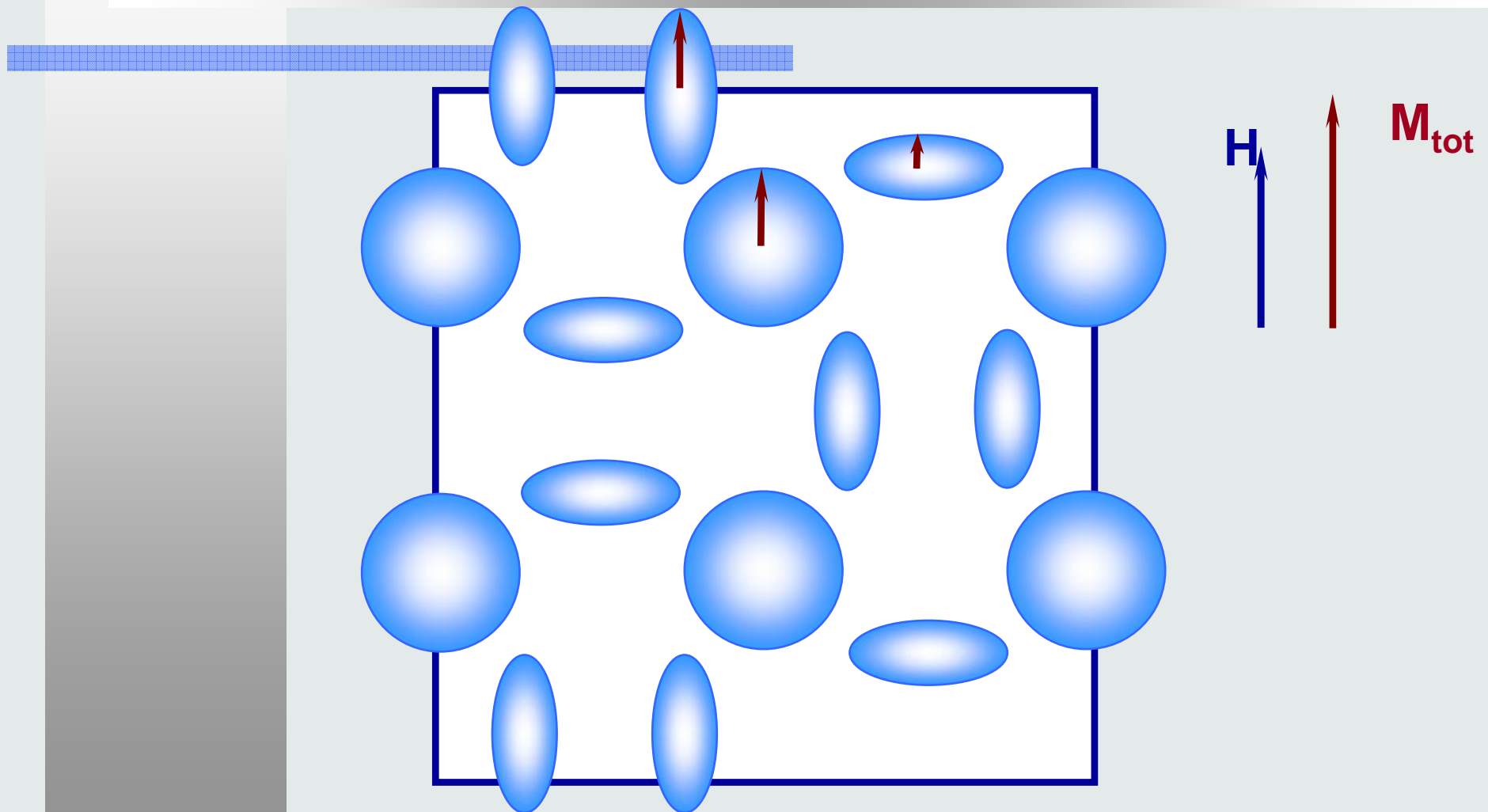


Oblate $\text{Nd}_{3-x}\text{S}_4$

$$\chi_{11} > \chi_{33}$$

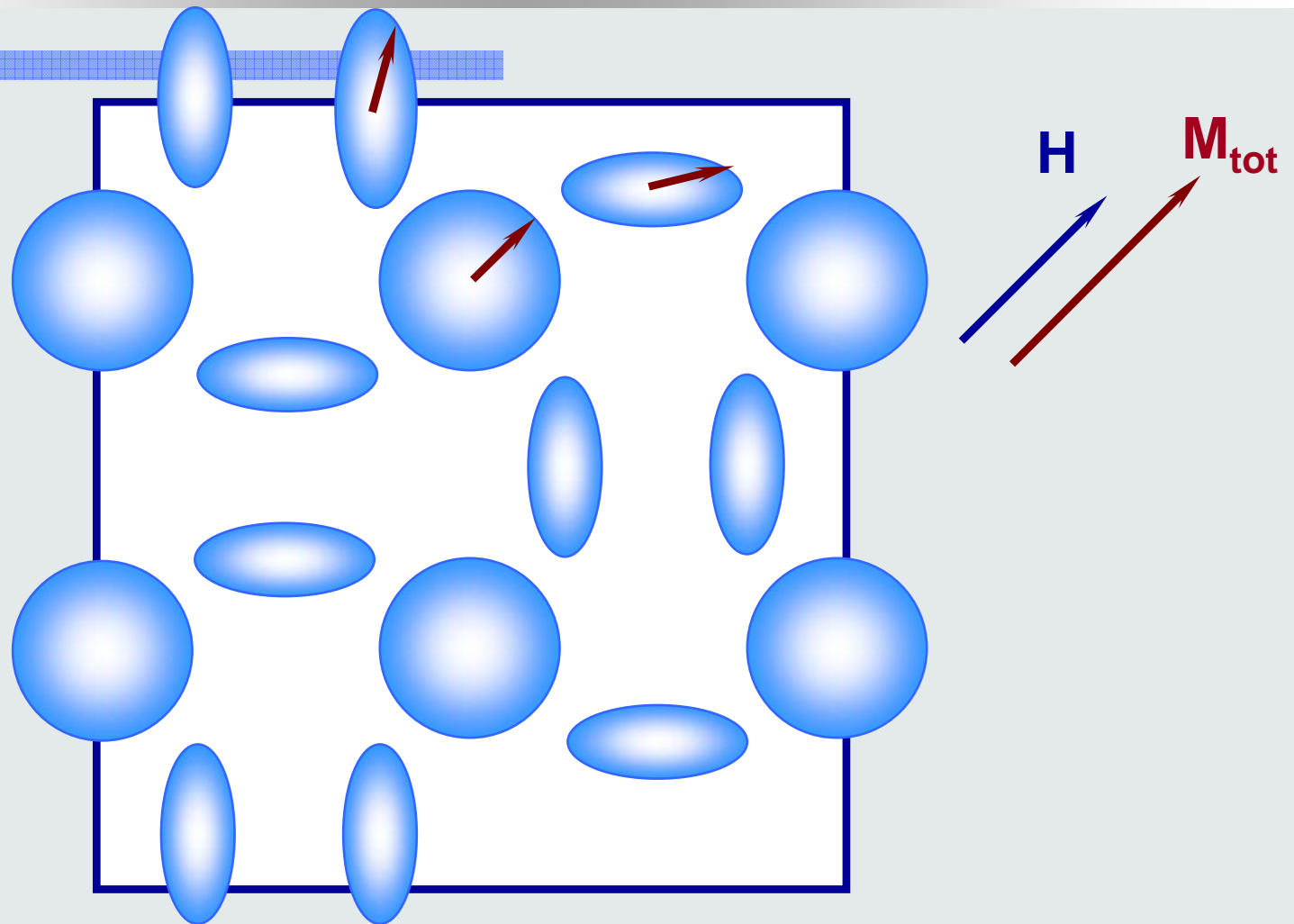


OBLATE MAGNETIC ELLIPSOIDS IN $\text{Nd}_{3-x}\text{S}_4$



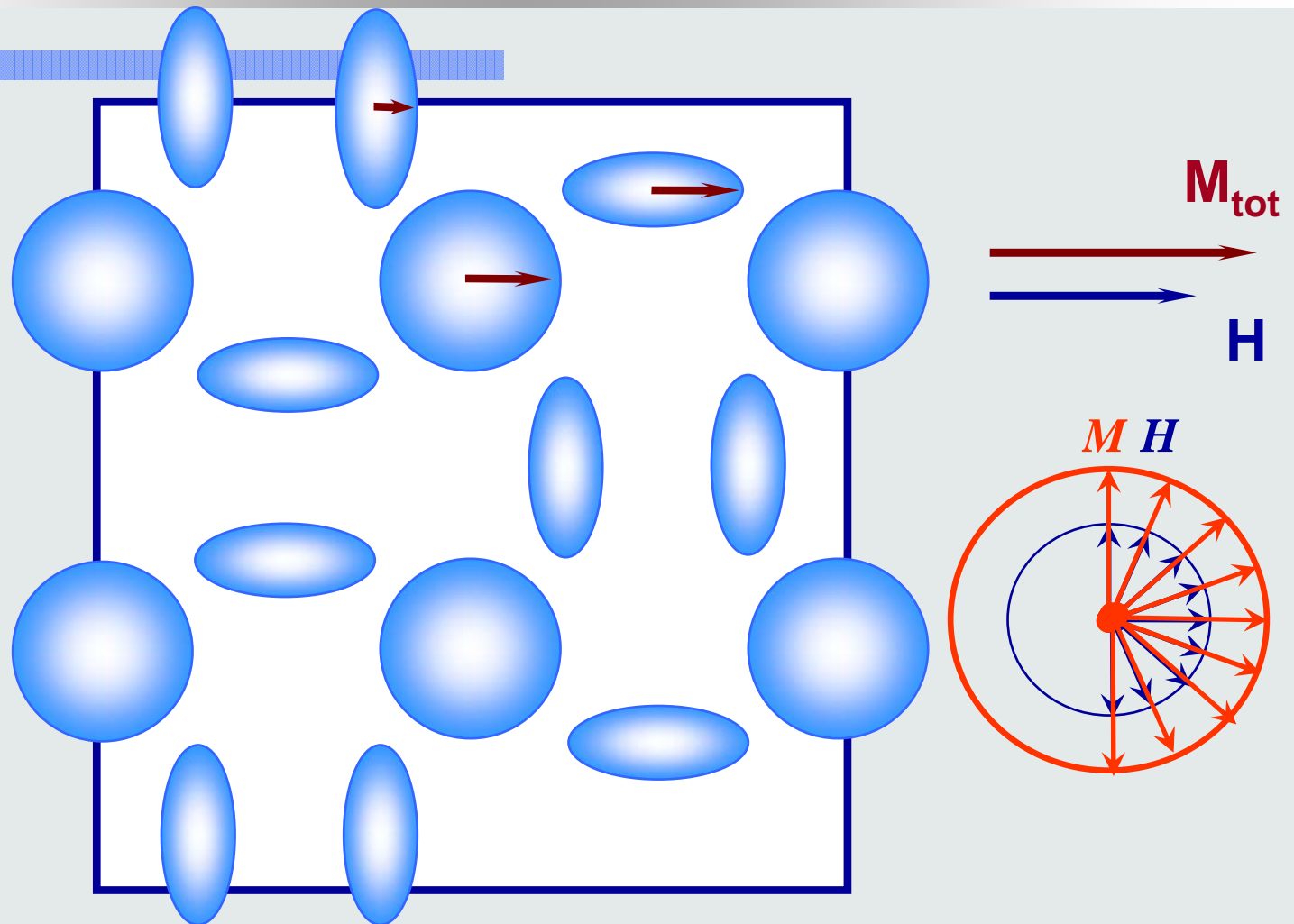
A Gukasov and P J Brown, J Phys C, 14, 8831, 2002

OBLATE MAGNETIC ELLIPSOIDS IN $\text{Nd}_{3-x}\text{S}_4$



A Gukasov and P J Brown, J Phys C, 14, 8831, 2002

OBLATE MAGNETIC ELLIPSOIDS IN $\text{Nd}_{3-x}\text{S}_4$



A Gukasov and P J Brown, J Phys C, 14, 8831, 2002

ATOMIC DISPLACEMENT PARAMETERS (ADPs) AND ATOMIC SUSCEPTIBILITY PARAMETERES (ASPs)

- **ADPs are a probe of the shape of elastic potential well**
- **ADPs give informaton about atomic vibration, dynamics, disorder ...**
- **ASPs :are a probe of magnetic interaction**
- **symmetry constraints of ASPs the same as for ADPs**
- **Anomalous ASPs indicate strong local anisotropy and a possible channel of ordering**

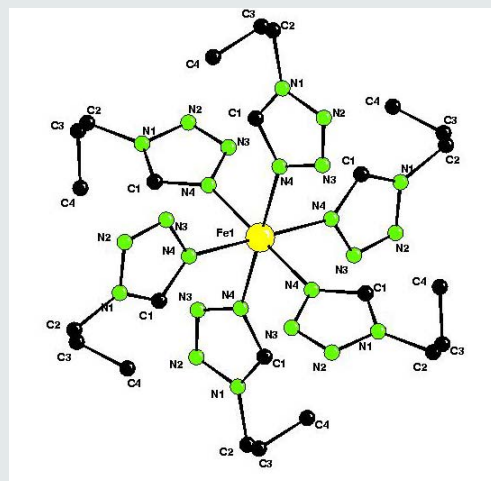
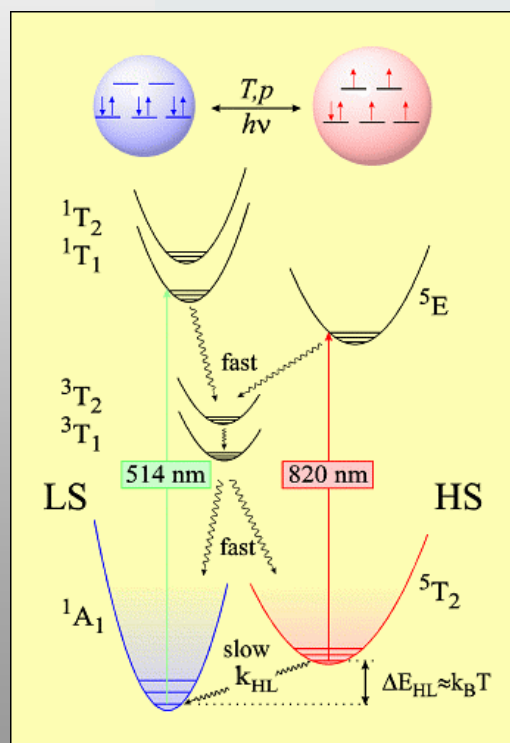
CONCLUSIONS

- PN give access :
 - to small magnetic densities ($10^{-3} \mu\text{B}$)
 - wave vector susceptibility $\chi(\mathbf{q})$
 - **local susceptibility tensor $\chi^{\alpha\beta}(\mathbf{r})$**
- Very large covalency in Rutenates and rather ordinary one in garnets
- Very high magnetisation ‘ prolate ’ anisotropy for Sm_3Te_4 and medium ‘ oblate ’ for Nd_3S_4

MOST IMPORTANT CONCLUSION

- **In a paramagnetic state the moments of equivalent atoms are equal, but...**
- **under magnetic field some of them will be more equal than the others !**

Light Induced Excited Spin State Trapping (LIESST) in $\text{Fe}(\text{ptz})_6](\text{BF}_4)_2$



$\lambda \sim 514 \text{ nm}$ direct

$\lambda = 820 \text{ nm}$ reverse

S. Decurtins et al. Inorg. Chem. 24 (1985) 2174

Photo-excitation setup at 5C1 diffractometer

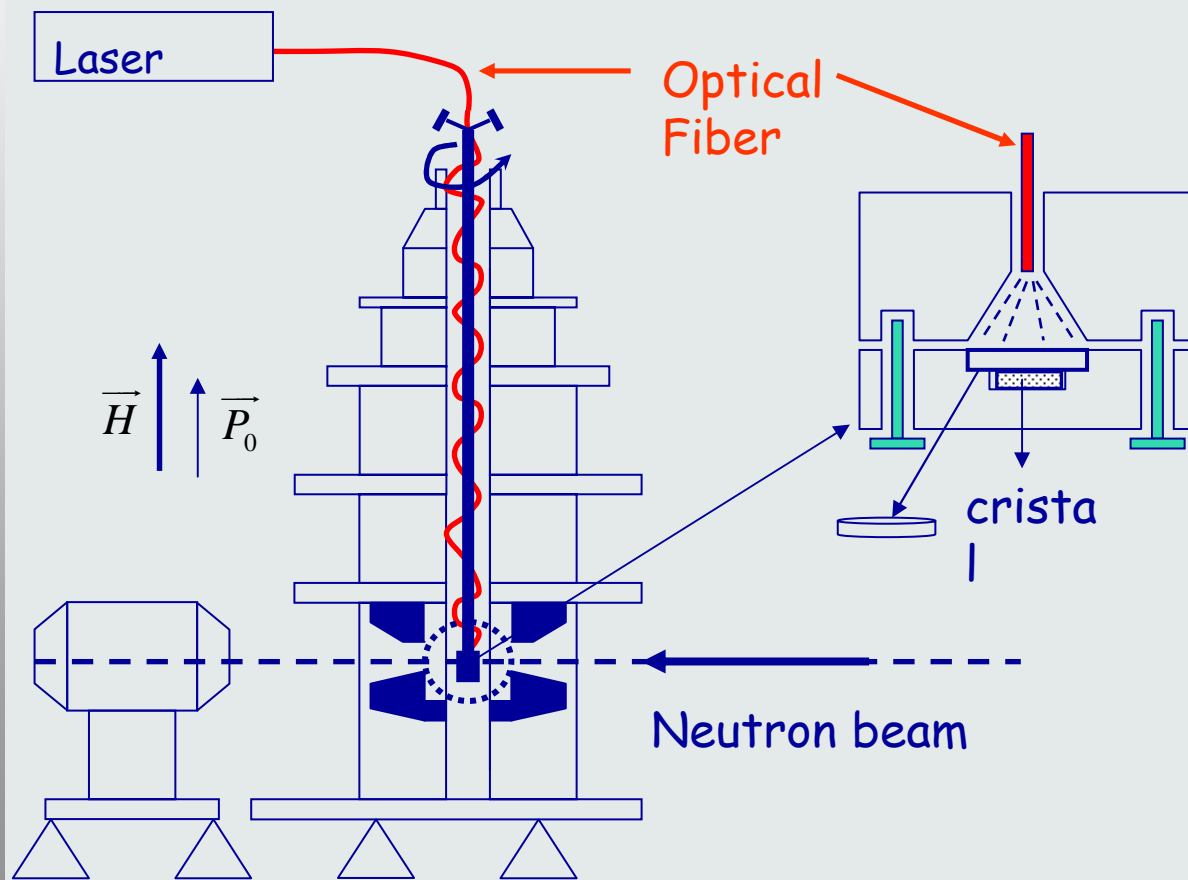
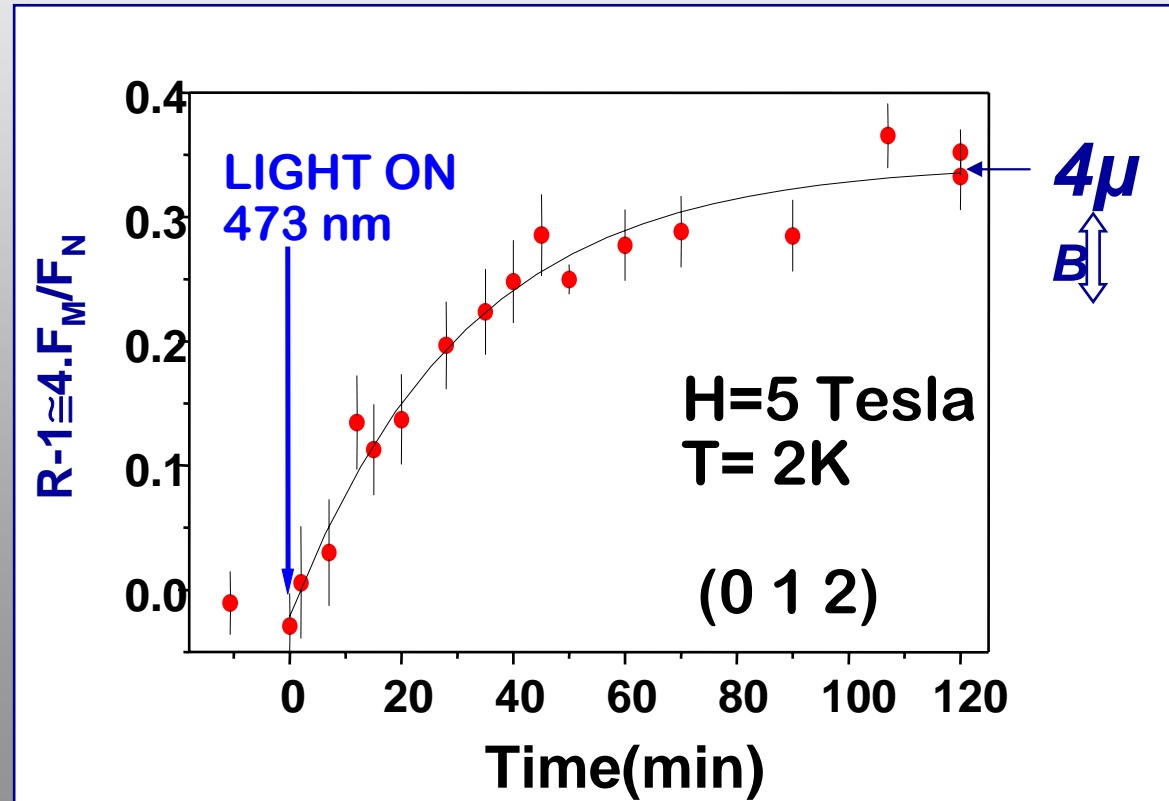
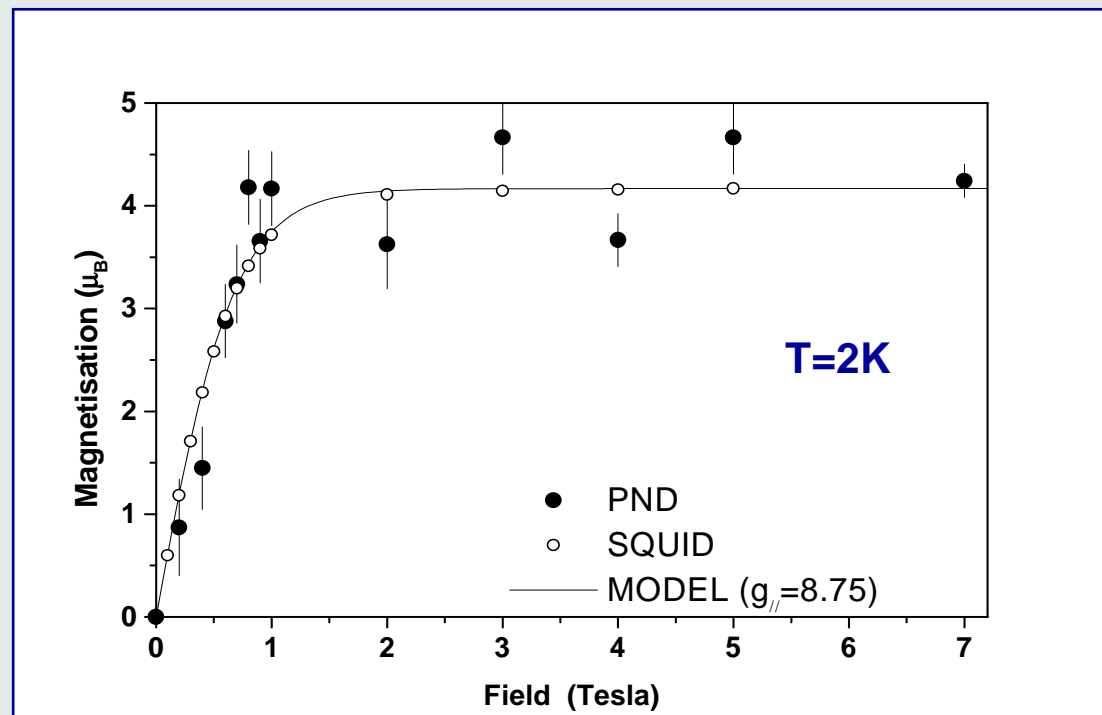


Photo-excited state in $[\text{Fe}(\text{ptz})_6](\text{BF}_4)_2$

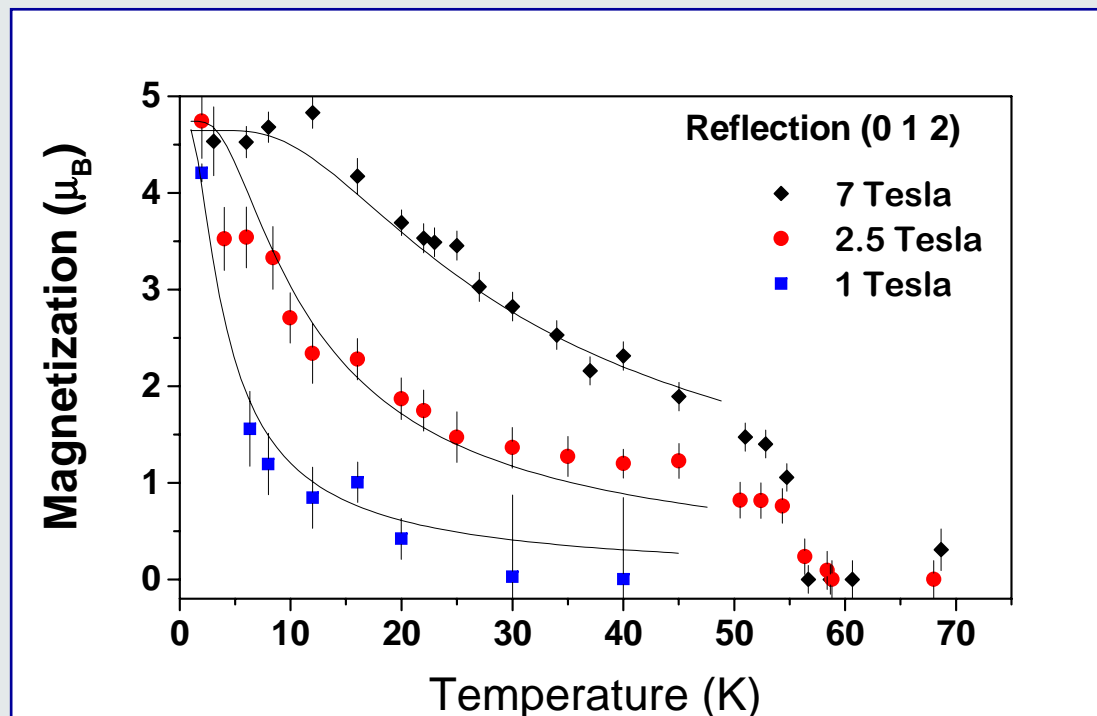
A. Goujon, B. Gillon A Gukasov, J Jeltic, and F Varret Phys. Rev. B 67, 2003



Magnetization

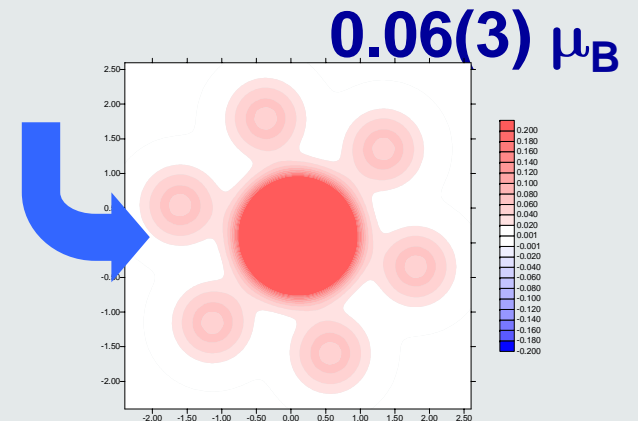
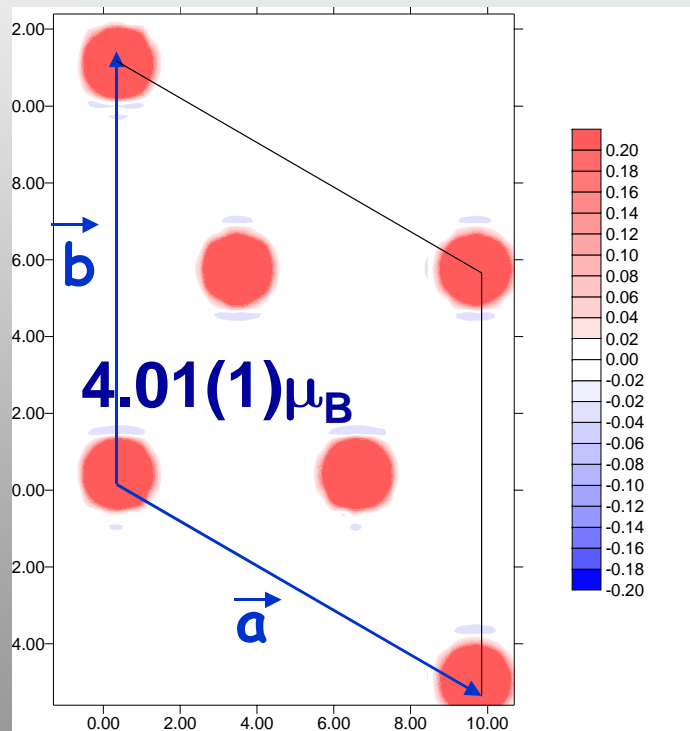


TEMPERATURE BEHAVIOUR



Spin Density of in Photo-induced State

projection on **c** →

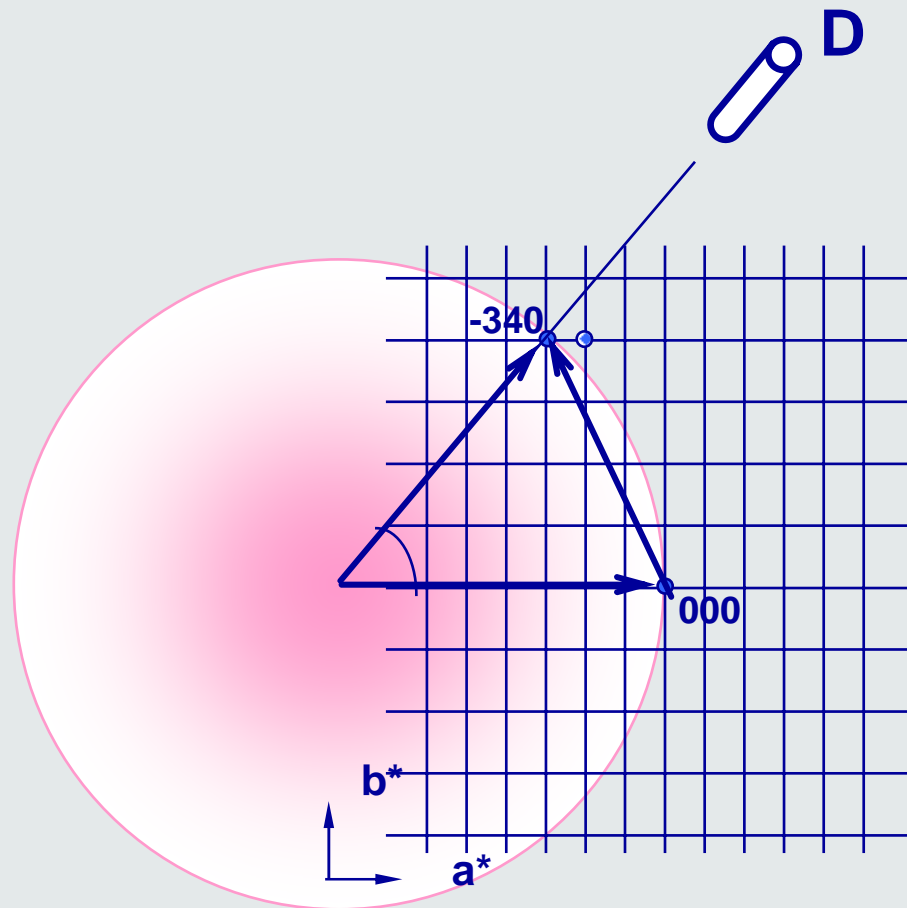


SOME EXPERIMENTAL ASPECTS OF POLARIZED NEUTRON DIFFRACTION

A. GUKASOV

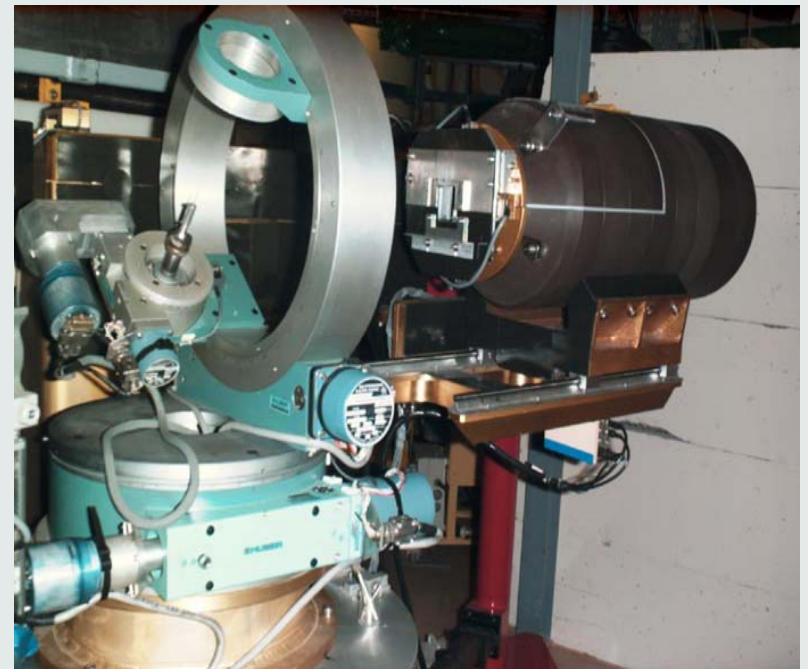
Laboratoire Léon Brillouin, CEA-CNRS, Saclay, France

CONVENTIONAL METHOD

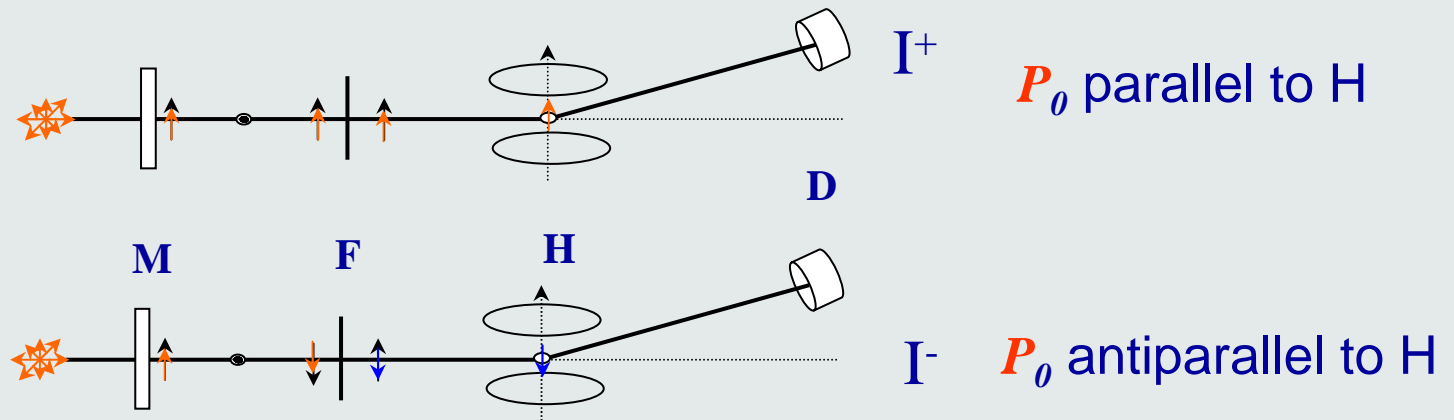


Unpolarized Neutron Diffraction

- **6T2, 4-circles mode**
- **Cu (220) 0.90 Å**
- **PG 1.55, 2.35 Å**
- **5-300 K**
- **6T2, Lifting counter mode**
- **7.5 T + 40 mK**
- **7.5 T +10 Gpa+40 mK**



PRINCIPLES OF NEUTRON POLARIZATION IN DIFFRACTION



$$I^\pm \propto (F_N \pm F_M)^2$$

$$I^\pm \propto F_N^2 \pm 2F_N(P_0 * F_M) + F_M^2 \quad (P_0=1)$$

$$\text{If } F_N = F_M \quad I^+ = 4F_N^2 \quad \Gamma = 0$$

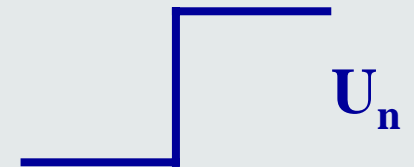
$$\text{if } P_0=0 \quad I \propto F_N^2 + F_M^2 = 2F_N^2$$

PRINCIPLES OF NEUTRON POLARIZATION BY TOTAL REFLECTION

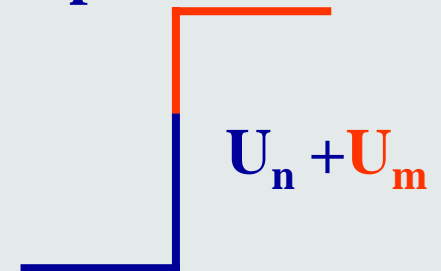
N9. Double Refraction and Polarization of Neutron Beams. OTTO HALPERN, *University of Southern California*.—The magnetic double-refraction¹ of neutrons can be utilized to obtain completely polarized neutron beams with an intensity loss of only 50 percent of the primary beam. For this purpose a well defined neutron beam of moderate spread in wave-length is allowed to fall on a sheet of iron which can be magnetized. To obtain a maximum effect the direction of magnetization should be chosen parallel to the projection of the beam on the iron sheet. Total reflection will then occur for the two spin states at different critical glancing angles which will be smaller and larger than the critical angle for unmagnetized iron. Theory leads in the case of iron to values of 12.5 minutes and 6 minutes, respectively. Variation of the direction of magnetization should permit a test of the assumed expression for the interaction energy of the magnetic moments of neutron and ion.

¹ Halpern, Hamermesh, and Johnson, *Phys. Rev.* **59**, 981 (1941). The formula preceding (5.1) suffers from misprints; the denominator obviously is k^2 and not k ; furthermore $+1$ must be added to the right side.

Unpolarized



Spin up



Spin down

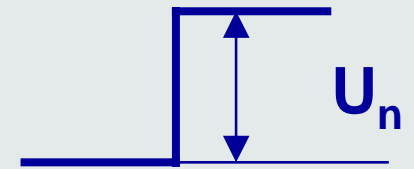


TOTAL REFLECTION FROM IRON

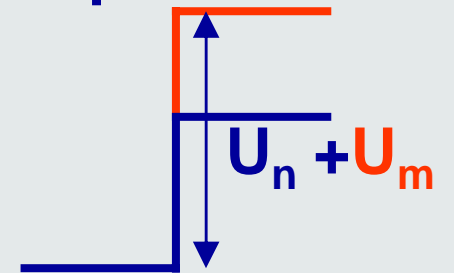
$$U_n \sim 9.4 \text{ Fm}$$

$$U_m \sim 6.0 \text{ Fm}$$

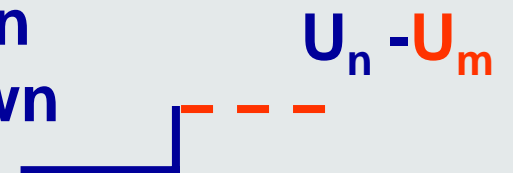
Unpolarized



Spin up



Spin down



PRINCIPLES OF NEUTRON POLARIZATION BY TOTAL REFLECTION

Total Reflection of Neutrons on Cobalt

MORTON HAMERMESH
Argonne National Laboratory, Chicago, Illinois
April 13, 1949

barns for Fe. At the same time, the magnetic amplitude for Co is $\sim 4.6 \times 10^{-13}$ cm, which is only slightly below the value 6.0×10^{-13} for Fe, so that for Co the magnetic amplitude *exceeds* the nuclear amplitude. Consequently, the refractive indices for the two spin states lie on opposite sides of unity for *all* wave-lengths, and only one of the spin components is capable of undergoing total reflection. With an arbitrarily broad spectrum of incident neutrons, the mirror will reflect a completely polarized beam.

D. J. Hughes and his associates are now conducting reflection experiments with Fe and Co.

¹ O. Halpern, Phys. Rev. **75**, 343 (1949).

² C. G. Shull and E. O. Wollan, unpublished.

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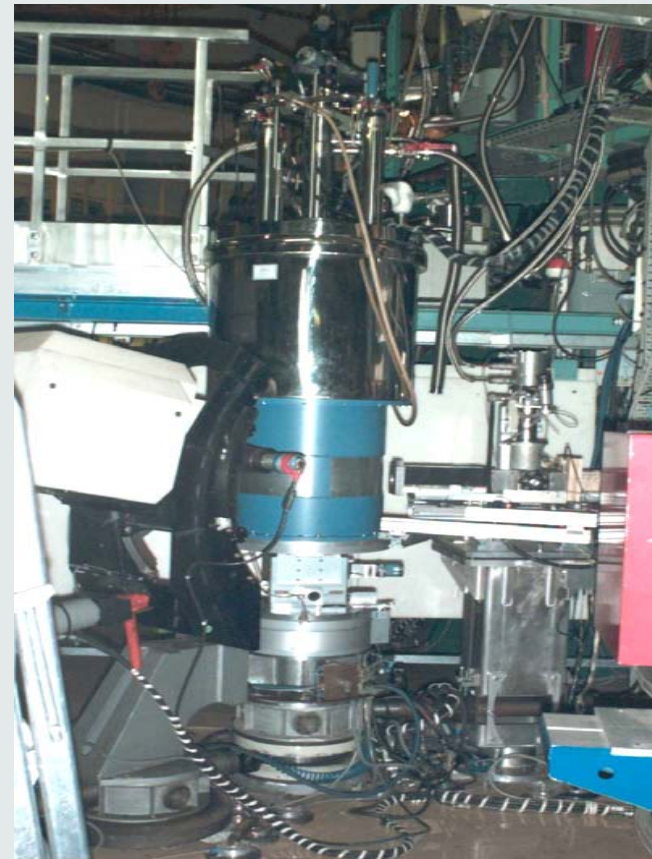
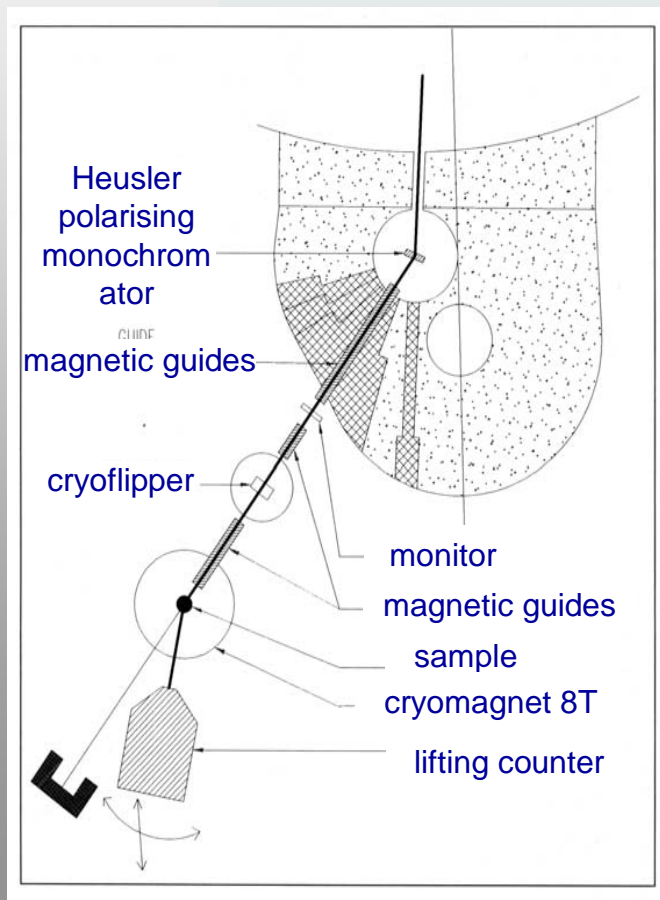
¹ O. Halpern, Phys. Rev. **75**, 343 (1949).

² C. G. Shull and E. O. Wollan, unpublished.

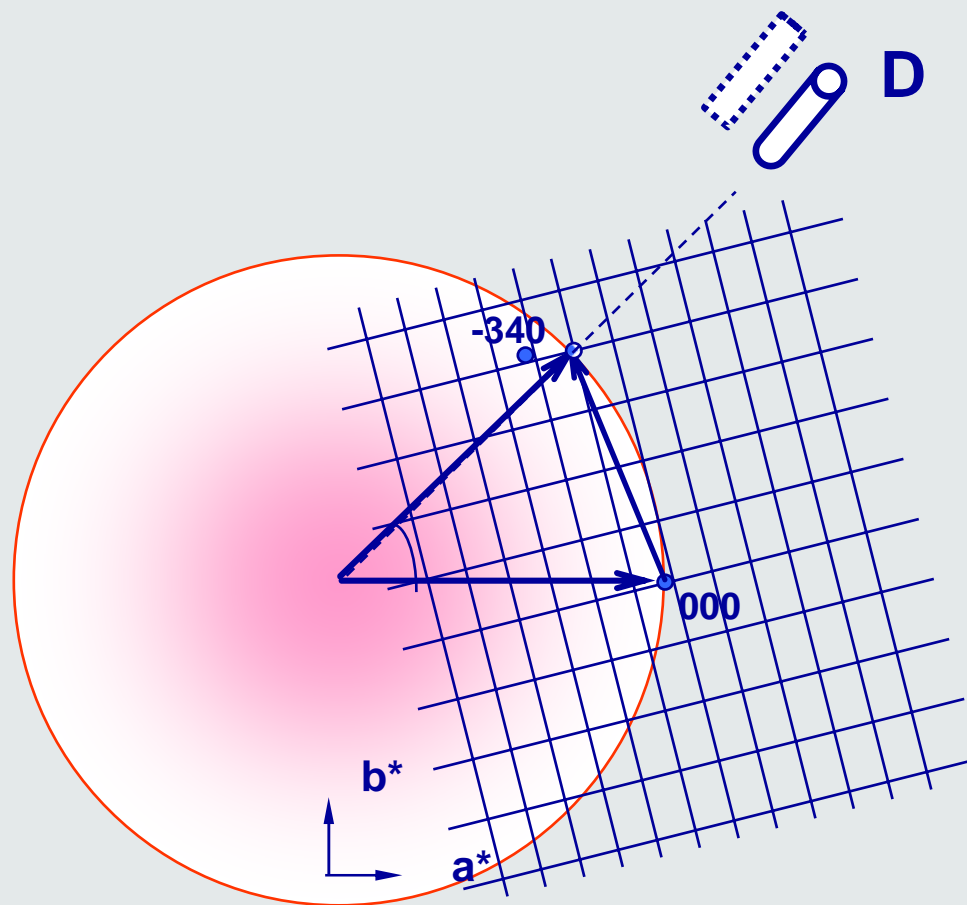
Heusler polarising monochromator of IN20, ILL



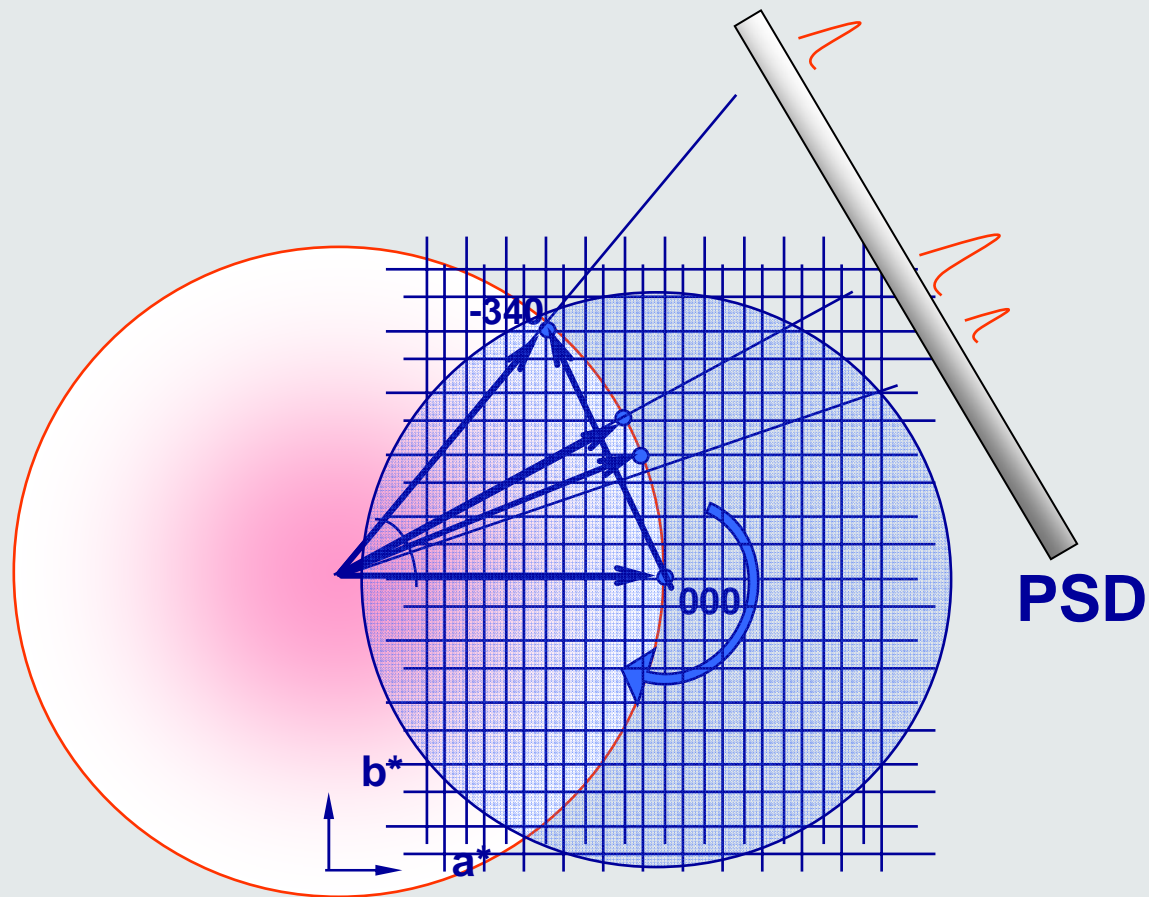
5C1 polarised neutron diffractometer (LLB)



CONVENTIONAL METHOD

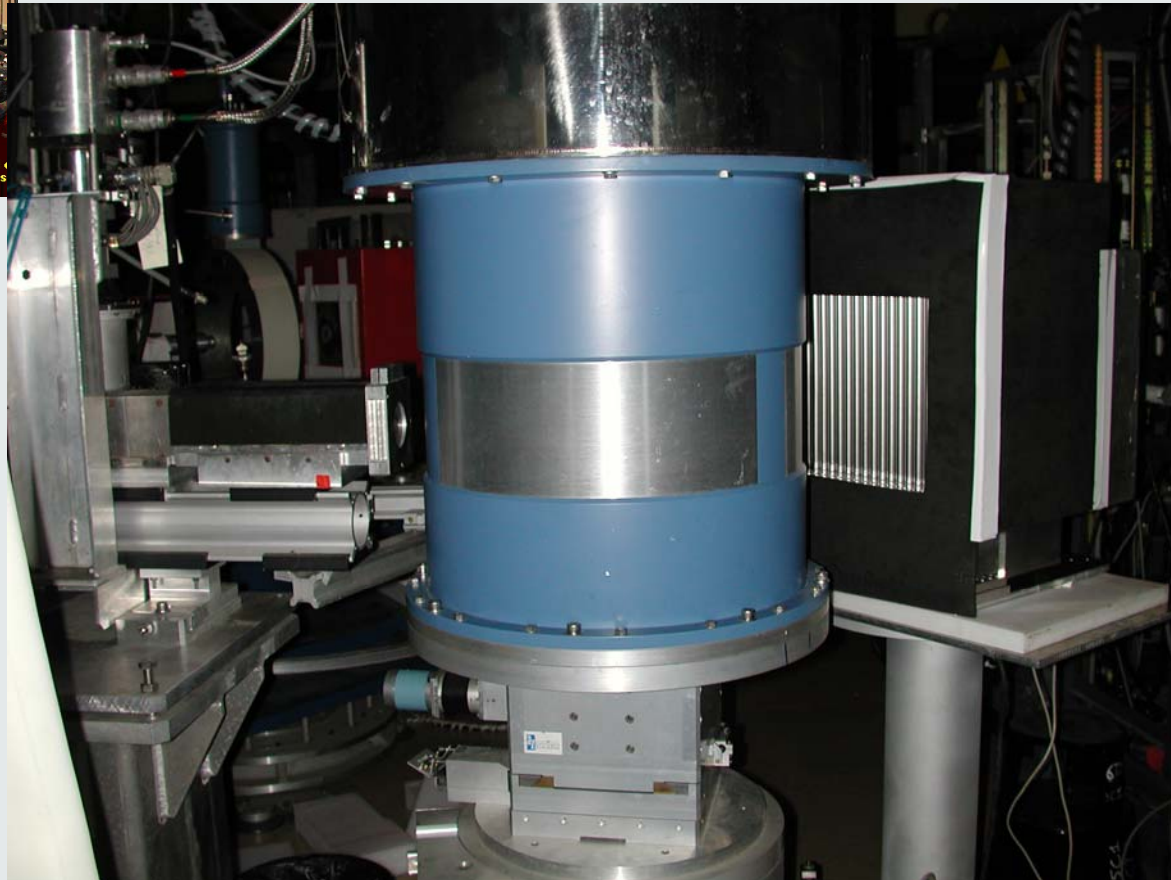
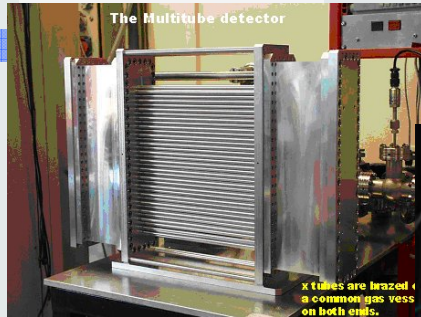


ROTATION (OSCILLATION) METHOD

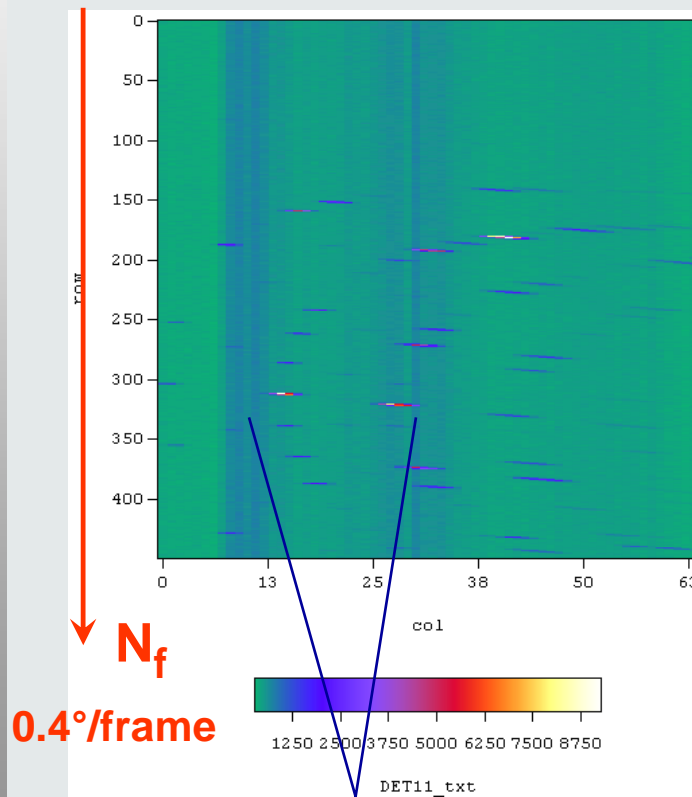


Very Intense Polarized Neutron Diffractometer

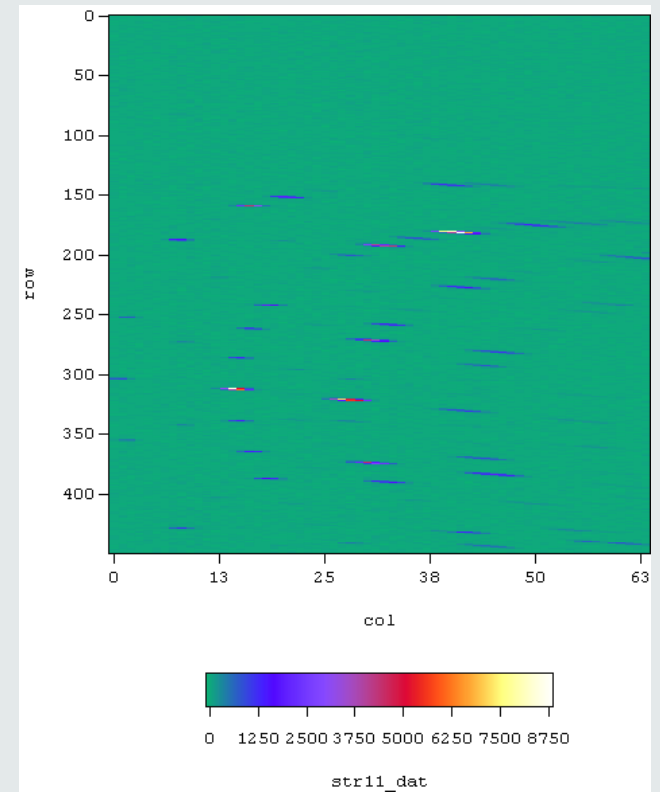
5C1, juin 2005



SINGLE SECTION OF ROTATION IMAGE (correspond to 1 tube rebinned in 64 pixels)

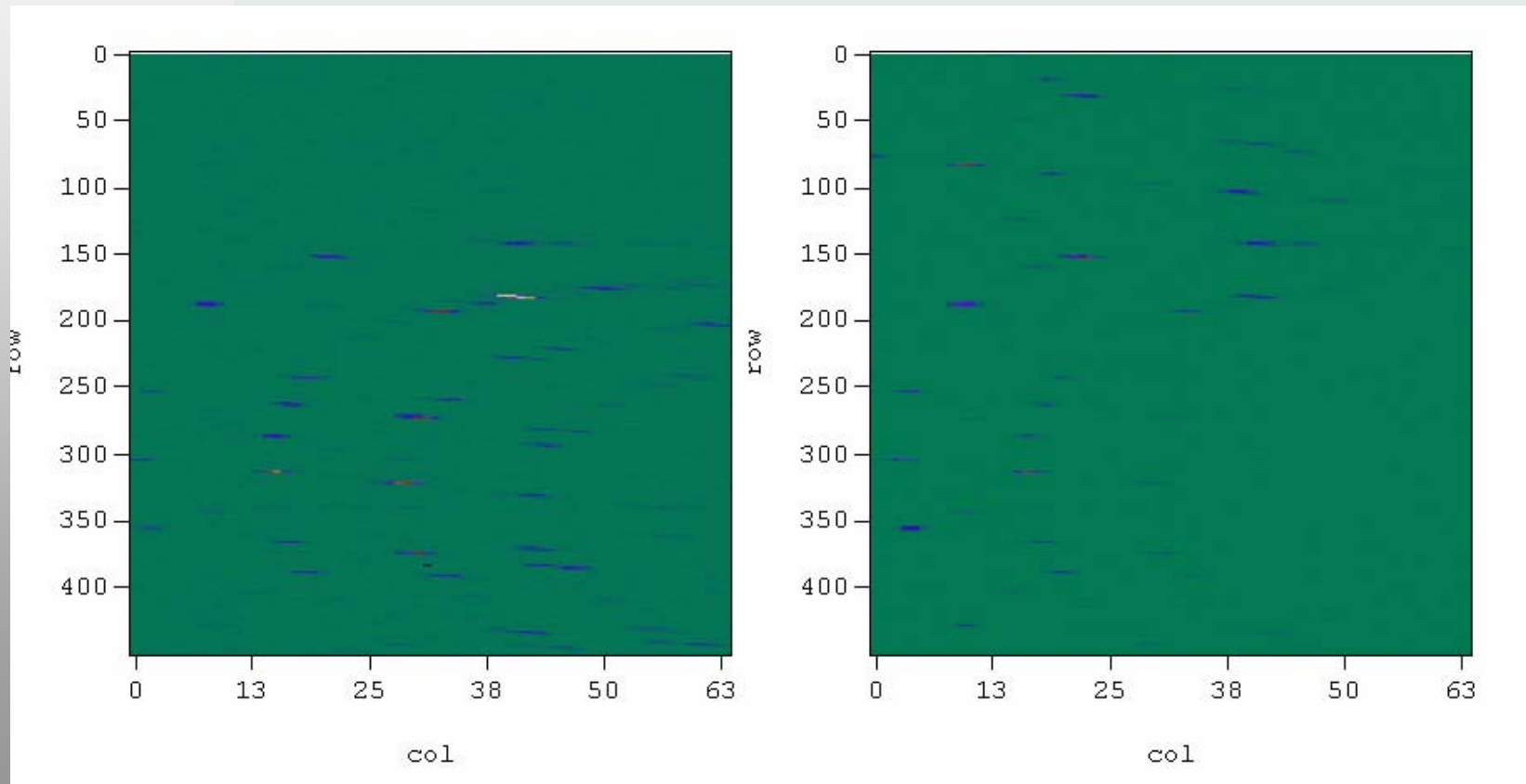


Aluminium lines



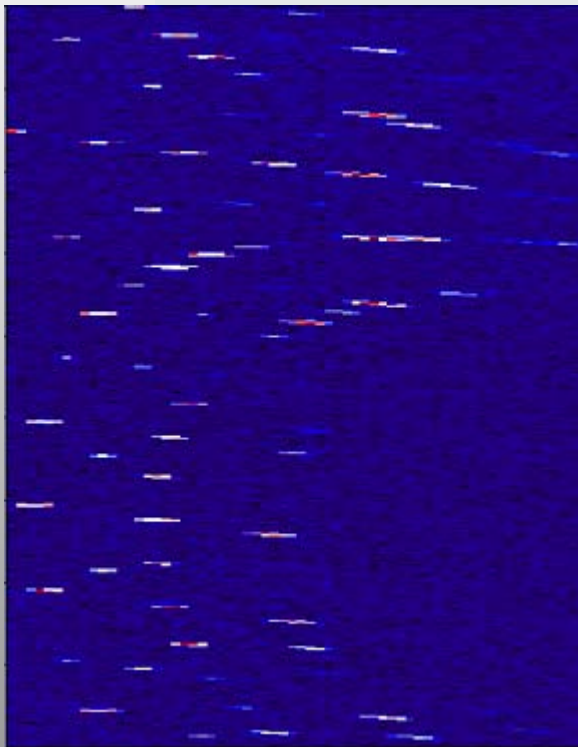
Background substructured

ROTATION IMAGES OF 2 NEIGHBOUR TUBES (rebinned in 64 pixels)

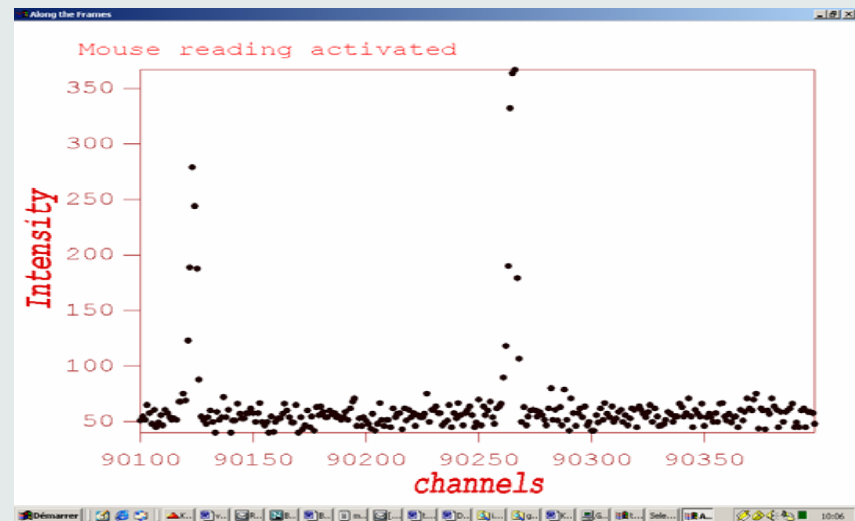


Very Intense Polarized Neutron Diffractometer

Étape 2005



Section d'image de précession de
 $\text{Mn(dca)(N}_2\text{C}_4\text{H}_4\text{)(H}_2\text{O)}$ a 1.5 K



Intensity of one *pixel* as a function
of *rotation angle*, step 0.1°

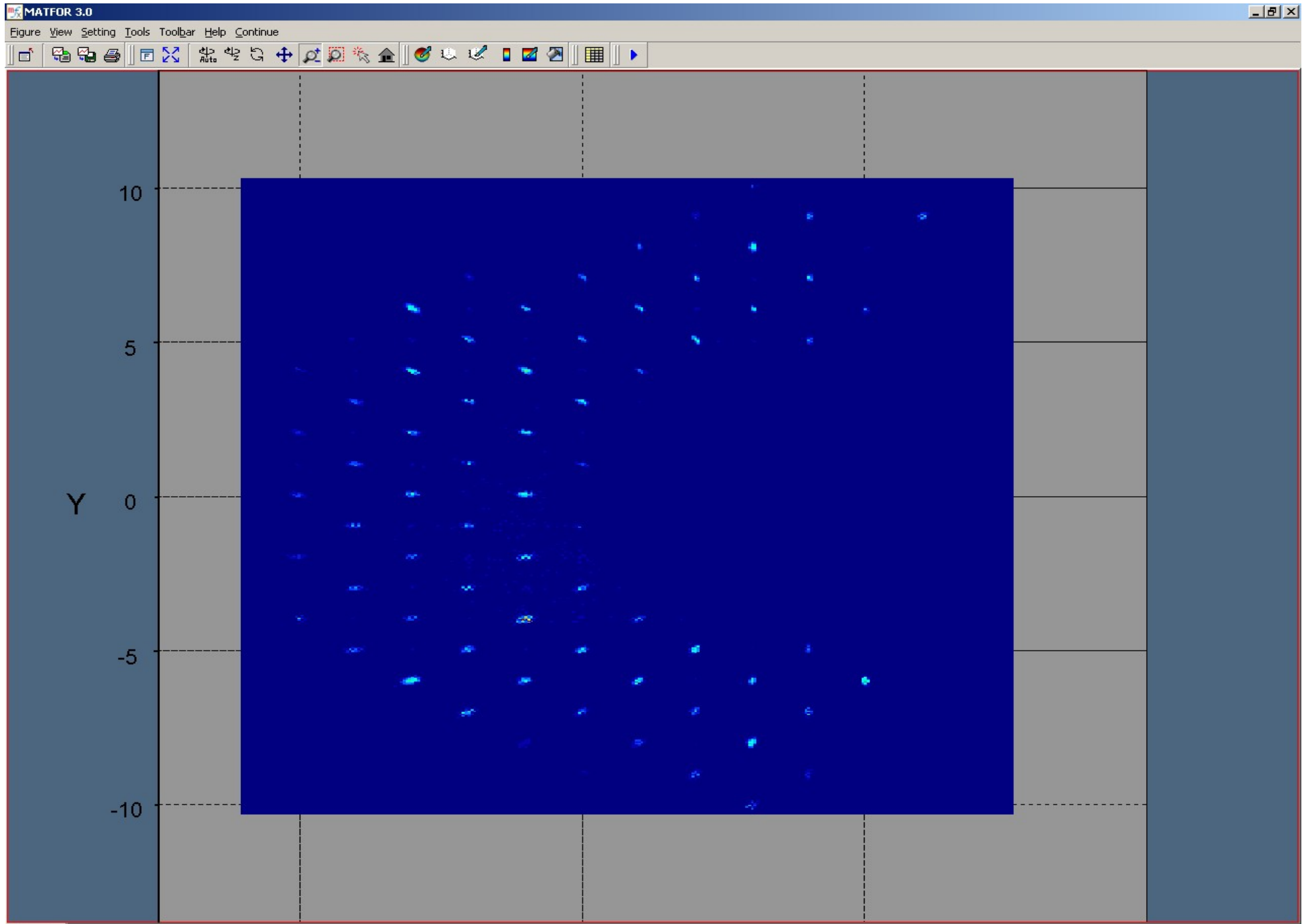
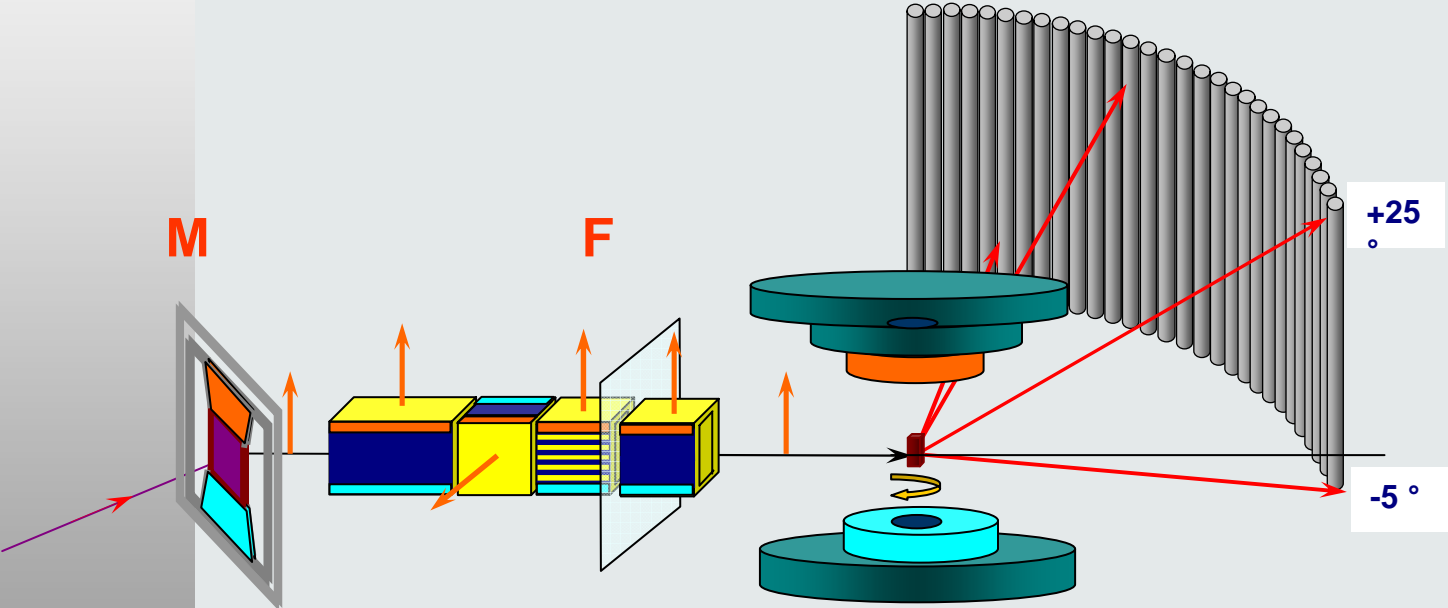
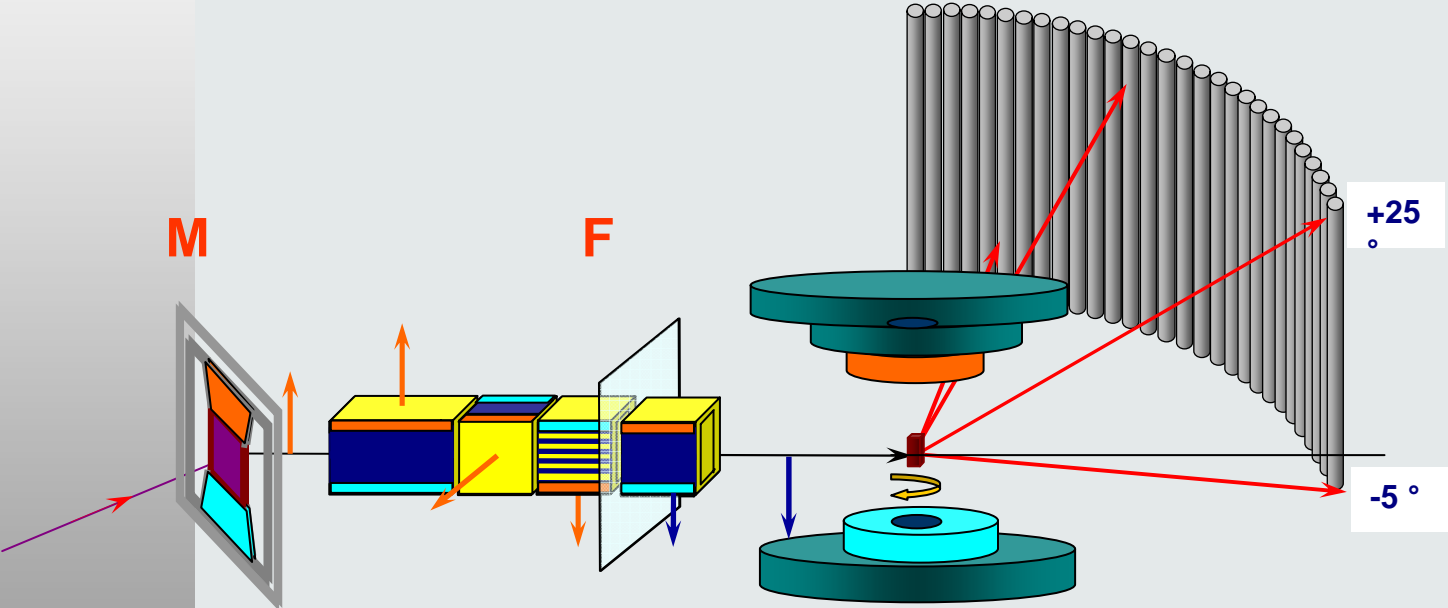


Figure 1

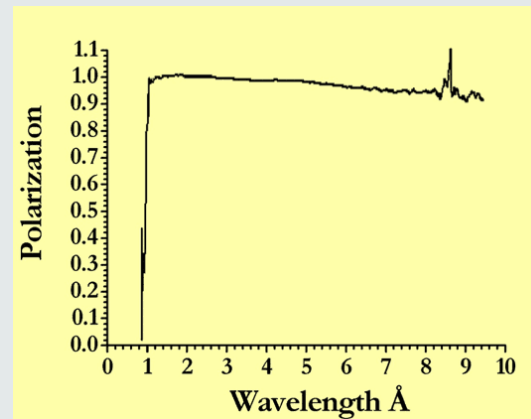
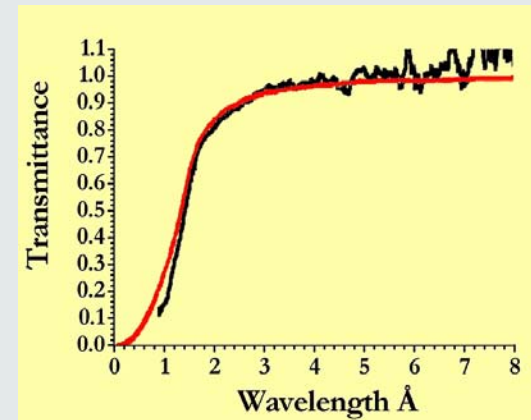
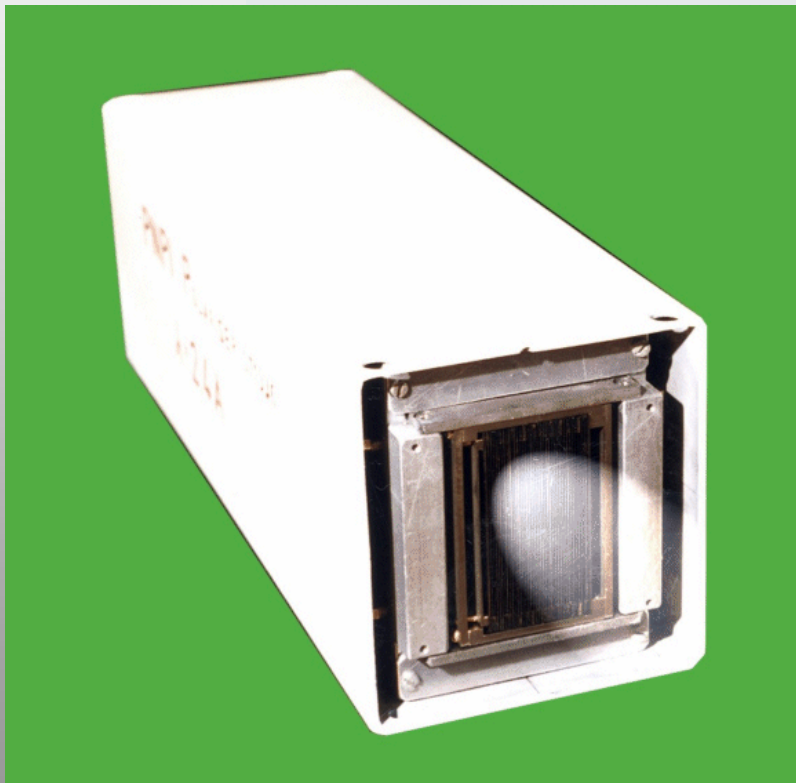
CRYOFLIPPER



CRYOFLIPPER



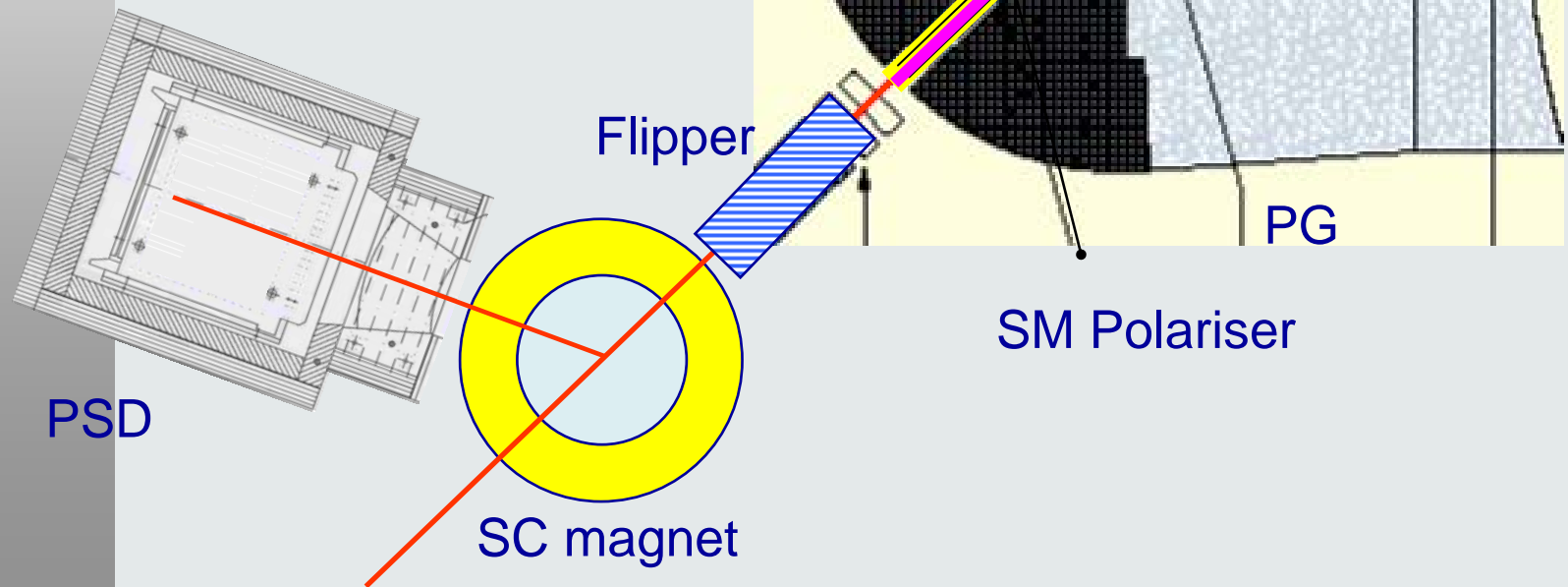
SUPERMIRROR BENDER, made in PNPI (Gatchina)



Very Intense Polarized Neutron Diffractometer

6T2 february 2006

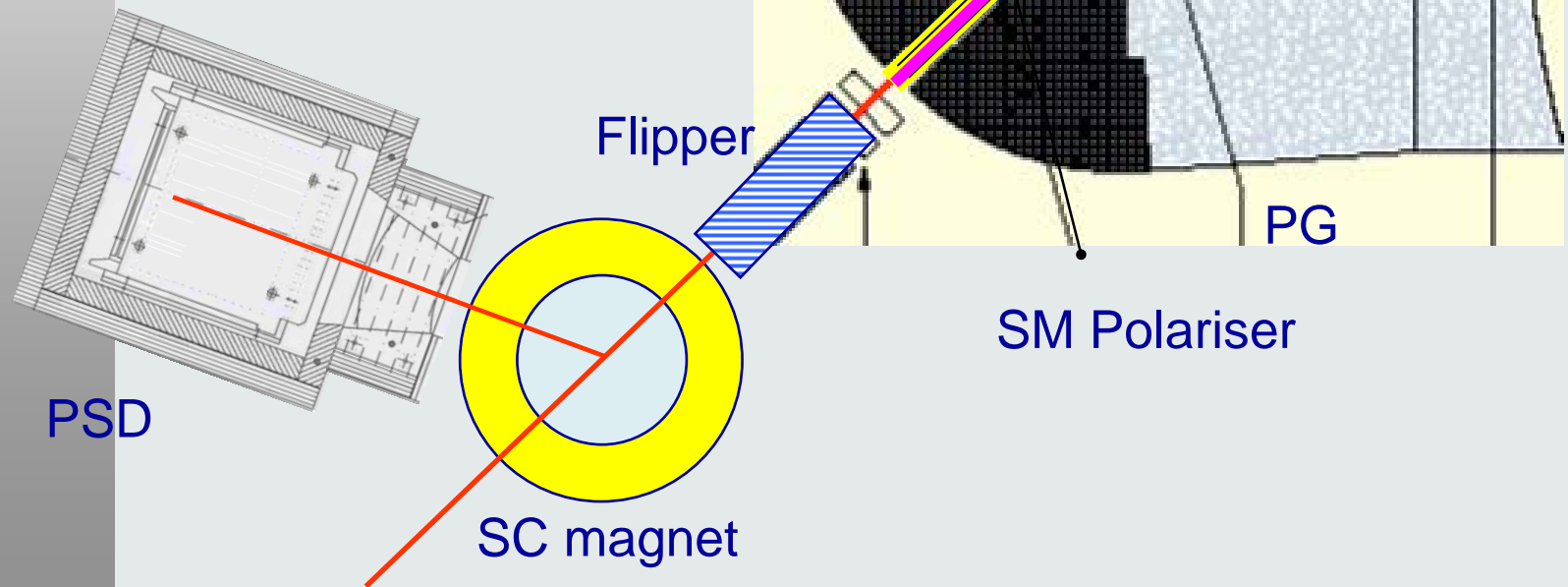
- 1.4 A, PSD mode
- 25x25° acceptance angle
- 7.5 T + 40 mK
- 7.5 T +10 Gpa+40 mK
- Laser, UV source



Very Intense Polarized Neutron Diffractometer

6T2 february 2006

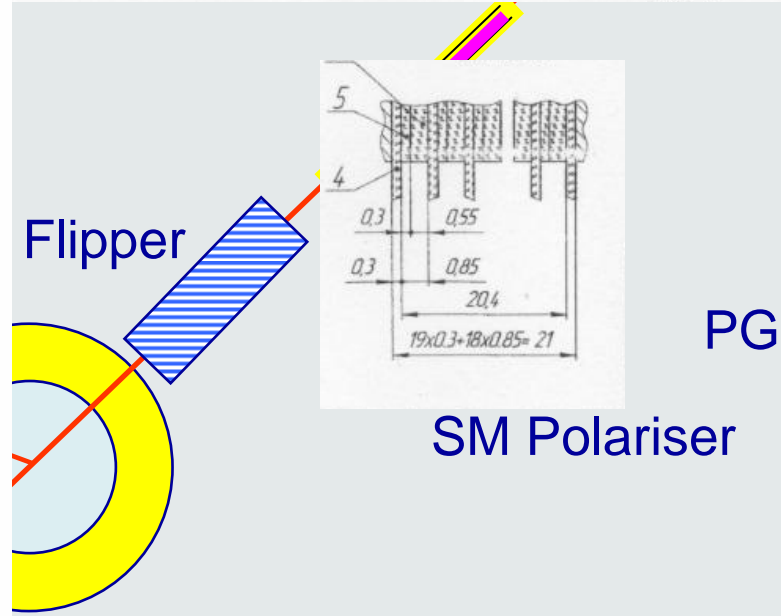
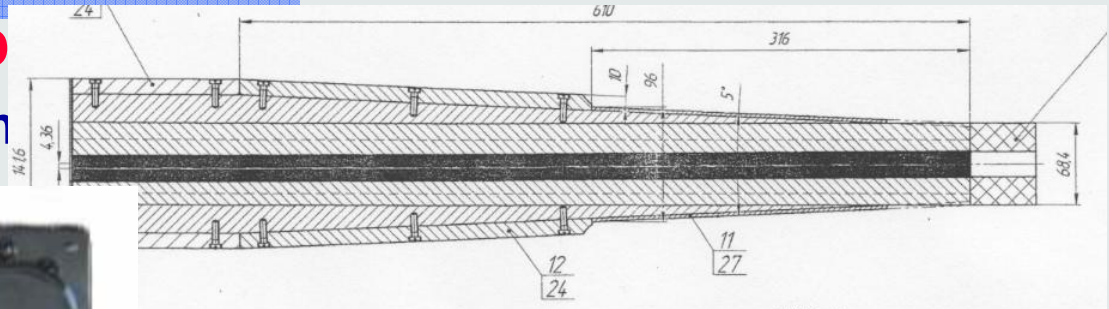
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- Laser, UV source



Very Intense Polarized Neutron Diffractometer

6T2 february 2006

- 1.4 A, PSD
- 25x25° acceptance angle



SC magnet

SM Polariser

PG

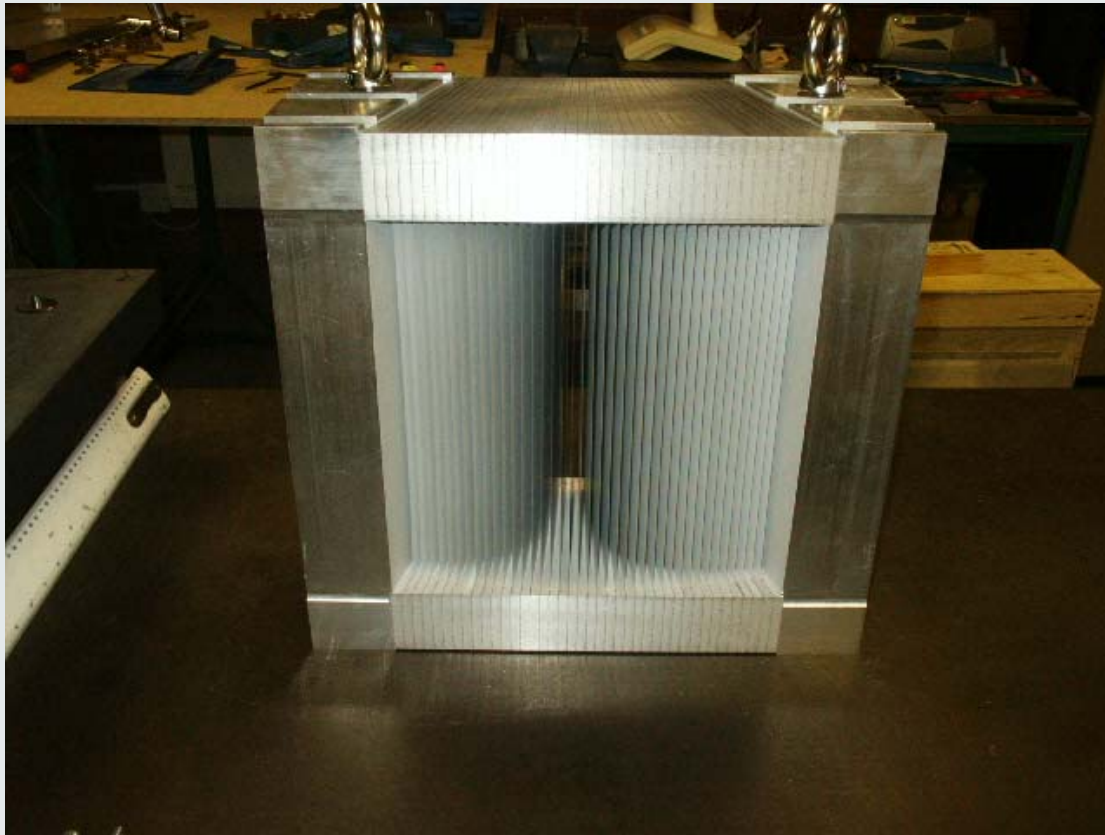
Very Intense Polarized Neutron Diffractometer

- 1.4 Å, PSD mode
- 25x25° acceptance angle

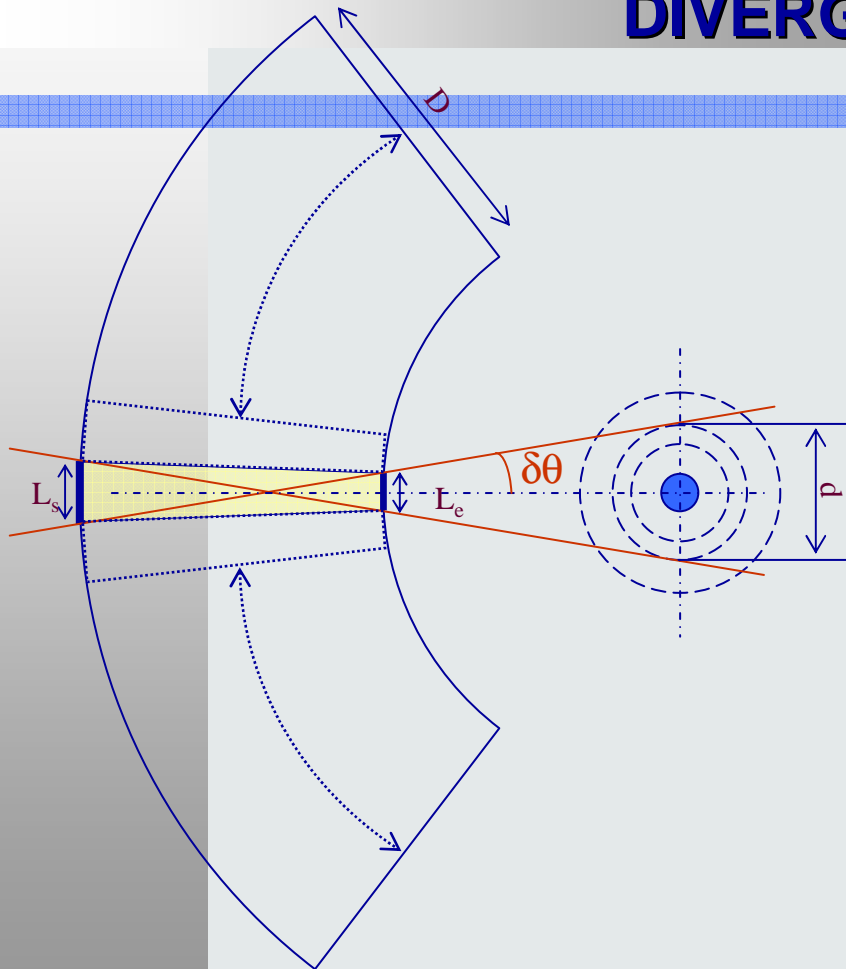


Very Intense Polarized Neutron Diffractometer

- **Radial Collimator**
- **25x25° acceptance angle**



LENGTH OF RADIAL COLLIMATOR AND ITS DIVERGENCE



$$\tan(\delta\theta) = \frac{L_e + L_s}{2.D}$$

$$\delta\theta = \frac{d - L_e}{2.D_{ec}}$$

$$D = \frac{L_e/2 + \tan(\beta/2).D_{ec}}{\tan(\delta\theta) - \tan(\beta/2)}$$

$$L_s = 2. \tan(\beta/2).(D + D_{ec})$$

L_e (mm)	L_s (mm)	β (°)	$\delta\theta$ (°)	D (mm)
7,05	15,23	1,15	1,71	355,48